



(An Autonomous Institution)
Coimbatore-641035.

UNIT-II COMPLEX DIFFERENTIATION

Construction of Analytic functions

Construct for of Analytic function:

Milne is Thomson method

i) To find f(x), when u is given $f(x) = \int [\phi_i(x, 0) - i \phi_j(x, 0)] dx$ where $\phi_i(x, 0) = \left(\frac{\partial u}{\partial y}\right)_{(x, 0)}$ and $\phi_j(x, 0) = \left(\frac{\partial u}{\partial y}\right)_{(x, 0)}$ ii). To find f(x), when V is given $f(x) = \int [\phi_i(x, 0) + i \phi_j(x, 0)] dx$ where $\phi_i(x, 0) = \left(\frac{\partial V}{\partial y}\right)_{(x, 0)}$ and $\phi_j(x, 0) = \left(\frac{\partial V}{\partial y}\right)_{(x, 0)}$ iii). If u - V or u + V is given, then to find take f(x) = u + iV if(x) = iu - V

II. Find the analytic function
$$f(z)$$
 whose seal part is $u = 3x^2y + 2x^2 - y^3 - 2y^2$ solo.

Creen $u = 3x^2y + 2x^2 - y^3 - 2y^2$

$$\frac{\partial y}{\partial x} = 6xy + 4x$$





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$$\phi_{1}(x,0) = \left(\frac{\partial u}{\partial x}\right) = 4x$$

$$(x,0)$$

$$\frac{\partial u}{\partial y} = 3x^{2} - 3y^{2} - 4y$$

$$\phi_{2}(x,0) = \left(\frac{\partial u}{\partial y}\right)_{(x,0)} = 3x^{2}$$

By Miline Thomson method,
$$f(x) = \int [d_{1}(x,0) - i d_{2}(x,0)] dx$$

$$= \int [1+x - i 3x^{2}] dx$$

$$= \frac{4x}{2} - i \frac{3x^{3}}{3} + C$$

$$f(x) = 3x^{2} - i x^{3} + C$$

$$f(x) = 3x^{2} - i x^{3} + C$$
And Therefore with determine analytic function $f(x)$.

Given $v = e^{x}$ or $\cos y + e^{x}$ yeing $\frac{\partial v}{\partial x} = e^{x} \cos y - e^{x} \cos y + e^{x} y \sin y$

$$= e^{x} \cos y - x e^{x} \cos y - e^{x} \cos y + e^{x} y \sin y$$

$$= e^{x} \cos y - x e^{x} \cos y - e^{x} \cos y + e^{x} y \sin y$$

$$= e^{x} \cos y + x e^{x} \cos y - e^{x} \cos y + e^{x} y \sin y$$

$$= e^{x} \cos y + x e^{x} \cos y - e^{x} \cos y + e^{x} y \sin y$$

$$= e^{x} \cos y + x e^{x} \cos y + e^{x} y \cos y + e^{x} \sin y$$

$$= e^{x} \cos y + x e^{x} \cos y + e^{x} y \cos y + e^{x} \sin y$$

$$= e^{x} \cos y + e^{x} \cos y + e^{x} \cos y + e^{x} \cos y + e^{x} \cos y$$

$$= -x e^{x} \cos y + e^{x} (\cos y + e^{x} \cos y + e^{x} \cos y)$$

$$= -x e^{x} \cos y + e^{x} (\cos y + e^{x} \cos y + e^{x} \cos y)$$

$$= -x e^{x} \cos y + e^{x} (\cos y + e^{x} \cos y + e^{x} \cos y)$$

$$= -x e^{x} \cos y - y \sin y + e^{x} \cos y$$

$$= -x e^{x} \cos y - y \sin y + e^{x} \cos y$$

$$= -x e^{x} \cos y - y \sin y + e^{x} \cos y$$

$$= -x e^{x} \cos y - y \sin y + e^{x} \cos y$$

$$= -x e^{x} \cos y - y \sin y + e^{x} \cos y$$

$$= -x e^{x} \cos y - y \sin y + e^{x} \cos y$$





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$$= -xe^{x} \cos y - e^{-x}y \sin y + 2e^{-x} \cos y$$

$$= -xe^{x} \cos y + xe^{-x} \cos y + e^{-x} y \sin y$$

$$= -xe^{-x} \cos y - e^{-x}y \sin y + 2e^{-x} \cos y$$

$$= -xe^{-x} \cos y - e^{-x}y \sin y + 2e^{-x} \cos y$$

$$= -xe^{-x} \cos y - e^{-x}y \sin y + 2e^{-x} \cos y$$

$$= -xe^{-x} \cos y - e^{-x}y \sin y + 2e^{-x} \cos y$$

$$= -xe^{-x} \cos y - e^{-x}y \sin y + 2e^{-x} \cos y + e^{-x} \sin y$$

$$= -xe^{-x} \sin y + e^{-x}y \cos y + e^{-x} \sin y$$

$$= -xe^{-x} \sin y + e^{-x}y \cos y + e^{-x} \sin y$$

$$= -xe^{-x} \cos y - xe^{-x} \cos y + e^{-x} \sin y$$

$$= -xe^{-x} \cos y - xe^{-x} \cos y + e^{-x} \sin y$$

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$$= -xe^{-x} \cos y - xe^{-x} \cos y + e^{-x} \cos y + e^{-x} \sin y$$

$$= -xe^{-x} \cos y - xe^{-x} \cos y + e^{-x} \cos y + e^{-x} \sin y$$

$$= -xe^{-x} \cos y - xe^{-x} \cos y + e^{-x} \cos y + e^{-x} \sin y$$

$$= -xe^{-x} \cos y - xe^{-x} \cos y + e^{-x} \cos y + e^{-x$$





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By Milne's Thomson method,

$$F(x) = \int [\phi_{1}(x,0) - i \phi_{2}(x,0)] dx$$

$$= \int (e^{x} + i e^{x}) dx$$

$$= (i+i) \int e^{x} dx$$

$$(i+i) f(x) = (i+i) e^{x} + c$$

$$f(x) = e^{x} +$$





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UNIT-II COMPLEX DIFFERENTIATION

By MPINELS TRANSON Method,

$$f(x) = \int [d_1(x, 0) - id_2(x, 0)] dx$$

$$= \int [-\cos^2 x - i(0)] dx$$

$$= -\int \cos^2 x dx$$

$$f(x) = \cot x + C$$

All production $f(x) = u + iv$
where $u - v = e^{x}(\cos y - \sin y)$
Solon.

Let $f(x) = u + iv \rightarrow m$

$$if(x) = iu - v \rightarrow m$$

$$(1) + (m) \Rightarrow (1 + i) + (m) = u + iv + iu - v$$

$$(1 + i) + (m) = u + iv + iu - v$$

$$(1 + i) + (m) = u + iv + iu - v$$

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$$(1 + i) + (m) = u + iv + iu + v$$

$$(1 + i) + (m) = u + iv + iu + v$$

$$(1 + i) + (m) = u + iv + iu + v$$

$$(1 + i) + (m) = u + i$$





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But 1 is
$$\frac{Sh}{2x}$$
 $\frac{2x}{\cos h \, 2y} = \frac{Sh}{2x}$ $\frac{2x}{\cos h \, 2x} = \frac{Sh}{2x}$ $\frac{2x}{\sin h \, 2$





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$$= \frac{2\cos 3x - 2(1+\cos 2x)}{1-\cos 3x}$$

$$= \frac{2\cos 3x - 1-\cos 3x}{1-\cos 3x}$$

$$= \frac{-2}{1-\cos 2x} = \frac{-1}{1-\cos 2x}$$

$$= \frac{-2}{1-\cos 2x} = \frac{-1}{1-\cos 2x}$$

$$= \frac{-3\cos 2x}{2} = \frac{-1}{\sin^2 x}$$

$$\frac{3y}{3y} = \frac{-\cos^2 x}{(\cos h^2y - (\cos 2x)^2)}$$

$$= -\frac{2\sin 2x}{(\cos h^2y - (\cos 2x)^2)}$$

$$= -\frac{3\cos 2x}{(\cos h^2y - (\cos 2x)^2)}$$

$$= -\frac{1}{(\cos h^2x - (\cos 2x)^2)}$$

$$= -\frac{3\cos 2x}{(\cos h^2x - (\cos h^2x -$$