**EVALUATE:** SINCE CONTRACT (An Autonomous Institution)  
Combatore-641035.  
UNIT-III PARTIAL DIFFERENTIAL EQUATIONS Solution of First Order Partial Differential Equations  
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A FRENTIAL detEnerthal Equations are of the  
proof deepeed. Is said to be Finears; otherword see  
R is said to be non - Isbnear.  
Solutional TYPEs:  
TYPE 1: 
$$f(E, q) = 0$$
  
TYPE 2:  $X = bx + q.y + f(E, q) [classical second
TYPE 3:  $f(X, E, q) = 0$   
TYPE 4:  $f_1(x, p) = f_2(y, q)$   
TYPE 4:  $f_1(x, p) = f_2(y, q)$   
TYPE 4:  $f_2(x, q) = 0$   
TYPE 4:  $f_1(x, p) = f_2(y, q)$   
TyPE 5:  $P(E, q) = 0$   
TYPE 4:  $f_2(x, q) = 0$   
TYPE 7:  $P(E, q) = 0$   
TYPE 8:  $P(x, q) = 0$   
TYPE 9:  $P(x, q) = 0$   
Solve  $P + q = P(q) \rightarrow CU$   
Solve  $P + q = p(q) \rightarrow$$ 



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UNIT-III PARTIAL DIFFERENTIAL EQUATIONS Solution of First Order Partial Differential Equations Subs. the above values 910 (1), we get a+b=aba = ab - b  $a = b(a - 1) \Rightarrow b = \frac{a}{a - 1}$ The complete entegral fs,  $z = ax + \left(\frac{q}{a-1}\right)y + c \rightarrow (3)$ Sangulai Integral: dats. (3) parthally ou.r. + a and c and equal to seeo.  $\frac{\partial x}{\partial a} = x + \left[ \frac{(a-1)(1) - a(1)}{(a-1)^2} \right] y = 0$  $\frac{\partial z}{\partial t} = i \neq 0 \quad (P \cup P) = i \neq 0 \quad (P \cup P) = i \neq 0$ 8C There is no singular Integral. General Integral: put  $c = \phi(a)$  in (3)  $z = az + \left(\frac{a}{a-1}\right)y + \phi(a) \rightarrow (4)$ 196. (4) partfally w.r. t ca  $\frac{\partial x}{\partial a} = x + \begin{bmatrix} a - y (i) - a(i) \end{bmatrix} y + \phi'(a) = 0 \longrightarrow (5)$ Elementate (a) b/w (4) and (5>, we get the general solution. EJ. Solve  $\sqrt{P} + \sqrt{q} = 1$  $\sqrt{P} + \sqrt{q} = ) \longrightarrow (1)$ Let z = ax + by + CSoln :



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UNIT-III PARTIAL DIFFERENTIAL EQUATIONS Solution of First Order Partial Differential Equations complete Integral:  $\frac{\partial x}{\partial x} = a \Rightarrow P = a$  $\frac{\partial x}{\partial y} = b \Rightarrow q = b$   $\frac{\partial x}{\partial y} = b \Rightarrow q = b$ Subs. the above values qn(1), we get  $\sqrt{q} + \sqrt{b} = 1$  $\sqrt{b} = 1 - \sqrt{a}$  $b = (1 - \sqrt{a})^2$ The complete integral B,  $\chi = \alpha \chi + (1 - \sqrt{\alpha})^2 y + c \rightarrow (2)$  $\frac{\partial x}{\partial a} = \mathbf{x} + 2(1 - \sqrt{a})\left(\frac{-1}{2\sqrt{a}}\right) \mathbf{y} = 0$ Singular Integral:  $\frac{\partial x}{\partial c} = i \neq 0$ Dr = 1 = 0 Dr = 1 = 0 There is no singular integral. Ciencial Integral: Fut c=  $\phi(a)$  gn (2)  $x = ax + (1 - \sqrt{a})^{2}y + \phi(a) \longrightarrow (3)$ partfally w.r. t'a'  $\frac{\partial z}{\partial a} = g + 2(1 - \sqrt{a})\left(\frac{-1}{2\sqrt{a}}\right)y + \phi'(a) = 0 \rightarrow (4)$ Ekiminate 'a' blue (3) and (4), we get the general so Integral. Hw