

It is a palt of a sentence that certains



predicate calculus puro

and problècate. Subject does on a porce

Priedecate

A part of a declarative sentence descipping the proposition of an object (09) relation among object is called a predicate.

Fg: Ram 18 a 10911 B(2) J. Tigos is an wild animal. It is denoted by P(5).

al sam is poor and Ram is intelligent

It is denoted by P(S) A I(8)

Quartages:

Quantifier is the one which is used to quantity the nature of variables.

Types of quantifier: J. Unriversal quantifies (toc) or (x)

The quantifier "for all x" is called ungversal quantifiel.

Eg: I for all x, or is an integer In symbolic forms +xx, I(x)

2). Every apple is sed.

For all x, 96 x 18 an apple then x 18 (tro) [A(x) -> R(x)] Hed.





J. Exerctentfal quantifier: (Jx) The quantifier "for some x" is called the exactantial quantifier. Eg: some men ave Intelligent There exist an or such that x is a man and or is intelligent. (Fx) (M(x) / I(x))

Bound and force variables: The variable is said to be bound 9% It is concerned with either whilesal (+21) on existential (Jx) quantities.

Otherwase It is called brice variable. Super of the Supe of the quantifier is the too mula to 110 wing the quantifier (x) P(x,y) => x 的 bound variable y is brief voortable prx, y) 98 the scope of the quantifect.

Theory of Inference for Predecate easculus

J. UARVELSAL Specification [US Rule]

 $(\forall x) P(x) \Rightarrow P(y)$ J. Universal Generalization [UG Rule]

P(y) => (+x) P(x)

Existential speatication [Es Rule]

(Jx) P(x) => P(y)

H. Existential Generality atten [EGI Rule]

 $P(y) \Rightarrow (\exists x) P(x)$





```
1. Show that (Jx) M(x) follows loggically
   (x) [H(x) + M(x)], (fx) H(x)
    Step piemises Rule
    1. (\alpha) [H(\alpha) \rightarrow M(\alpha)]
\{i\} &. H(y) \rightarrow M(y)

3. (\exists x) H(x)

\{i\} 4. H(y)

\{i\} M(y)
                           ES
                          E61
    6. (FOU M(O1)
  2. All humans are mortal. Sachen is a human
  Therefore he is mostal.
        H(21): x 98 a human
  M(x): x "18 Morstal
H(6): Sachen 18 a buman
    The premeses wie.
      (4x) [H(x) -> M(x)], H(5)
     (wholu shon: M(5)
     1. (+x)[H(x) -> M(x)] P
                M(S)
  3. Show that the premises, "one Student in this
    class knows how to write programs 9n JAVA "a
   "Everyone who knows how to weste program in
   JAVA can get a high-paying 306" amply the
    Conclusion "some one 90 this class can got a
                          high - paying dets ".
                                    Scanned with CamScanner
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Let A(x): x 98 90 +695 clougs
           J(21): x knows how to write program 90 JAVA
           H(x): 2 can get a high paying got.
     The premises are,
       [f_{\mathcal{X}})(A(x) \wedge J(x)), (\forall x)(J(x) \rightarrow H(x))
     Copolu Scon: Fx (A(x) A H(x))
                                 Rule
              piemisos
     Step
         (\exists x) (A(x) \wedge J(x)) \qquad P
A(y) \wedge J(y) \qquad E(x)
T \qquad A(y) \wedge J(y) \Rightarrow A(y)
 {i} &. A(y) ∧ J(y)
 fay 3. A(y)
                 J(4)
     S. (4a) (J(x) > H(x))
 ₹53 6. J(9) → H(4)
     7. H(Y)
$3, Ty 8. A1Y) A1Y)
         (DX) (AID) EG
 4]. veryy the valldety of the following argument.
  "Every Aving thing is a plant or an animal"
  "John's gold flat is alre and & & not a plant"
  "All ausmals bave hearts". Therefore, " John's
   gold best bas a beart".
      L(x1): x & a 1949ng thang L(j): j93 attre
P(x): x & a plant P(j): j is not a plo
A(x): x & an animal
H(71): x & a heart H(j): j has a
heart
                                     PG): jis not a
  GIVN: (+x) [L(x) + P(x) V A(x)]
           LG) ATP(J), (4x) [A(x) > H(x)]
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	The contract of the contract o	
Con Clus	sion: H(j)	
Step	Priemises	Rule
1.	(Ya) [L(x) -> P(x) VA(x)	J P
١٦ 2.		US
3.	$L(j) \to p(j) \vee A(j)$	Р
	L(j) n TP(j)	T PAR > P
£334.	r(j)	T P, P>Q >Q
叙州35	1,954,149	T PARENTPVR
gsy 6.	TP(j) -> A(j)	P
7. (4	FX) [AIXI > H(X)]	115
18 y 8.		2 E G 3 C 1 2 C 1
9.	7 P(j) -> H(j)	T PNQ => P, Q
533 10.	7 P(j)	T P, P-) Q => Q
11.	Hg)	A SECTION AND A
		HANDE THE
De S €		(a) Egg." "some
1 1	lock mouse is lock	d music, loud music
5]. Al	LOCK MEDGE 33 1000 music except " Therefore	se some
exes.	1 "	1.090
6703	0. 0 1000	me 1994
	R(x): $x > 8$ a loud (Sex (See)
Givn.	Decer.v. 6 [50] \$ [80] [78	(x)
	$(\forall x) [R(x) \rightarrow L(x)], (\exists$	(x) their male
Conclu	1 55(1)	by forther place
	$(4x) (R(x) \rightarrow L($	x)) P
£13	$\begin{array}{cccc} 1. & (430) & (100) \\ 2. & & R(4) \rightarrow & L(4) \end{array}$	() (K) Proloubres
	3. (Fx) R(x)	ES
433	4. R(Y)	T
र्2,43	5.	EG
	6. (Jx) L(x)	





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6] Establish the validity of argument.
    i). All antogers are eathernal not
    ii) some antogers are power of three.
   111). Therefore some sational numbers are
       Power of 3.
    I(x): of is an integer
    R(x): 21 % an eathoral number
    P(x): of 98 power of 3.
    Brun (tr) (I(x) + R(x)), (fx) (I(x) A P(x))
   conclusion: (Fx) [R(x) 1 P(x)]
                                  Rule
     Stop
               Premases
        (\forall x) [I(x) \rightarrow R(x)]
                                   US
  £13 2.
              T(y) \rightarrow R(y)
         (FX) [I(X) AP(X)]
  £394.
                                  ES
              I(9) 1 P(9)
                                     PAR => PER
                I(Y)
                R19)
                P(y)
76,73 8. R(4) 1 P.(4)
       (Fx) [R(xx) AP(xx)]
J. Show that (x) [ P(x) VQ(x)]
   Premases: (x) [P(x) Va(x)]
   Conclusion: (x) P(x) V (7x) Q(x)
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Stop 1. 23. 23. 24. 25. 25. 25. 25. 25. 25. 25. 26. 27. 27. 29. 29. 20. 20. 20. 20. 20. 20. 20. 20	PROMPERS (X) [P(X) V R(X)] P(Y) V R(Y) T[(X) P(X) V (FX) R(X)] (FX) P(X) V (FX) R(X) (FX) P(X) (FX) P(X) (F(Y) (X) T R(X) T R(Y) T R(Y) T R(Y) TP(Y) V R(Y) T(P(Y) V R(Y)) [P(Y) V R(Y)] \ T [P(Y) V R(X)	Pule P US Nogation of conclusion T T(PAR) ATPYTR T PARAPR US T PARAPR
を 1. 2099 (サマンドア (サマンドア (サマンドア まなりる よ。 を 13. 45 を 13. 6. で 15. 63 T.	Forg cp sule, obtain the to $[xx) \rightarrow a(x)$], $[+x)[x] \rightarrow 7$ $[xx) \rightarrow a(x)$], $[+x)[x] \rightarrow 7$ $[+x][x] \rightarrow a(x)$	m son pratton





$$\{4,73 \ 8. \ R(y) \rightarrow 7P(y) \ CP$$
 $\{83 \ 9. (\forall x) [R(x) \rightarrow 7P(x)] \ UG$