

Ch 2 – Equipotential surfaces

Equipotential surfaces:

- An equipotential surface is a surface on which the electric potential is the same at every point.

- **Properties:**

- (i) Potential difference on an equipotential surface is zero.

$$(\Delta V = V_2 - V_1 = 0)$$

Properties of equipotential surfaces:

(ii) Work done in moving a test charge on an equipotential surface is zero.(we know, potential difference is work done per unit charge)

- $W_{\text{ext}} = q \Delta V$
 $= q (v_2 - v_1)$
 $= q (0)$
 $= 0$

moving a test charge along an equipotential surface requires no work, as there is no change in electric potential

Properties of equipotential surfaces:

(iii) Electric field is always normal (perpendicular) to the equipotential surface at every point.

$$dw = F \cdot dr$$

$$= q E \cdot dr$$

Electric field is always perpendicular to the surface, that is displacement($\theta = 90^\circ$)

Therefore, $dw = 0$

$$W = 0$$

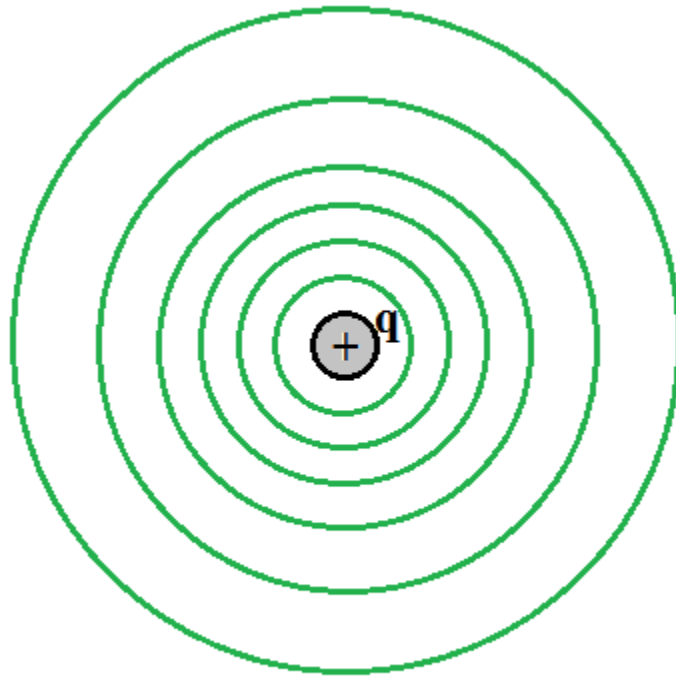
Properties of equipotential surfaces:

(iv) No two equipotential surfaces can intersect each other. Because at the same point, no two electric field lines can lie.

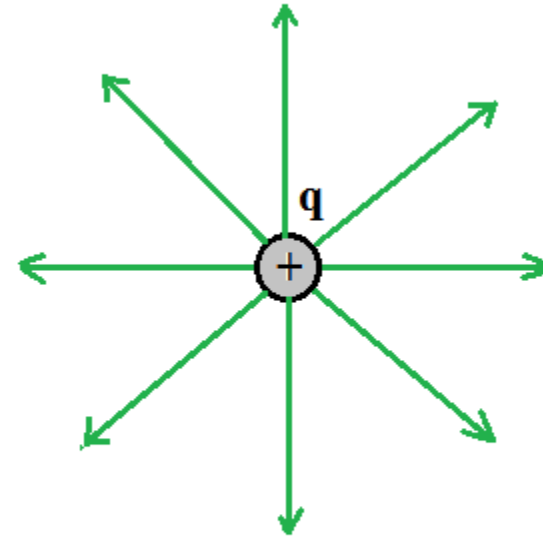
(v) Equipotential surfaces are closer together in regions of a strong field and further apart in the regions of a weak field.

$$dr \propto 1/E$$

Equipotential surfaces of a point charge(As the field gets weaker, distance between equipotential surfaces become larger)



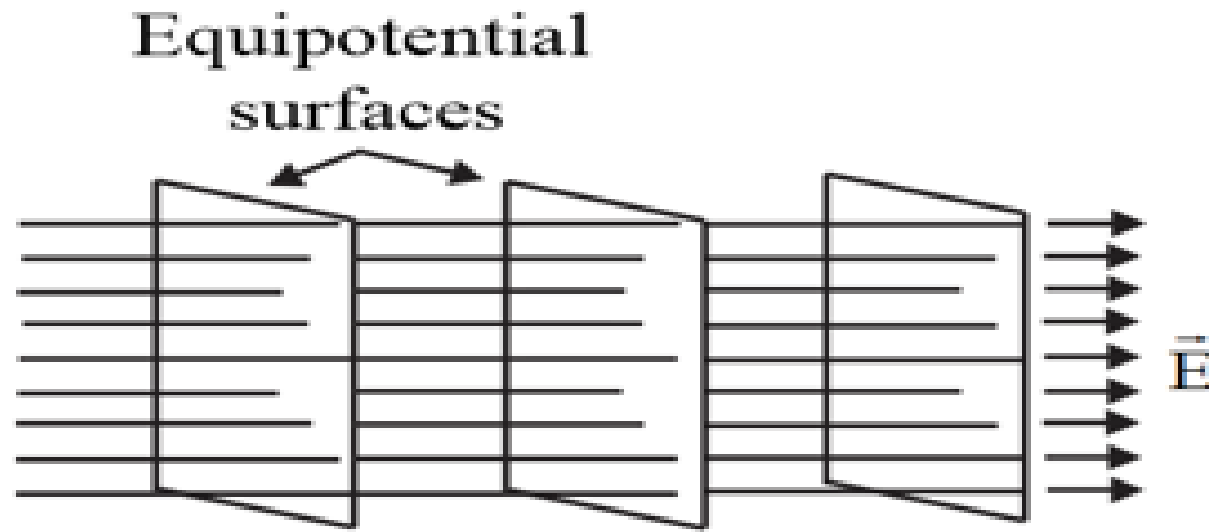
(a)



(b)

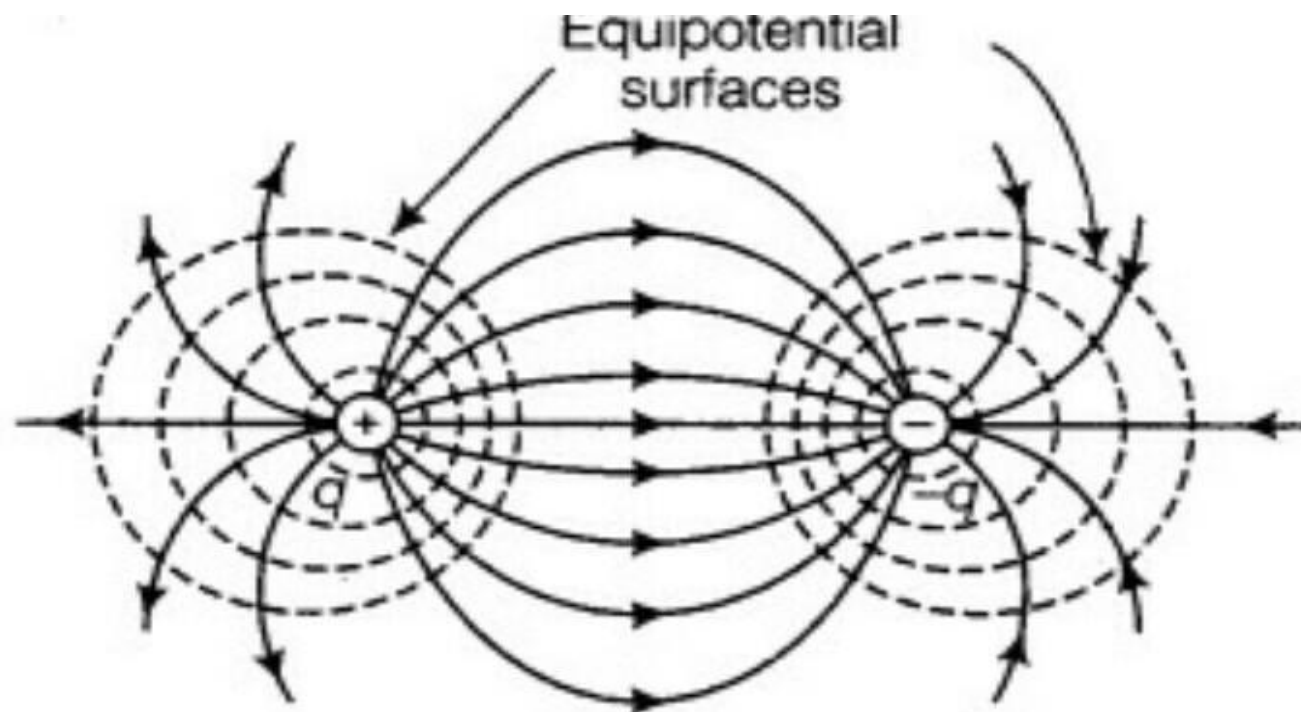
- As we move from one surface to the other surface, the electric potential decreases along the direction of the electric field.
- $V = kq / r$ (Note: The relation between V and r)

Equipotential surfaces for a uniform electric field:(flat plane surface)



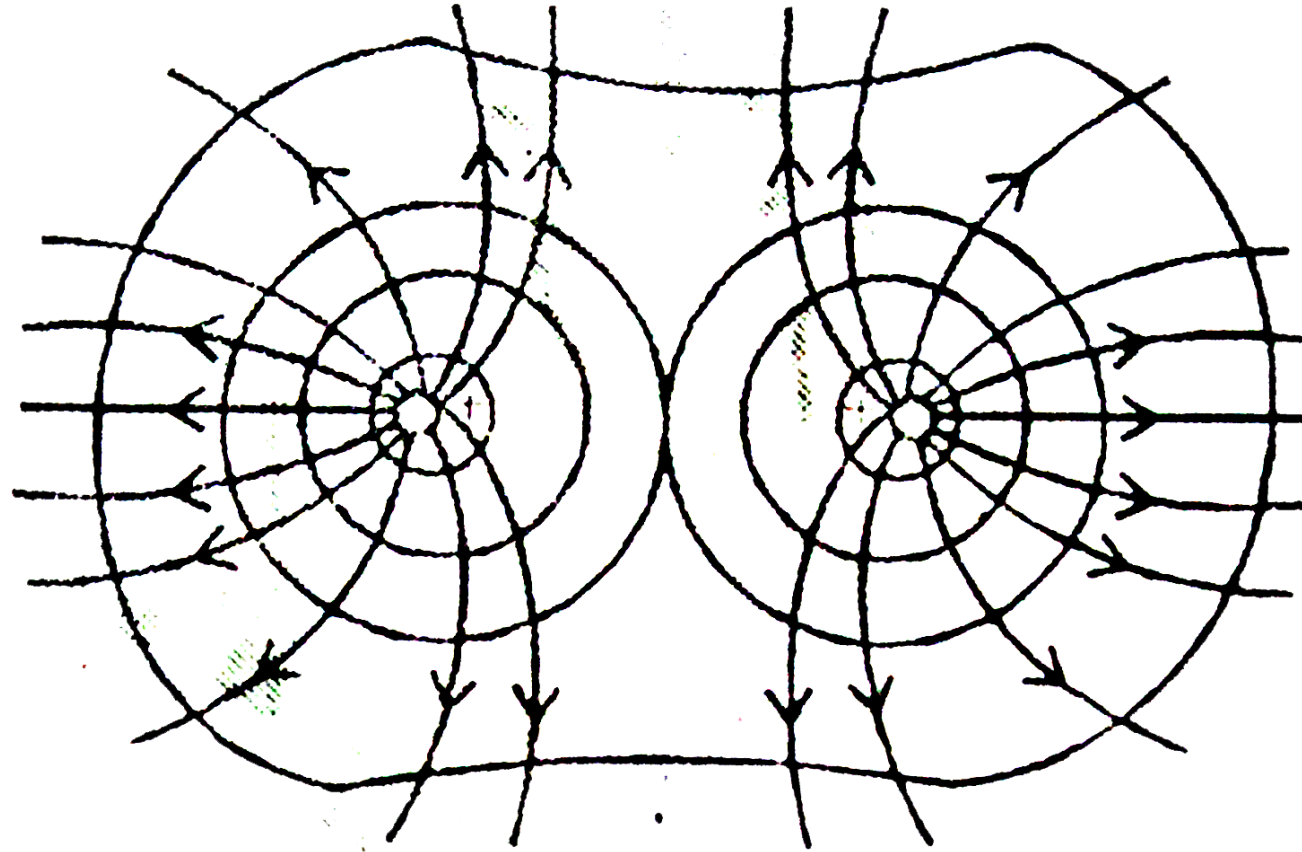
Equipotential surfaces for
uniform electric field

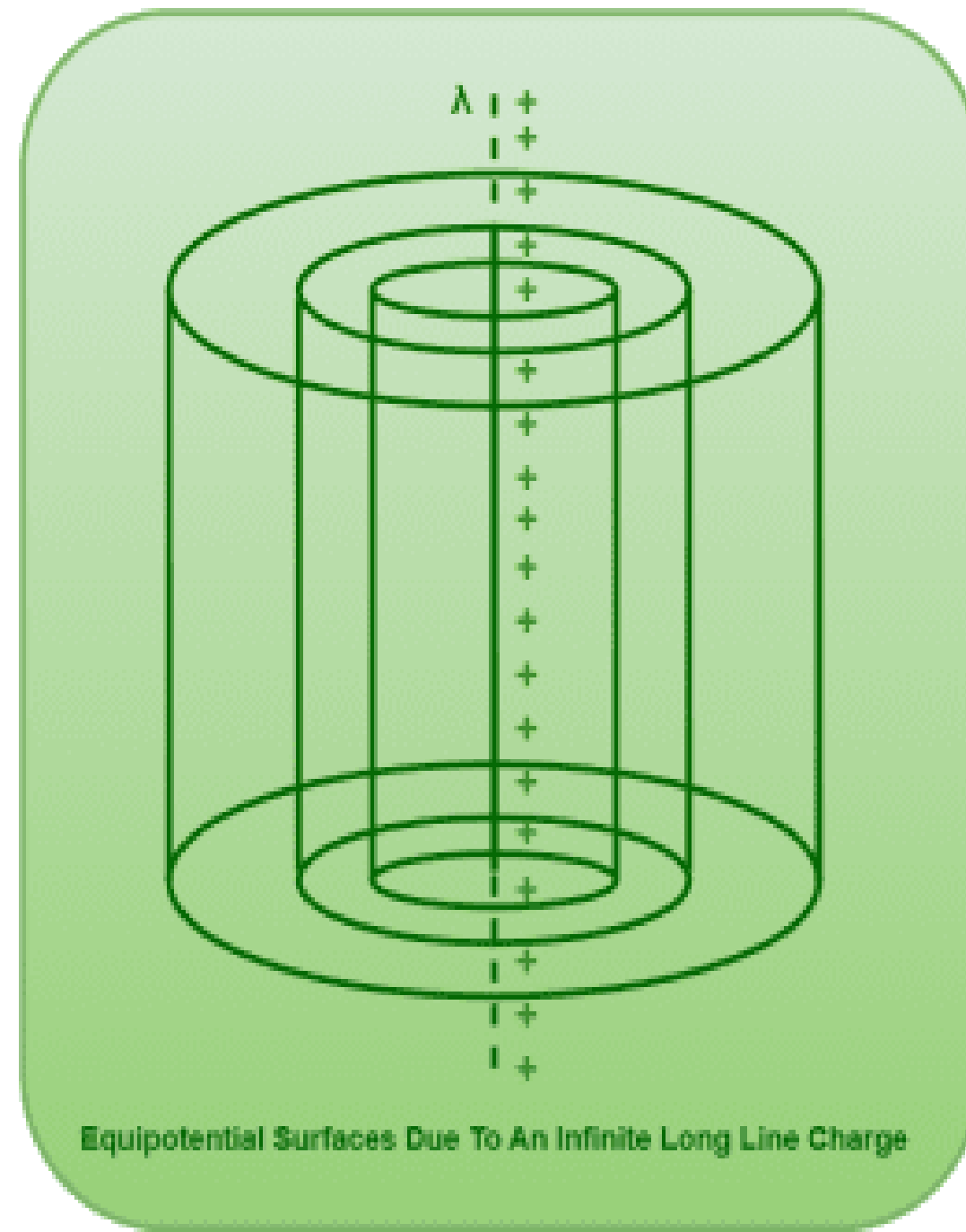
Equipotential surfaces for an electric dipole:



Equipotential surfaces due to an electric dipole

Equipotential surfaces of two equal positive point charges:





Equipotential Surfaces Due To An Infinite Long Line Charge