



(An Autonomous Institution)
Coimbatore-641035.

UNIT-II ORDINARY DIFFERENTIAL EQUATIONS

Method of variation of parameters

2]. Solve
$$\frac{d^2y}{dx^2} + y = esc x$$
 using method of variation of parameters.

Solon.

Garen (
$$\mathcal{D}^2+1$$
) $y = CSC \times 1$

AE

 $\mathcal{M}^2+1 = 0$
 $\mathcal{M}^2 = -1$
 $\mathcal{$

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Method of variation of parameters

The general
$$Solp.$$
 Ps.

 $y = Cf + PI$
 $= C_1 \cos x + C_2 \sin x - x \cos x + \sin x$
 $\log (Sin x)$
 $gI.$ Solve $\frac{d^2y}{dx^2} + y = \cot x$ using method of rowation of Parameters.

Soln.

Often $B = (B^2 + 1)y = \cot x$
 $B^2 + 1 = 0$
 $B^2 +$





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Method of variation of parameters

$$= \int \frac{\cos^{9}x}{89n \times} dx$$

$$= \int \frac{1 - 89n^{2}x}{89n \times} dx$$

$$= \int [cscx - s9nx] dx$$

$$= \int cscx dx - \int s9nx dx$$

$$= -log [cscx + cotx] + cos x$$

$$\therefore PI = -89n \times cos x + flog (cscx + cotx) + cos x flox$$
The general sdp. 9s,
$$y = cr + PI$$

$$= c_{1} cos x + c_{2} s9nx - s9nx cos x + flog (cscx + cotx)$$

$$+ c9nx cos x$$

$$= c_{1} cos x + c_{2} s9nx + log (cscx + cotx) s9nx.$$

4]. Solve $(D^3 + \alpha^2)y = \sec qx$ using method of variation of Parameters. Solve $(D^3 + \alpha^2)y = \sec qx$ using method of

Garen
$$(D^2 + a^2)y = \sec \alpha x$$

AE

 $m^2 + a^2 = 0$
 $m^2 = -a^2$
 $m = \pm ai$
 $CF = C_1 \cos \alpha x + C_2 \sin \alpha x$

Here $f_1 = \cos \alpha x$
 $f_1 = -a \sin \alpha x$
 $f_1 = -a \sin \alpha x$
 $f_2 = \sin \alpha x$
 $\omega = f_1 f_2 - f_1 f_2$
 $= \cos \alpha x (a \cos \alpha x) + a \sin \alpha x \sin \alpha x$
 $= a \cos^2 \alpha x + a \sin^2 \alpha x$
 $= a [\cos^2 \alpha x + \sin^2 \alpha x] = \alpha(1) = a$

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 $\int \omega = a$





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UNIT-II ORDINARY DIFFERENTIAL EQUATIONS

Method of variation of parameters

PI = Pf, +8f₂

$$P = -\int \frac{f_2 \times dx}{w} dx$$

$$= -\int \frac{S^2 n \, ax \, Sec \, ax}{a} dx = -\int \frac{1}{a} \tan ax \, dx$$

$$= -\int \frac{1}{a} \int \frac{S^2 n \, ax}{a} dx = -\int \frac{1}{a} \tan ax \, dx$$

$$= +\int \frac{1}{a} \log \frac{(Sec \, ax)}{a} \int \frac{1}{a} \tan ax + \frac{1}{a} \log \frac{(Sec \, ax)}{a}$$

$$P = -\int \frac{1}{a^2} \log \frac{(Sec \, ax)}{a} dx$$

$$= \int \frac{f_1 \times dx}{w} dx$$

$$= \int \frac{\cos ax \, Sec \, ax}{a} dx$$

$$= -\int \frac{1}{a^2} \int \frac{1}{a^2} \cos ax + \frac{1}{a} \int \frac{1}{a^2} \sin ax + \frac{1}{a} \int \frac{1}{a^2} \log \frac{(Sec \, ax)}{a} \cos ax + \frac{1}{a} \int \frac{1}{a^2} \log \frac{(Sec \, ax)}{a} \cos ax + \frac{1}{a} \int \frac{1}{a^2} \log \frac{(Sec \, ax)}{a} \cos ax + \frac{1}{a^2} \cos \cos a$$