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AN AUTONOMOUS INSTITUTION



Approved by AICTE, New Delhi & Affiliated to Anna University, Chennai

Interpolation with unequal Intervals
Lagrange's Interpolation formula

Let y_0, y_1, \dots, y_n be $(n+1)$ points of a function $y = f(x)$ where $f(x)$ is assumed to be a polynomial in x , corresponding to arguments x_0, x_1, \dots, x_n , not necessarily equally spaced.

$$y = f(x) = \frac{(x-x_1)(x-x_2)\dots(x-x_n)}{(x_0-x_1)(x_0-x_2)\dots(x_0-x_n)} y_0$$
$$+ \frac{(x-x_0)(x-x_2)\dots(x-x_n)}{(x_1-x_0)(x_1-x_2)\dots(x_1-x_n)} y_1$$
$$+ \dots$$
$$+ \frac{(x-x_0)(x-x_1)\dots(x-x_{n-1})}{(x_n-x_0)(x_n-x_1)\dots(x_n-x_{n-1})} y_n$$

This is called the Lagrange's formula for interpolation.

Problems

① Using Lagrange's interpolation formula, find the value of y corresponding to $x = 10$ from the following data

x	: 5	6	9	11
y	: 12	13	14	16



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Given $x_0 = 5, x_1 = 6, x_2 = 9, x_3 = 11$
 $y_0 = 12, y_1 = 13, y_2 = 14, y_3 = 16$

By Lagrange's interpolation formula,

$$y(x) = \frac{(x-x_1)(x-x_2)(x-x_3)}{(x_0-x_1)(x_0-x_2)(x_0-x_3)} y_0$$
$$+ \frac{(x-x_0)(x-x_2)(x-x_3)}{(x_1-x_0)(x_1-x_2)(x_1-x_3)} y_1 + \frac{(x-x_0)(x-x_1)(x-x_3)}{(x_2-x_0)(x_2-x_1)(x_2-x_3)} y_2$$
$$+ \frac{(x-x_0)(x-x_1)(x-x_2)}{(x_3-x_0)(x_3-x_1)(x_3-x_2)} y_3$$

$y(10) = \frac{4 * 1 * (-1)}{(-1)(-4)(-6)} (12) + \frac{5(4)(-1)}{1(-3)(-5)} (13)$

$$+ \frac{5(4)(-1)}{4(3)(-2)} (14) + \frac{5(4)(1)}{6(5)(2)} (16)$$

$\therefore y(10) = \underline{\underline{14.67}}$

② Using Lagrange's interpolation formula, fit polynomial to the following data

x	0	1	3	4
y	-12	0	6	12