



(An Autonomous Institution)
Coimbatore-641035.

UNIT-III COMPLEX DIFFERENTIATION

Bilinear Transformations

Mobilus Teansformation B919mean teams for mation The houstonation $\omega = \frac{\alpha z + b}{cz + d}$, ad- $\frac{k}{c}$, where a, b, c, d are complex numbers is all a billippoad teamsformation. Formula: Bilineau transformation of Z, Za, Za 90th w, wa, wa is gun by $\frac{(\omega-\omega_1)(\omega_2-\omega_3)}{(\omega-\omega_3)(\omega_2-\omega_1)} = \frac{(z-z_1)(z_2-z_3)}{(z-z_3)(z_2-z_1)}$ J. Find the bilinear transformation which make the pennts X=9-1-1 Porto w= 1, 1, 0 stempe chive Solo .: 7 CAVON 7,=0, 72=-1, 73=-1 $w_1 = i$, $w_2 = i$, $w_3 = 0$ The bilinear transformation is. $\frac{(\omega - \omega_{1})(\omega_{2} - \omega_{3})}{(\omega - \omega_{3})(\omega_{2} - \omega_{1})} = \frac{(x - z_{1})(z_{2} - z_{3})}{(x - z_{3})(z_{2} - z_{1})}$ $\frac{(\omega - i)(1 - 0)}{(\omega - 0)(1 - i)} = \frac{(z - 0)(-i + 1)}{(z + 1)(-i - 0)}$ $\frac{\omega - i}{\omega - \omega i} = \frac{\pi (1 - i)}{(-i)(\pi + i)}$ $\frac{\omega - i}{\omega - \omega i} = \frac{z - zi}{-iz - i}$ (w-i) (ix-1) = (x-xi) (w-wi) - ルスラールリースー = ロスー いスラー いスリーのス _ wzi-wi +wzi +wzi = 7+ wzi-wi = 7H い (エー1) = スサ



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$$\omega = \frac{1}{1} \frac{x+t}{x-1}$$

$$= \frac{1}{1^{2}} \frac{x+t}{x-1}$$

$$\omega = -i \left(\frac{x+t}{x-1}\right)$$

$$\omega = -i \cdot x_{0} = -i$$

$$\omega = -i \cdot x_{0} =$$



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$$\Rightarrow \frac{2\omega}{-2i} = \frac{z(i+1) + (1-i)}{z(i-1) - (1+i)}$$

$$z(i+1) + (1-i)$$

$$z(i+$$

 $= \frac{z + iz - 1 - i}{-iz - z - i - 1}$

(-Z-1)+1(-X-1)



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Bilinear Transformations

$$= \frac{(\pi-1)(1+i)}{(-\chi-1)(1+i)}$$

$$= \frac{1-\chi}{1+\chi}$$

$$= \frac{1-\chi}{\chi+1}$$

$$= \frac{1-\chi}{\chi+1$$



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Bilinear Transformations

Soln.

bilippean transformation is

$$\frac{(\omega_{-}\omega_{1})(\omega_{2}-\omega_{3})}{(\omega_{-}\omega_{3})(\omega_{2}-\omega_{1})} = \frac{(z-z_{1})(z_{2}-z_{3})}{(z-z_{3})(z_{2}-z_{1})}$$

$$(\omega_{-}\omega_{3})$$
 $(\omega_{2}-\omega_{1})$ $(z_{-}z_{2})(z_{3}-z_{1})$

$$\frac{(\omega-\omega_1)(\omega_2-\omega_3)}{(\omega-\omega_3)(\omega_2-\omega_1)} = \frac{(z-z_1)z_3\left|\frac{z_3}{z_3}-1\right|}{(\omega-\omega_3)(\omega_2-\omega_1)}$$

$$r_3 \left(\frac{x}{z_3} - 1 \right) \left(z_3 - z_1 \right)$$

$$\frac{(\omega+5)(-1-3)}{(\omega-3)(-1+5)} = \frac{(z-0)(o-1)}{(o-1)(1-0)}$$

$$(\omega - 3)(-1+5)$$
 $(\omega - 1)(1-0)$

$$\frac{(\omega+5)(-4)}{(-3)(1)} = \frac{-7}{-1}$$

$$-(\omega+5) = x$$

$$-(\omega+5) = 7(\omega-3)$$

$$\omega(x+1) = 3x-5$$

$$w = 3x - 5$$