

## SNS COLLEGE OF TECHNOLOGY



(An Autonomous Institution) Coimbatore-641035.

## **UNIT-I VECTOR CALCULUS**

DIVERGENCE AND CURL OF A VECTOR FIELD

Direigence and everl:

Peoblems:

Caven 
$$\vec{F} = x^2 + y^2 + z^2 + \vec{x}$$

$$\nabla \cdot \vec{F} = \frac{\partial}{\partial x} (x^2) + \frac{\partial}{\partial y} (y^2) + \frac{\partial}{\partial z} (z^2)$$

$$= 2x + 2y + 2z$$

$$\nabla \cdot \vec{F} = 2(x + y + z)$$

and 
$$\nabla x \vec{f} = \begin{vmatrix} \vec{r} & \vec{J} & \vec{K} \\ \frac{\partial}{\partial x} & \frac{\partial}{\partial y} & \frac{\partial}{\partial z} \\ \frac{\partial}{\partial x} & y^2 & z^2 \end{vmatrix}$$

$$= \overrightarrow{r} \left[ \frac{\partial}{\partial y} (x^{2}) - \frac{\partial}{\partial z} (y^{2}) \right] - \overrightarrow{J} \left[ \frac{\partial}{\partial x} (x^{2}) - \frac{\partial}{\partial z} (x^{2}) \right] \\ + \overrightarrow{R} \left[ \frac{\partial}{\partial y} (y^{2}) - \frac{\partial}{\partial y} (x^{2}) \right]$$

$$=0\overrightarrow{r}+0\overrightarrow{r}+0\overrightarrow{r}$$

$$\nabla \times \overrightarrow{F}=\overrightarrow{\sigma}$$

I petermane the constant 'a' so that the F= (x+z)+ (3x+ay) ]+ (x-57) F & Such that "its devergence is zero. 80/n.

Now 
$$\frac{\partial}{\partial x}(x+x) + \frac{\partial}{\partial y}(3x + \alpha y) + \frac{\partial}{\partial x}(x-5x) = 0$$



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Solve Solve 
$$\nabla \cdot \left(\frac{1}{\gamma} \overrightarrow{s}\right)$$

Solve  $\overrightarrow{r} = x\overrightarrow{r} + y\overrightarrow{j} + x\overrightarrow{k}$ 

$$\frac{1}{\delta} \overrightarrow{s} = \frac{x}{s} \overrightarrow{r} + \frac{y}{3} \overrightarrow{j} + \frac{z}{s} \overrightarrow{k}$$

Naco,  $\nabla \cdot \left(\frac{1}{\gamma} \overrightarrow{r}\right) = \left(\overrightarrow{r} \frac{\partial}{\partial x} + \overrightarrow{j} \frac{\partial}{\partial y} + \overrightarrow{k} \frac{\partial}{\partial x}\right) \cdot \left(\frac{x}{s} \overrightarrow{r} + \frac{y}{s} \overrightarrow{j} + \frac{z}{s} \overrightarrow{k}\right)$ 

$$= \frac{\partial}{\partial x} \left(\frac{x}{s}\right) + \frac{\partial}{\partial y} \left(\frac{y}{s}\right) + \frac{\partial}{\partial x} \left(\frac{x}{s}\right)$$

$$= \frac{r(1) - x}{s} \frac{\partial x}{\partial x} + \frac{r(1) - y}{s} \frac{\partial x}{\partial y} + \frac{r(1) - z}{s} \frac{\partial x}{\partial x}$$

$$= \frac{1}{\sqrt{s}} \left[x - x\left(\frac{x}{\gamma}\right) + x - y\left(\frac{y}{\gamma}\right) + x - x\left(\frac{z}{\gamma}\right)\right]$$

$$= \frac{1}{\sqrt{s}} \left[3x - \frac{x}{s} - \frac{y^2}{s} - \frac{x^3}{s}\right]$$

$$= \frac{1}{\sqrt{s}} \left[3x - \frac{1}{\gamma} \cdot \left(x^2 + y^2 + x^2\right)\right]$$

$$= \frac{1}{\sqrt{s}} \left[3x - \frac{1}{\gamma} \cdot \left(x^3 + y^2 + x^3\right)\right]$$

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 $\nabla \cdot \left( \frac{1}{2} \overrightarrow{r} \right) = \frac{2}{2}$