



SNS COLLEGE OF ENGINEERING
Kurumbapalayam(Po), Coimbatore – 641 107
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DEPARTMENT OF ARTIFICIAL INTELLIGENCE & DATASCIENCE



What is Regression?

What is regression?

	ENGINE SIZE	CYLINDERS	FUEL CONSUMPTION_COMB	CO2 EMISSIONS
0	2.0	4	8.5	196
1	2.4	4	9.6	221
2	1.5	4	5.9	136
3	3.6	6	11.1	265
4	3.5	6	10.6	244
5	3.5	6	10.0	230
6	3.5	6	10.1	232
7	3.7	6	11.1	265
8	3.7	6	11.6	267
9	2.4	4	9.2	?

Regression is the process of predicting a continuous value



Can we Predict?

- We can use the regression methods to predict a continuous value such as co2 emission
- In Regression there are two types of variables:
 - ✓ A Dependent variable and
 - ✓ One or more Independent variable
- Dependent variables are state, target and try to predict
- Independent variable are also known as explanatory variables can be the causes of those states

X: Independent variable

Y: Dependent variable

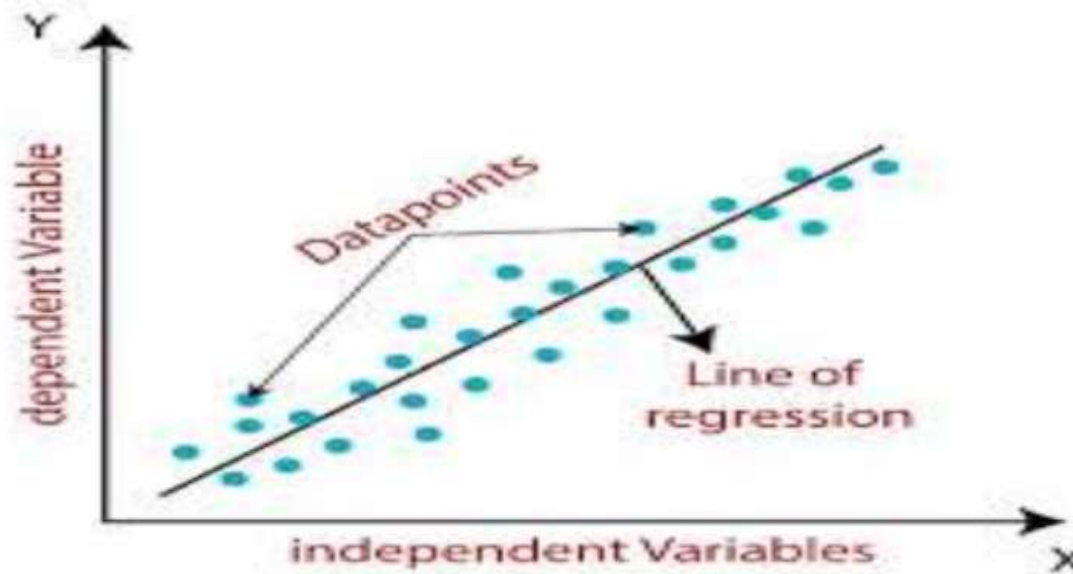
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Continuous Values

Regression is the process of predicting a continuous value

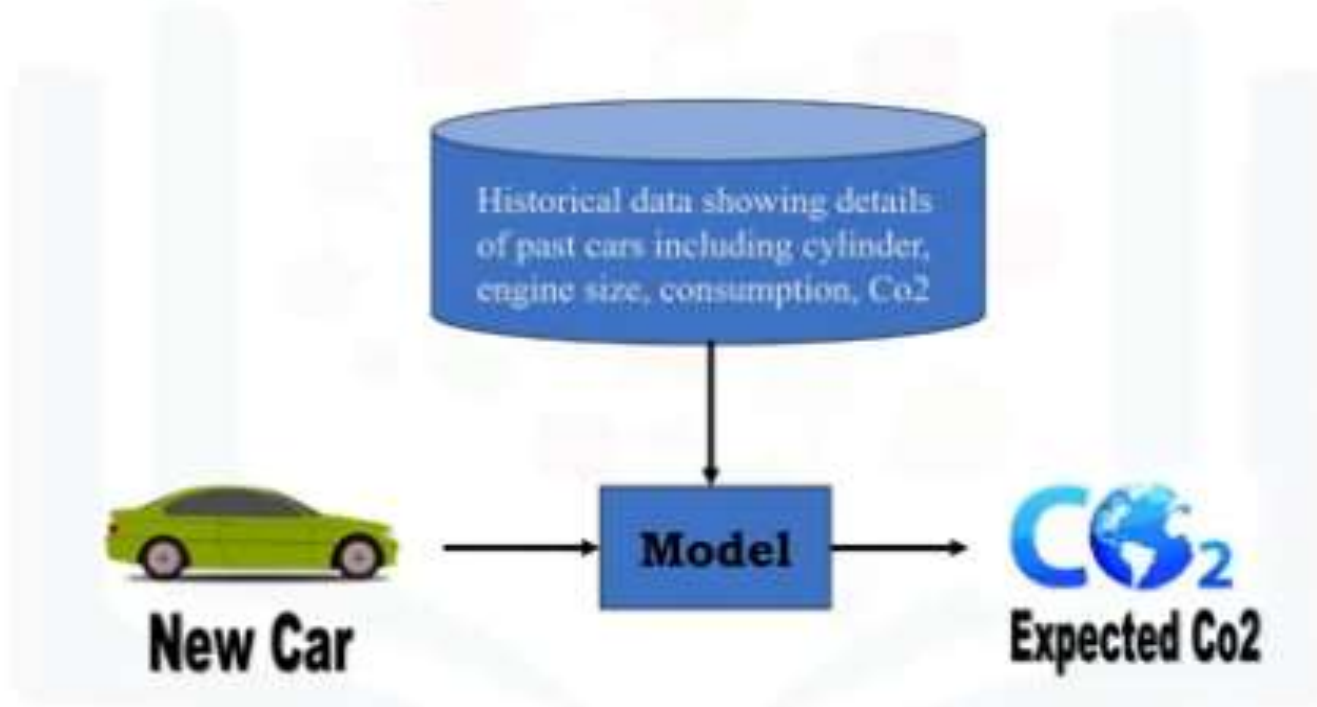


Line of Regression



- **Dependent value should be continuous** and cannot be a discrete value.
- The independent variable or variable can be measured on either a categorical, **or continuous measurement scale.**

What is a regression model?



1. We use regression to build such a regression estimation model,
2. Then the model is used to predict the expected CO₂ emission for a new, or unknown car.



REGRESSION TYPES

Types of regression models

- Simple Regression:

- Simple Linear Regression
- Simple Non-linear Regression

Predict **co2emission** vs **EngineSize** of all cars

- Multiple Regression:

- Multiple Linear Regression
- Multiple Non-linear Regression

Predict **co2emission** vs **EngineSize** and **Cylinders** of all cars



- **Simple regression** is when one independent variable is used to estimate a dependent variable.
- It can be either linear, or non-linear.
- For example, predicting CO₂ emission using the variable of **engine size**.
- When more than one independent variable is present the processes is called **multiple linear regression**.
- For example, predicting CO₂ emission using **engine size** and the **number of cylinders** in any given car.
- Again, depending on the relation between dependent and independent variables it can be either linear or nonlinear regression.



Linear regression

- Linear regression algorithm shows a linear relationship between a **dependent (Y) and one or more independent (X) variables**, hence called as linear regression.
- Since linear regression shows the linear relationship, which means it finds how the **value of the dependent variable is changing according to the value of the independent variable**.

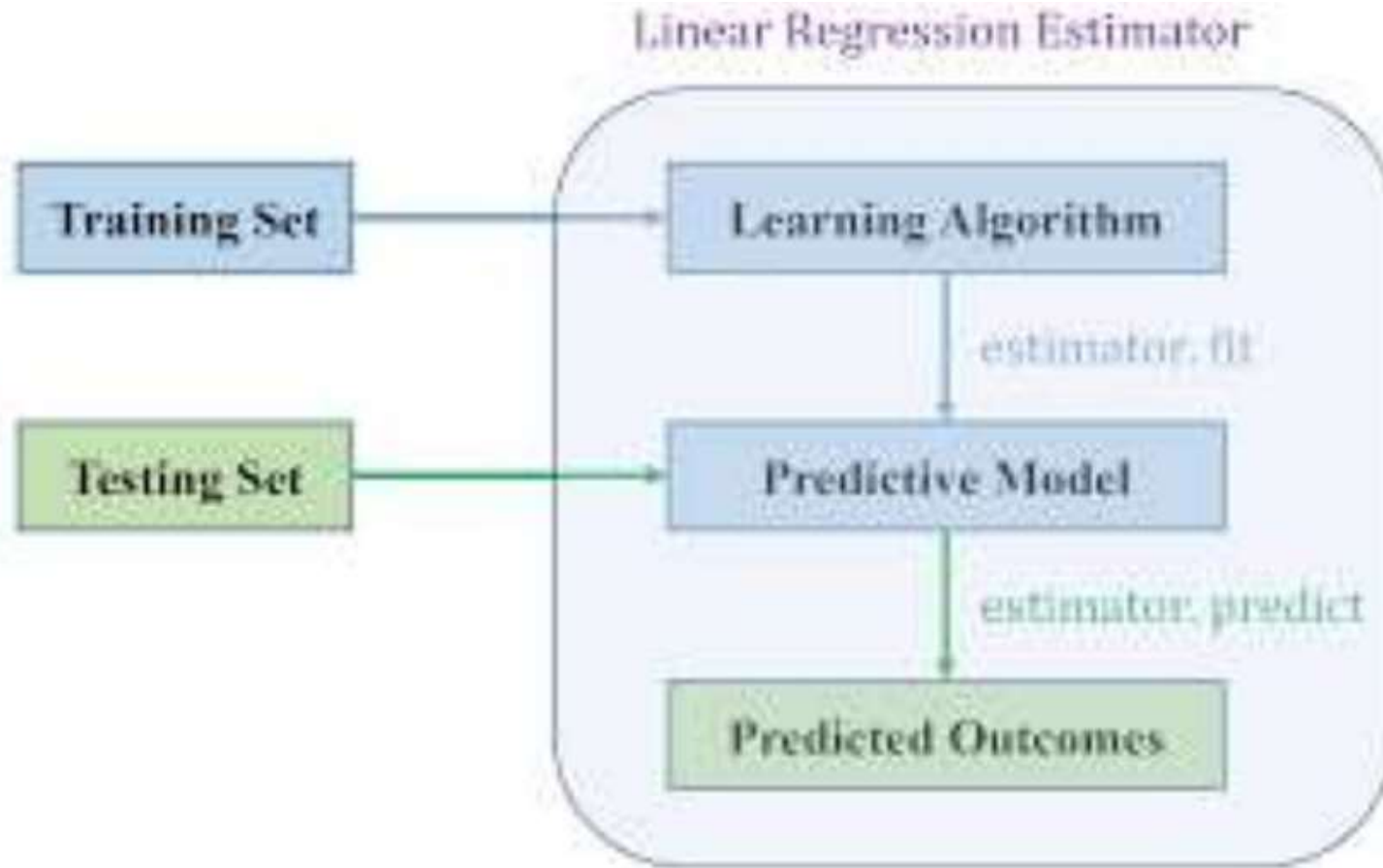


Linear models for Regression

- Linear Regression is a machine learning algorithm based on supervised learning. It performs a **regression task**.
- Regression models are a **target prediction value** based on independent variables.
- Linear regression is one of the **easiest and most popular Machine Learning algorithms**.
- It is a **statistical method** that is used for predictive analysis.
- Linear regression makes predictions for continuous/real or numeric variables such as **sales, salary, age, product price, etc**



Linear Regression Estimator





Examples

Applications of regression

- Sales forecasting
- Satisfaction analysis
- Price estimation
- Employment income



Algorithms

Regression algorithms

- Ordinal regression
- Poisson regression
- Fast forest quantile regression
- Linear, Polynomial, Lasso, Stepwise, Ridge regression
- Bayesian linear regression
- Neural network regression
- Decision forest regression
- Boosted decision tree regression
- KNN (K-nearest neighbors)



- Mathematically, we can represent a linear regression as:
 - $y = a_0 + a_1 x + \epsilon$ Here,
- Y= Dependent Variable (Target Variable)
- X= Independent Variable (predictor Variable)
- a_0 = intercept of the line (Gives an additional degree of freedom)
- a_1 = Linear regression coefficient (scale factor to each input value).
- ϵ = random error
- The values for x and y variables are training datasets for Linear Regression model representation



DEFINITIONS

- Simple Linear Regression: If a single independent variable is used to predict the value of a numerical dependent variable, then such a Linear Regression algorithm is called Simple Linear Regression.
- Multiple Linear regression: If more than one independent variable is used to predict the value of a numerical dependent variable, then such a Linear Regression algorithm is called Multiple Linear Regression



Linear Regression Line

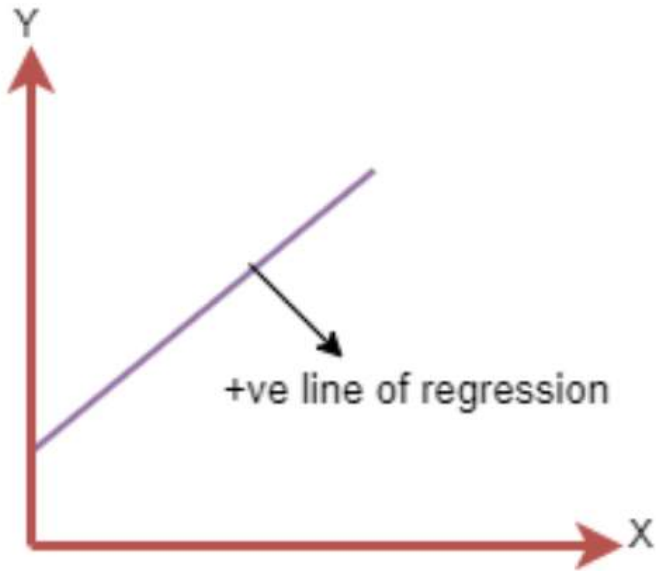
- Linear Regression Line A linear line showing the relationship between the dependent and independent variables is called a regression line.
- A regression line can show two types of relationship
 - Positive Linear Relationship
 - Negative Linear Relationship

- **Positive Linear Relationship:**

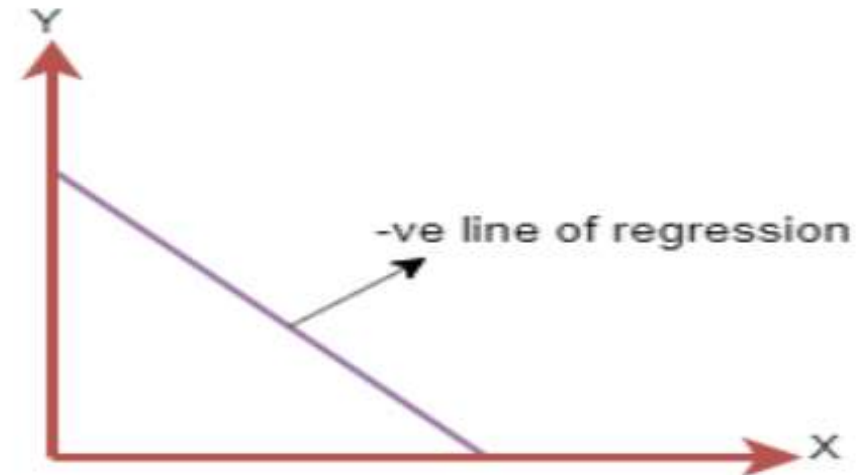
If the dependent variable increases on the Y-axis and independent variable increases on X-axis, then such a relationship is termed as a Positive linear relationship

- Negative Linear Relationship:

If the dependent variable decreases on the Y-axis and independent variable increases on the X-axis, then such a relationship is called a negative linear relationship.



The line equation will be: $Y = a_0 + a_1X$



The line of equation will be: $Y = -a_0 + a_1X$