

SNS COLLEGE OF TECHNOLOGY

**An Autonomous Institution
Coimbatore-35**



DEPARTMENT OF ARTIFICIAL INTELLIGENCE & DATA SCIENCE

23ADT202 – FUNDAMENTALS OF DATA SCIENCE AND ANALYTICS

II YEAR IV SEM

UNIT II – DESCRIBING VARIABILITY

Describing Variability

EMPATHY:

- Variability refers to the **divergence of data** from its mean value and is commonly used in the statistical and financial sectors.
- Variability shows how spread out the scores are in a distribution.

Scores: **10, 10, 10, 10** → no variability

Scores: **5, 10, 15, 20** → more variability

- Variability can be measured with the **range**, the interquartile range and the standard deviation.
- In each case, variability is determined by measuring distance.

Range

- The range is the total distance covered by the distribution, from the highest score to the lowest score (using the upper and lower real limits of the range).

Range=Maximum value - Minimum value

Merits :

- a) It is easier to compute.
- b) It can be used as a measure of variability where precision is not required.

Demerits :

- a) Its value depends on only two scores
- b) It is not sensitive to total condition of the distribution.

DEFINE:**Variance**

- Variance is the expected value of the squared deviation of a random variable from its mean.
- In short, it is the measurement of the distance of a set of random numbers from their collective average value.
- Variance is used in statistics as a way of better understanding a data set's distribution.
- Variance is calculated by finding the square of the standard deviation of a variable.

$$\sigma^2 = \frac{\sum (X - \mu)^2}{N}$$

IDEATE:

- In the formula above,
 μ - represents the mean of the data points,
 x - is the value of an individual data point and
 N - is the total number of data points.
- Data scientists often use variance to **better understand** the distribution of a data set.
- Machine learning uses variance calculations to make generalizations about a data set, aiding in a neural network's understanding of data distribution.
- Variance is often used in conjunction with probability distributions.

Standard Deviation

- Standard deviation is simply the square root of the variance.
- Standard deviation measures the standard distance between a score and the mean.

$$\text{Standard deviation} = \sqrt{\text{Variance}}$$

- The standard deviation is a measure of how the values in data differ from one another or how spread-out data is.
- There are two types of variance and standard deviation in terms of sample and population.

- The standard deviation measures **how far apart the data points** in observations are from each.
- we can calculate it by **subtracting each data point from the mean value and then finding the squared mean of the differenced values**; this is called Variance.
- The square root of the variance gives us the standard deviation.

PROTOTYPING:

Example 1: The heights of animals are: 600 mm, 470 mm, 170 mm, 430 mm and 300 mm. Find out the mean, the variance and the standard deviation.

Solution:

$$\begin{aligned}\text{Mean} &= 600 + 470 + 170 + 430 + 300 / 5 \\ &= 1970 / 5 = 394\end{aligned}$$

$$\sigma^2 = \frac{\sum (X - \mu)^2}{N}$$

$$\begin{aligned}\text{Variance} &= \frac{(600-394)^2 + (470-394)^2 + (170-394)^2 + (430-394)^2 + (300-394)^2}{5}\end{aligned}$$

$$\text{Variance} = 42436 + 5776 + 50176 + 1296 + 8836 / 5$$

$$\text{Variance} = 21704$$

$$\begin{aligned}\text{Standard deviation} &= \sqrt{\text{Variance}} = \sqrt{21704} \\ &= 142.32 \approx 142\end{aligned}$$