

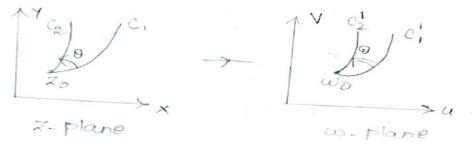
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UNIT-III COMPLEX DIFFERENTIATION

Conformal mapping

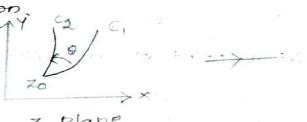
Conformal mapping:

A transferention that preserves angles between every pair of curives through a point both In mognitude and sense, is said to be conformal at that point.



Isogonal mapping:

A transformation under which angles between every pain of wives through a point are preserved in magnifiede, but different in derection.



z-plane

The point to 95 said to be confical coppedal point: Point of the transformation w= f(x) 9f f(x) 18 not conformal at to. The critical popul is defend by,

$$\frac{dw}{dx} = 0 \text{ and } \frac{dx}{dw} = 0$$





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Conformal mapping

Find the cofffical point of the transform J. $\omega = x + \frac{1}{x}$ Soln. arven w= x+ 1 $\frac{d\omega}{dx} = 1 - \frac{1}{x^2} = \frac{x^2 - 1}{x^2}$ $\frac{dx}{d\omega} = \frac{x^2}{x^2}$ Now $\frac{dw}{dx} = 0 \Rightarrow \frac{x^2}{x^2} = 0$ and $\frac{dx}{dw} = 0 \Rightarrow \frac{x^2}{x^2} = 0 \Rightarrow x^2 = 0$ The offfical popple area, ±1. E]. Find the couffical point of wa = (x-a) (x-B) Soin. (Aver wa = (z-a) (x-b) Differentiate wir to Z, $2w \frac{dw}{dz} = (z-\alpha)(1) + (z-\beta)(1)$ = (z-a) + (z-B) $\frac{d\omega}{dx} = \frac{2x - (\alpha + \beta)}{2\omega}$ and $\frac{dx}{dw} = \frac{2w}{2x - (x+B)}$ Now $\frac{d\omega}{dz} = 0 \Rightarrow \frac{2z - (\alpha + \beta)}{2\omega} = 0$ 87 = X+B $x = \frac{\alpha + \beta}{3}$



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Conformal mapping

and
$$\frac{dx}{dw} = 0 \Rightarrow \frac{\Re w}{\Re x} = 0$$
 $\frac{\partial w}{\partial x} = 0$
 $\frac{\partial w}{\partial x$

1100 1- 10: 100 X





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UNIT-III COMPLEX DIFFERENTIATION

Conformal mapping

A point z=a & said to be freed point of a mapping w= f(x) % its image under under f(x) is etself.

ie., f(x) = x

find the invariant points of w= 1+2 Soln.

Given $w = \frac{1+\chi}{1-\chi}$

The Privariant points are

$$z = \frac{1+z}{1-z} \quad (: w=f(z) = z)$$

$$z = \frac{2z+6}{z+7}$$

$$(z+1)(z+6)=0$$

SATHYA S/AP/MATHS

Hw :0= /