



# 16ME207- STRENGTH OF MATERIALS

UNIT I - STRESS STRAIN DEFORMATION OF SOLIDS

**Stresses in Stepped shafts and varying sections** 





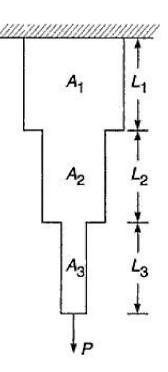
### BARS WITH CROSS SECTIONS VARYING IN STEPS

Consider a bar of varying three sections of lengths L1 L2 and L3 having respective areas of cross-sections A1, A2 and A3 subjected to an axial pull P. Let  $\delta$ L1,  $\delta$ L2,  $\delta$ L3 be the changes in length of the respective three sections of the bar, then we have

$$\delta L_1 = \frac{PL_1}{A_1E}, \quad \delta L_2 = \frac{PL_2}{A_2E}, \quad \delta L_3 = \frac{PL_3}{A_3E}$$

Now the total elongation of the bar,

$$\delta L = \delta L_1 + \delta L_2 + \delta L_3 = \frac{PL_1}{A_1E} + \frac{PL_2}{A_2E} + \frac{PL_3}{A_3E} = \frac{P}{E} \left( \frac{L_1}{A_1} + \frac{L_2}{A_2} + \frac{L_3}{A_3} \right)$$







#### BARS WITH CONTINUOUSLY VARYING CROSS SECTIONS

#### Bars with varying Circular cross section

A bar uniformly tapering from a diameter D1 at one end to a diameter D2 at the other end is shown in Figure.

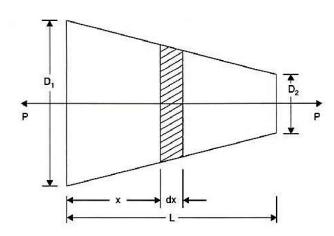
Let P = Axial tensile load on the bar

L = Total length of the bar

E = Young's modulus.

Consider a small element of length dx of the bar at a distance x from the left end. Let the diameter of the bar be D at a distance x from the left end.

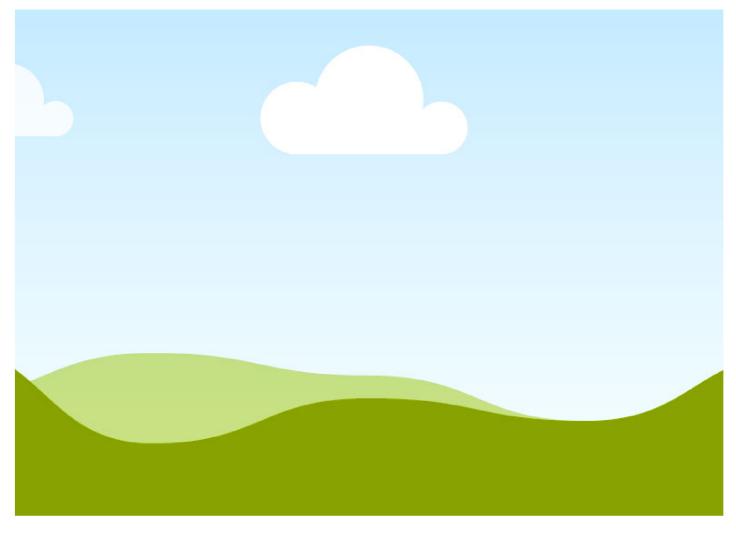
$$D_x = D_1 - \left(\frac{D_1 - D_2}{L}\right) x$$
 
$$= D_1 - kx \qquad \text{where } k = \frac{D_1 - D_2}{L}$$







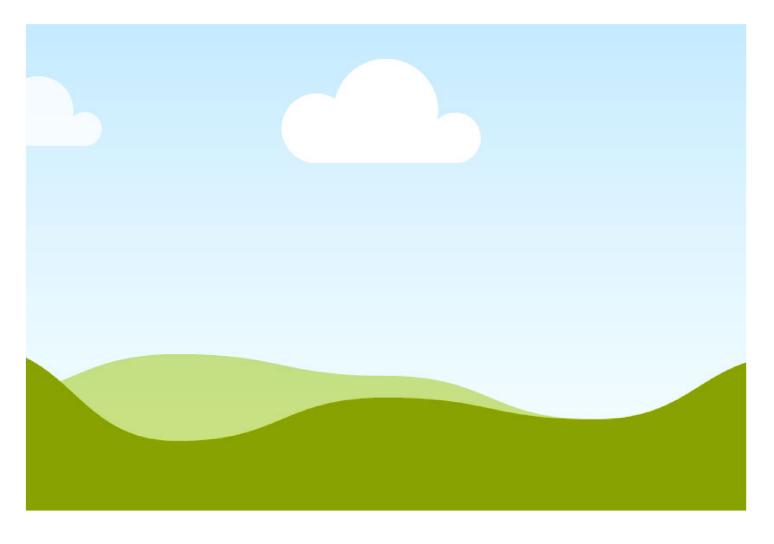
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