

#### SNS COLLEGE OF TECHNOLOGY

Coimbatore – 35

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## Perceptron

Perceptron/Rajarajeswari.S/AP/AIML/SNSCT

# I. PERCEPTRON REPRESENTATION & ISSUES CLASSIFICATION LEARNING II. LINEAR SEPARABILITY

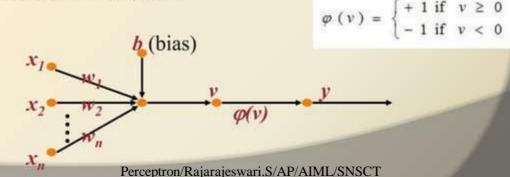
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## **Introduction of Perceptron**

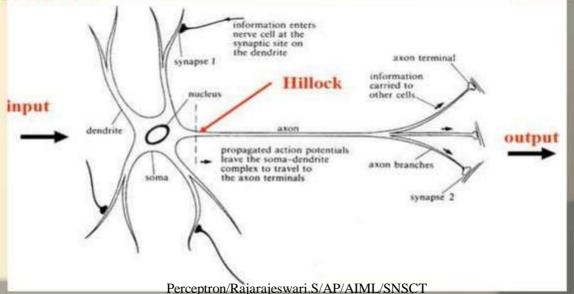
- The perceptron was first proposed by Rosenblatt (1958) is a simple neuron that is used to classify its input into one of two categories.
- A perceptron is a single processing unit of a neural network. A
  perceptron uses a step function that returns +1 if weighted sum of its
  input ≥ 0 and -1 otherwise.



# Perceptron in terms of a Biological



#### Neuron





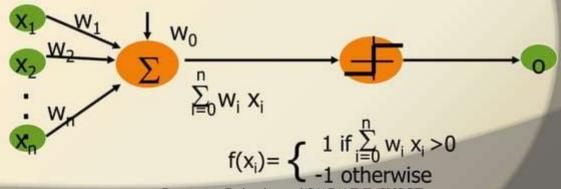
While in actual neurons the dendrite receives electrical signals from taxons of other neurons, in the perceptron these electrical signals are represented as numerical values. At the synapses between the dendrite and axons, electrical signals are modulated in various amounts. This is also modeled in the perceptron by multiplying each input value by a value called the weight.

• An actual neuron fires an output signal only when the total strength of the input signals exceed a certain threshold. We model this phenomenon in a perceptron by calculating the weighted sum of the inputs to represent the total strength of the input signals, and applying a step function on the sum to determine its output. As in biological neural networks, this output is fed to other perceptrons.





- Perceptron can be defined as a single artificial neuron that computes its weighted input with the help of the threshold activation function or step function.
- It is also called as a TLU (Threshold Logical Unit).



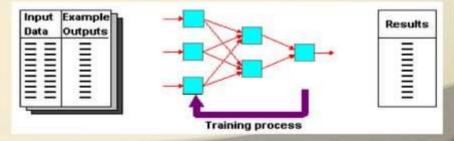
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#### **Definition of Supervised Learning Network**

Supervised learning is used when we have a set of training data. This training data consists of some input data that is connected with some correct output values. The output values are often referred to as target values. This training data is used by learning algorithms like back propagation or genetic algorithms.







- In machine learning, the perceptron is an algorithm for supervised classification of an input into one of several possible non-binary outputs.
- Perceptron can be defined as a single artificial neuron that computes its weighted input with the help of the threshold activation function or step function.
- The Perceptron is used for binary Classification.
- The Perceptron can only model linearly separable classes.
- First train a perceptron for a classification task.
  - Find suitable weights in such a way that the training examples are correctly classified.
  - Geometrically try to find a hyper-plane that separates the examples of the two classes Perceptron/Rajarajeswari.S/AP/AIML/SNSCT



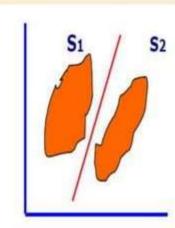


## **Linear Separability:**

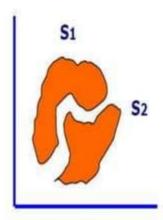
- Linear separability is the concept wherein the separation of the input space into regions is based on whether the network response is positive or negative.
- When the two classes are not linearly separable, it may be desirable to obtain a linear separator that minimizes the mean squared error.
- Definition: Sets of points in 2-D space are linearly separable if the sets can be separated by a straight line.
- Generalizing, a set of points in n-dimensional space are linearly separable if there is a hyper plane of (n-1) dimensions separates the sets.







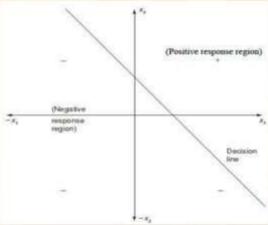
(a) Linearly separable patterns



(b) Not Linearly separable patterns



Consider a network having positive response in the first quadrant and negative response in all other quadrants (AND function) with either binary or bipolar data, then the decision line is drawn separating the positive response region from the negative response region.

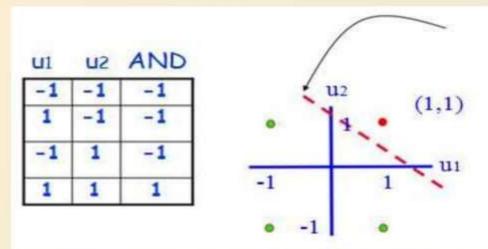


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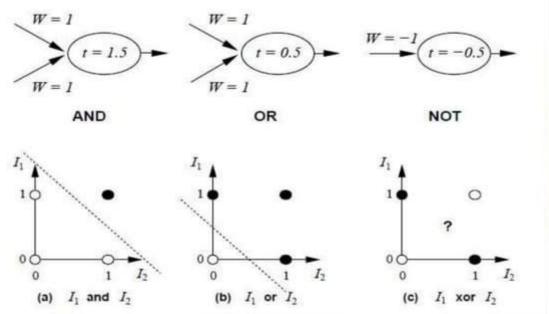
#### SIS

# AND Gate is linearly Separable



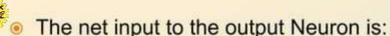






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$$Y_{in} = W_0 + \Sigma_i x_i W_i$$

$$Y_{in}$$
 = The net inputs to the ouput neurons.  
 $i$  = any integer  
 $w_0$  = initial weight

 The following relation gives the boundary region of net input.

$$b + \sum_i x_i w_i = 0$$





- The equation can be used to determine the decision boundary between the region where  $Y_{in} > 0$  and  $Y_{in} < 0$ .
- Depending on the number of input neurons in the network.
   this equation represents a line, a plane or a hyper-plane.
- If it is possible to find the weights so that all of the training input vectors for which the correct response is 1. lie on the either side of the boundary, then the problem is called linearly separable.
- Otherwise. If the above criteria is not met, the problem is called linearly non-separable.





## **Exclusive OR (XOR) Problem:-**

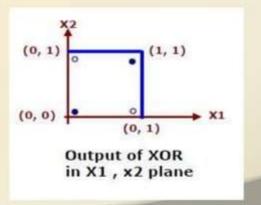
Input x1	Input x2	Output	
0	0	0	1
1	1	0	Even parity •
0	1	1	٦
1	0	1	Odd parity °

#### XOR truth table

- Even parity means even number of 1 bits in the input
- Odd parity means odd number of 1 bits in the input



- There is no way to draw a single straight line so that the circles are one side of the line and the dots on the other side.
- Perceptron is unable to find a line separating even parity input patterns from odd parity input patterns.







## Limitation of Perceptron :-

 The perceptron can only model linearly separable functions, those functions which can be drawn in 2-dim graph and single straight line separates values in two part.

Boolean functions given below are linearly separable:

AND

OR

COMPLEMENT

It cannot model XOR function as it is non linearly separable.

When the two classes are not linearly separable, it may be desirable to obtain a linear separator that minimizes the mean squared error.

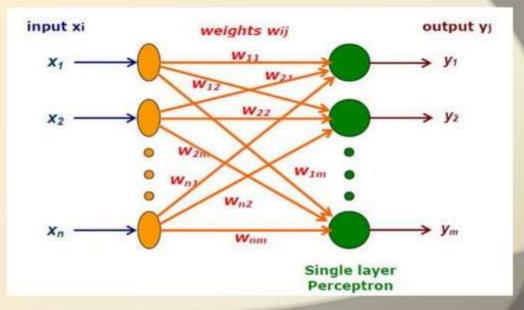
# Single Layer Perceptron :-

- A Single Layer Perceptron consists of an input and an output layer. The activation function employed is a hard limiting function.
- Definition: An arrangement of one input layer of neurons feed forward to one output layer of neurons is known as Single Layer Perceptron.

$$y_j = f(net_j) = \begin{cases} 1 & \text{if } net_j \ge 0 \\ 0 & \text{if } net_j < 0 \end{cases} \quad \text{where } net_j = \sum_{i=1}^n x_i \text{ wij}$$









# Single Layer Perceptron Learning

- Algo :-
- Step 1: Create a perceptron with (n+1) input neurons  $x_0$ ,  $x_1$ , ...,  $x_n$ , where  $x_0 = 1$  is the bias input. Let O be the output neuron.
- Step 2 : Initialize weight W = (w<sub>0</sub>, w<sub>1</sub>, . . . . , . w<sub>n</sub>) to random weights.
- Step 3 :Iterate through the input patterns x<sub>j</sub> of the training set using the weight set; i.e compute the weighted sum of inputs

net 
$$j = \sum X_i w_i$$
 For  $i=1$  to n

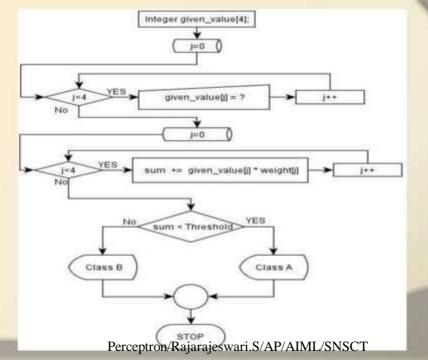
for each input pattern j.

Step 4 : Compute the output Y<sub>j</sub> using the step function

$$y_j = f(net_j) = \begin{cases} 1 & \text{if } net_j \ge 0 \\ 0 & \text{if } net_j < 0 \end{cases} \quad \text{where } net_j = \sum_{i=1}^n x_i \text{ wij}$$

- Step 5 :Compare the computed output  $y_j$  with the target output for each input pattern j.
  - If all the input patterns have been classified correctly, then output (read) the weights and exit.
  - Step 6: Otherwise, update the weights as given below: If the computed outputs y<sub>i</sub> is 1 but should have been 0,
  - Then  $w_i = w_i \alpha x_i$ , i = 0, 1, 2, ..., n
  - If the computed outputs y<sub>j</sub> is 0 but should have been 1,Then w<sub>j</sub> = w<sub>i</sub> + α x<sub>i</sub>, i= 0, 1, 2, . . . , n
  - where α is the learning parameter and is constant.
  - Step 7 : goto step 3
  - END





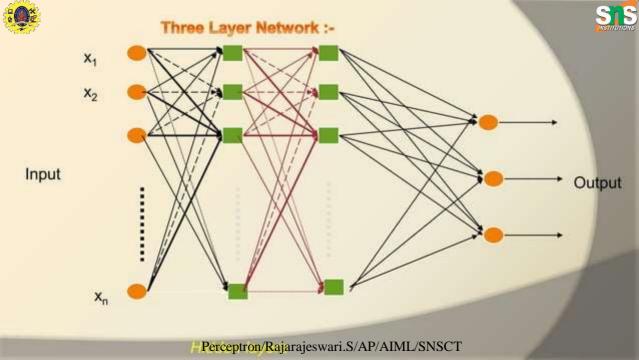


# Multi Layer Perceptron :-



- Multilayer perceptrons (MLP) are the most popular type of neural networks in use today. They belong to a general class of structures called feedforward neural networks, a basic type of neural network capable of approximating generic classes of functions, including continuous and integrable functions.
- A multilayer perceptron:
  - has one or more hidden layers with any number of units.
  - uses linear combination functions in the input layers.
  - uses generally sigmoid activation functions in the hidden layers.
  - has any number of outputs with any activation function.
  - has connections between the input layer and the first hidden layer, between the hidden layers, and between the last hidden layer and the output layer.

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## Layers in Neural Network :-

#### The input layer:

- Introduces input values into the network.
- No activation function or other processing.

#### The hidden layer(s):

- Performs classification of features.
- Two hidden layers are sufficient to solve any problem.
- Features imply more layers may be better.

#### The output layer:

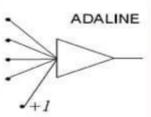
- Functionally is just like the hidden layers.
- Outputs are passed on to the world outside the neural network. Perceptron/Rajarajeswari.S/AP/AIML/SNSCT

### **Adaptive Linear neuron**

SIS

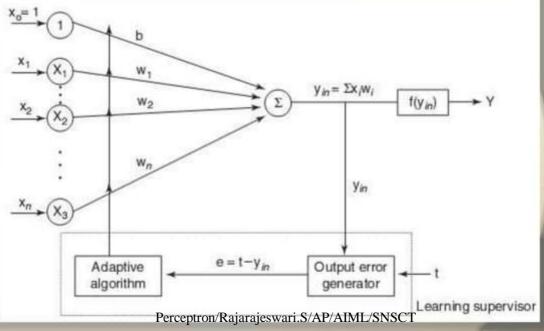
(ADALINE):-

In 1959, Bernard Widrow and Marcian Hoff of Stanford developed models they called ADALINE (Adaptive Linear Neuron) and MADALINE (Multilayer ADALINE). These models were named for their use of Multiple ADAptive LINear Elements. MADALINE was the first neural network to be applied to a real world problem. It is an adaptive filter which eliminates echoes on phone lines.









# Jsing ADALINE Network:-

- Initialize
  - Assign random weights to all links Training
  - Feed-in known inputs in random sequence
  - Simulate the network
  - Compute error between the input and the output (Error Function)
  - Adjust weights (Learning Function)
  - Repeat until total error < ε

#### Thinking

- Simulate the network
- Network will respond to any input
- Does not guarantee a correct solution even for trained inputs

Initialize Training Thinking Perceptron/Rajarajeswari.S/AP/AIML/SNSCT



## Perceptron Learning Algo:-

- Training patterns are presented to the network's inputs; the output is computed. Then the connection weights w<sub>j</sub> are modified by an amount that is proportional to the product of the difference between the actual output, y, and the desired output, d, and the input pattern, x.
- The algorithm is as follows:
- Initialize the weights and threshold to small random numbers.
- Present a vector x to the neuron inputs and calculate the output.
- Update the weights according to:

$$w_j(t+1) = w_j(t) + \eta(d-y)x$$





- where
  - d is the desired output,
  - t is the iteration number, and
  - eta is the gain or step size, where 0.0 < n < 1.0</li>
- Repeat steps 2 and 3 until:
  - the iteration error is less than a user-specified error threshold or
  - a predetermined number of iterations have been completed.







Let  $X = X^+ \cup X^-$  be the set of training examples. and let  $S_X = X_1, X_2, ..., X_k, ...$  be a training sequence on X.

Let w, be the weight vector at step k.

Choose  $w_0$  arbitrarily. For example,  $w_0 = (0, 0, ..., 0)$ .

Each each step k, k = 0, 1, 2, ...

Classify Xk using wk.

If  $X_k$  is correctly classified, take  $w_{k+1} = w_k$ .

If  $X_k$  is in  $X^k$  but misclassified, take  $w_{k+1} = w_k - c_k X_k$ .

If  $X_k$  is in  $X^+$  but misclassified, take  $w_{k+1} = w_k + c_k X_k$ .

The sequence  $c_k$  should be chosen according to the data. Overly large constant values can lead to oscillation during training. Values that are too small will increase training time. However,  $c_k = c_0/k$  will work for any positive  $c_0$ .

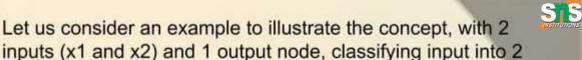




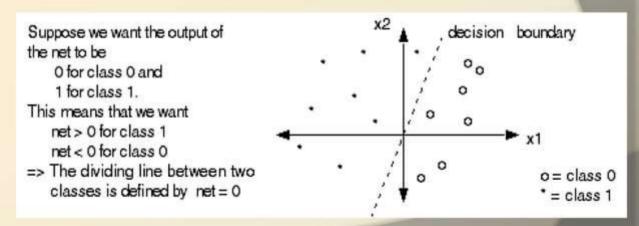
#### Classification of Patterns:-

- Training of Network: Given a set of inputs 'x', and output/target values 'y', the network finds the best linear mapping from x to y.
- Given an unpredicted 'x' value, we train our network to predict what the most likely 'y' value will be.
- Classification of pattern is also a technique of training the network, in which we assign a physical object, event or phenomenon to one set of pre-specified classes (or categories).









Classes (class 0 and class 1).