



**DEPARTMENT OF MATHEMATICS**

**UNIT - IV INTERPOLATION , NUMERICAL DIFFERENTIATION  
& INTEGRATION**

**NUMERICAL INTEGRATION BY SIMPSON'S 1/3 RULE**

**SIMPSON'S 1/3 RULE:**

$$\int_{x_0}^{x_n} y \, dx = \frac{h}{3} [(y_0 + y_n) + 4(y_1 + y_3 + \dots + y_{n-3}) + 2(y_2 + y_4 + \dots + y_{n-2})]$$
$$= \frac{h}{3} [A + 4B + 2C]$$

where A = Sum of the first & last ordinates

B = Sum of the odd ordinates

C = Sum of the even ordinates

(ie) an even number of equal sub-intervals.

Dividing the range into 10 equal parts, find the value

of  $\int_0^{\pi/2} \sin x \, dx$  by Simpson's 1/3 rule



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Soln:

$x$	:	0	$\pi/20$	$2\pi/20$	$3\pi/20$	$4\pi/20$	$5\pi/20$
$y = \sin x$	:	0	0.1564	0.3090	0.4540	0.5878	0.7071
$x$	:	$6\pi/20$	$7\pi/20$	$8\pi/20$	$9\pi/20$	$10\pi/20$	
$y = \sin x$	:	0.8090	0.8910	0.9511	0.9877	1	

By Simpson's  $\frac{1}{3}$  rule,

$$\int_0^{\pi/2} \sin x dx = \frac{h}{3} [(y_0 + y_{11}) + 4(y_1 + y_3 + y_5 + y_7 + y_9) + 2(y_2 + y_4 + y_6 + y_8 + y_{10})]$$
$$= \frac{\pi}{20} \cdot \frac{1}{3} [(0 + 1) + 4(3.1962) + 2(2.6569)]$$
$$= 1.0000$$



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Find the value of  $\log_e 5$  from  $\int_0^5 \frac{dx}{4x+5}$  by Simpson's  $\frac{1}{3}$  rule ( $n=10$ ).

Soln: Here  $y(x) = \frac{1}{4x+5}$

$$h = \frac{5-0}{10} = \frac{1}{2} = 0.5$$

$x$ :	0	0.5	1	1.5	2	2.5	3	3.5	4
$y$ :	0.2	0.1429	0.1111	0.0909	0.0769	0.0667	0.0588	0.0526	0.047
			4.5	5					
			0.0434	0.04					

By Simpson's  $\frac{1}{3}$  rule,

$$\int_0^5 \frac{dx}{4x+5} = \frac{h}{3} [(y_0 + y_n) + 2(y_2 + y_4 + y_6 + \dots) + 4(y_1 + y_3 + y_5 + \dots)]$$



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### UNIT - IV INTERPOLATION , NUMERICAL DIFFERENTIATION & INTEGRATION

$$= \frac{1}{6} [2.4148]$$
$$= 0.4025 \text{ --- (1)}$$

$$\int_0^5 \frac{dx}{4x+5} = \frac{\log(4x+5)}{4} \Big|_0^5$$
$$= \frac{1}{4} (\log 25 - \log 5)$$
$$= \frac{1}{4} \log \left(\frac{25}{5}\right)$$
$$= \frac{1}{4} \log 5 \text{ --- (2)}$$

From (1) & (2)

$$\Rightarrow \frac{1}{4} \log 5 = 0.4025 \quad \log e$$

$$\Rightarrow \log 5 = 1.61$$

Using Simpson's  $\frac{1}{3}$  rule, evaluate

$$\int_0^{1.2} e^{-x^2} dx, \text{ taking } h=0.2.$$