Solving Oifferent al Equation using Laplace Transforr

Shifting property of Unilateral Laplace Transform.

\* 
$$L\left(\frac{d}{dt} \times (t)\right) = S \times (S) - x(O)$$

$$\star \left[ \frac{d^2}{dt^2} \times (s) \right] = s^2 \times (s) - s \times (s) - x'(s)$$

$$\star L \left[ \frac{d^3}{dt^3} x(t) \right] = S^3 x(S) - S^2 x(S) - S x'(S) - x''(S)$$

) solve using Differential Equation  $\frac{d}{dt}y(t) + 5y(t) = x(t)$  with initial condition  $y(\bar{0}) = -2$  and  $i/p x(t) = 3e^{2t}u(t)$ 

$$\frac{d}{dt} y(t) + 5y(t) = x(t)$$

$$Y(S) [S+5] = \frac{3}{S+2} - 2$$

$$\frac{3}{(3+2)(5+5)} = \frac{A}{5+2} + \frac{B}{5+5}$$

$$3 = B(-3)$$

$$Y(S) = \begin{bmatrix} \frac{1}{S+2} & -\frac{1}{S+5} \end{bmatrix} - \frac{2}{S+5}$$

$$y(s) = \frac{1}{s+2} - \frac{3}{s+5}$$

system Transfer Function :=

H(S) = 
$$\frac{V(S)}{X(S)}$$
 -> system Transfer Function

Freq Response :-

O The input output relation of a System at hibal nest is given by  $\frac{d^2}{dt^2}y(t) + 4\frac{d}{dt}y(t) + 3y(t) =$ 

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$$H(S) = \frac{Y(S)}{X(S)} = \frac{S+2}{S^2+4S+3}$$

Freq Response:-

$$H(jw) = \frac{y(jw)}{x(jw)} = \frac{jw+2}{(jw)^2 + 4jw+3}$$

Impulse Response:

$$H(S) = \frac{S+2}{S^2+4S+3}$$

$$\frac{S+2}{(S+3)(S+1)} = \frac{A}{S+3} + \frac{B}{S+1}$$

$$H(S) = \frac{1}{2(S+3)} + \frac{1}{2(S+1)}$$

$$h(t) = \frac{1}{2} L^{-1} \left( \frac{1}{S+3} \right) + \frac{1}{2} L^{-1} \left( \frac{1}{S+1} \right)$$

$$h(t) = \frac{1}{2} e^{-3t} u(t) + \frac{1}{2} e^{-t} u(t)$$

The Differential Equation of a system is given commons

$$\frac{d^2}{dt^2}y(t) + 3\frac{d}{dt}y(t) + 2y(t) = x(t) \text{ with Initial}$$
conditions  $y(0^+) = 3$ ,  $y'(0^+) = -5$ . Determine the ope
for the  $i|p = x(t) = 2u(t)$ 

$$s^{2}y(s) - sy(o^{-}) - y'(o^{-}) + 3[sy(s) - y(o^{-})] + 2y(s) = x(s)$$
  
 $s^{2}y(s) - 3s + 5 + 3[sy(s) - 3] + 2y(s) = x(s)$ 

$$s^2 y(9) - 35 + 5 + 3 8y(9) - 9 + 2y(9) = x(9)$$

$$Y(S) \left[ S^2 + 3S + 2 \right] - 3S - 9 + 5 = X(S) - Y(S) \left[ S^2 + 3S + 2 \right] = \frac{2}{5} + \left[ \frac{3S + 4}{5} \right]$$

$$y(S) = \frac{2+3S^2+4S}{S(S+1)(S+2)}$$

$$S = -1$$

$$S = -2$$

$$S = -2$$

$$A = 1$$

$$Y(9) = \frac{1}{S} - \frac{1}{S+1} + \frac{3}{S+2}$$

$$= L^{-1}(\frac{1}{S}) - L^{-1}(\frac{1}{S+1}) + 3L^{-1}(\frac{1}{S+2})$$

$$\Rightarrow Y(t) = u(t) - e^{-t} u(t) + 3e^{-2t} u(t)$$