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UNIT-III PARTIAL DIFFERENTIAL EQUATIONS Solution of Second Order Partial Differential Equations

Lancar poe of 2nd and lagher order with constant coefficients.

Homogeneous 19 near PDEs:

A laneau PDE with constant In which all the partial developments

ove of the same orders is called homogeneous; otherwise it is called non-homogeneous. a 2 2

Example:

Homogeneous Equation:

$$\frac{3^{2}x}{9x^{2}} + 5 \frac{3^{2}x}{9x3y} + 6 \frac{3^{2}x}{9y^{2}} = Sfn x$$

Non-bomogeneous Equation:

$$\frac{\partial^2 x}{\partial x^2} - 5\frac{\partial x}{\partial x} + 7\frac{\partial x}{\partial y} + \frac{\partial^2 x}{\partial y^2} = e^{x+y}$$

Notation: (a) DI - a, DI-10 - DI-10

$$D = \frac{\partial}{\partial x}$$
,  $D' = \frac{\partial}{\partial y}$ 

 $D = \frac{\partial}{\partial x}$ .  $D' = \frac{\partial}{\partial y}$ Method of finding complementary function

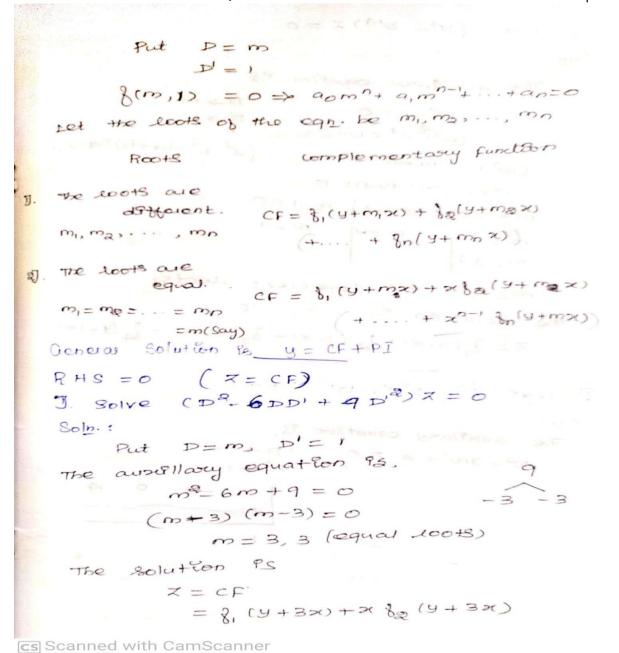
Let the given equation be of the form  $\delta(D, D') z = \delta(x, y)$ 





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$$PI = \frac{1}{B^2 - 4DD^2 + 4D^2}$$

$$= \frac{1}{2^2 - 4(2)(1) + 4(1)^2}$$

$$= \frac{1}{2^2 - 4(2)(1) + 4(1)^2}$$

$$= \frac{1}{A - 8 + 4}$$

$$= \frac{2x + y}{B^2 + 2}$$

$$= \frac{1}{2D - 4D^2}$$

$$= \frac{2x + y}{2}$$

$$= \frac{2x + y}{B^2 + 2}$$

$$= \frac{2x + y}{B^2 + 2}$$
The Solution 98  $x = CF + PI$ 

$$= \frac{2x + y}{B^2 + 2x + 2}$$

$$= \frac{2x + y}{B^2 + 2x + 2}$$

Solve 
$$\frac{\partial^2 x}{\partial x^2} - 4 \frac{\partial^2 x}{\partial x \partial y} + 4 \frac{\partial^2 x}{\partial y^2} = e^{2x} - y$$





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UNIT-III PARTIAL DIFFERENTIAL EQUATIONS Solution of Second Order Partial Differential Equations (m-1)(m-1)=0m=1, 1 (equal) CF= 1, (4+ x) + x 82 (4+x)  $PI = \frac{1}{D^{2} - 2DD' + D^{2}} (\cos(x-3y)) \quad \alpha = 1, b = -3$   $= \frac{1}{D^{2} - 2DD' + D^{2}} + (x-3y) \quad D^{2} \rightarrow -\alpha^{2} = -1^{2} = -1$   $= \frac{1}{1 - 2(3) - 9} \quad D^{2} \rightarrow -\alpha^{2} = -1(-3)$   $= \frac{1}{16} \cos(x-3y) \quad D^{2} \rightarrow -b^{2} = -(-3)^{2}$  = -92]. (B-ADI2) X = San (2x+y) AE  $m^2 - A = 0$  (m+2)(m-2) = 0 m = -2, a(p+2)(y+2) CF = b(y-2x) + ba(y+2x) = 0cs Scanned with CamScanner





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$$PI = \frac{1}{B^{2} - 4D^{1/2}} \qquad Sgn (2x+y) \qquad b = 1$$

$$PI = \frac{1}{B^{2} - 4D^{1/2}} \qquad Sgn (2x+y) \qquad D^{2} \rightarrow -a^{2} = -2^{2}$$

$$= \frac{1}{-4 - 4(-1)} \qquad Dp^{1} \rightarrow -ab = -2(0)$$

$$= x \frac{1}{2D} Sgn (2x+y) \qquad = -2$$

$$= \frac{x}{a} \left( \frac{-\cos(2x+y)}{2} \right)$$

$$= \frac{x}{a} \left( \frac{-\cos(2x+y)}{2} \right)$$

$$PI = -\frac{x}{4} \cos(2x+y)$$

$$= \frac{x}{4} = CF + PI$$

$$= \frac{1}{4} (y - 2x) + \frac{1}{2} (y + 2x) - \frac{x}{4} \cos(2x+y)$$

$$Sgn (x - y)$$

$$Sgn (x - y)$$

$$PI = \frac{1}{2} \left( \frac{1}{B^{2} - 3DD^{1} + D^{1/2}} \right) x = \frac{1}{2} \left[ Sgn (x + y) + \frac{1}{2} \left[ Sgn (x - y) \right] \right]$$

$$= \frac{1}{2} \left[ PI + PI \right] \rightarrow (1)$$





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$$PI_{1} = \frac{1}{D_{-}^{2} 3DD^{1} + D^{1} 2} SP_{1}(x+y) \qquad \alpha = 1, b = 1$$

$$= \frac{1}{1 - 3(-1) - 1} SP_{1}(x+y) \qquad D^{1} \Rightarrow -\alpha D^{2} = -1$$

$$= \frac{1}{1 - 2 + 3} SP_{1}(x+y) \qquad D^{1} \Rightarrow -\alpha D^{2} = -1$$

$$= SP_{1}(x+y) \qquad D^{1} \Rightarrow -\alpha D^{2} = -1$$

$$= SP_{2}(x+y) \qquad D^{2} \Rightarrow -\alpha D^{2} = -1$$

$$= \frac{1}{1 - 3(D^{-1})} SP_{2}(x-y) \qquad D^{2} \Rightarrow -\alpha D^{2} = -1$$

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$$= \frac{1}{1 - 3(D^{-1})} SP_{2}(x+y) - \frac{1}{10} SP_{2}(x-y) \qquad SP_{2}(x-y)$$

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$$= \frac{1}{1 - 3(D^{-1})} SP_{2}(x-y) \qquad SP_{2}(x-y)$$

$$= \frac{1}{1 - 3(D^{-1})} SP_{2}(x-y) \qquad D^{2} \Rightarrow -\alpha^{2} = -1 \Rightarrow 1$$

$$= \frac{1}{1 + 4(D^{-1})} SP_{2}(x-y) \qquad D^{2} \Rightarrow -\alpha^{2} = -1 \Rightarrow 1$$

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$$= \frac{1}{1 + 4(D^{-1})} SP_{2}(x-y) \qquad D^{2} \Rightarrow -\alpha^{$$





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RHS = 
$$x^{m}y^{n}$$

N. Solve  $(D^{2} - 4DD^{2} + 4D^{2}) \times = xy$ 

Soln.

AE  $m^{2} - 4m + 4 = 0$ 
 $(m-2)(m2) = 0$ 
 $m = 2, 2$  (Equal)

 $CF = \begin{cases} 1, (y+2x) + x \\ 2/y + 2x \end{cases}$ 

PI =  $\begin{cases} 1 \\ D^{2} \end{cases} = \begin{cases} 1 - \frac{4DD^{2}}{D^{2}} + \frac{4D^{2}}{D^{2}} \end{cases}$ 

$$= \begin{cases} 1 - (\frac{4D}{D} - \frac{4D^{2}}{D^{2}}) \\ \frac{1}{D^{2}} \end{cases} = \begin{cases} 1 - (\frac{4D^{2}}{D} - \frac{4D^{2}}{D^{2}}) \\ \frac{1}{D^{2}} \end{cases} = \begin{cases} 1 + (\frac{4D^{2}}{D} - \frac{4D^{2}}{D^{2}}) \\ \frac{1}{D^{2}} \end{cases} = \begin{cases} 1 + (\frac{4D^{2}}{D} - \frac{4D^{2}}{D^{2}}) \\ \frac{1}{D^{2}} \end{cases} = \begin{cases} 1 + (\frac{4D^{2}}{D} - \frac{4D^{2}}{D^{2}}) \\ \frac{1}{D^{2}} \end{cases} = \begin{cases} 1 + (\frac{4D^{2}}{D} - \frac{4D^{2}}{D^{2}}) \\ \frac{1}{D^{2}} \end{cases} = \begin{cases} 1 + (\frac{4D^{2}}{D} - \frac{4D^{2}}{D^{2}}) \\ \frac{1}{D^{2}} \end{cases} = \begin{cases} 1 + (\frac{4D^{2}}{D} - \frac{4D^{2}}{D^{2}}) \\ \frac{1}{D^{2}} \end{cases} = \begin{cases} 1 + (\frac{4D^{2}}{D} - \frac{4D^{2}}{D^{2}}) \\ \frac{1}{D^{2}} \end{cases} = \begin{cases} 1 + (\frac{4D^{2}}{D} - \frac{4D^{2}}{D^{2}}) \\ \frac{1}{D^{2}} \end{cases} = \begin{cases} 1 + (\frac{4D^{2}}{D^{2}} - \frac{4D^{2}}{D^{2}}) \\ \frac{1}{D^{2}} \end{cases} = \begin{cases} 1 + (\frac{4D^{2}}{D} - \frac{4D^{2}}{D^{2}}) \\ \frac{1}{D^{2}} \end{cases} = \begin{cases} 1 + (\frac{4D^{2}}{D} - \frac{4D^{2}}{D^{2}}) \\ \frac{1}{D^{2}} \end{cases} = \begin{cases} 1 + (\frac{4D^{2}}{D^{2}} - \frac{4D^{2}}{D^{2}}) \\ \frac{1}{D^{2}} \end{cases} = \begin{cases} 1 + (\frac{4D^{2}}{D^{2}} - \frac{4D^{2}}{D^{2}}) \\ \frac{1}{D^{2}} \end{cases} = \begin{cases} 1 + (\frac{4D^{2}}{D^{2}} - \frac{4D^{2}}{D^{2}}) \\ \frac{1}{D^{2}} \end{cases} = \begin{cases} 1 + (\frac{4D^{2}}{D^{2}} - \frac{4D^{2}}{D^{2}}) \\ \frac{1}{D^{2}} \end{cases} = \begin{cases} 1 + (\frac{4D^{2}}{D^{2}} - \frac{4D^{2}}{D^{2}}) \\ \frac{1}{D^{2}} \end{cases} = \begin{cases} 1 + (\frac{4D^{2}}{D^{2}} - \frac{4D^{2}}{D^{2}}) \\ \frac{1}{D^{2}} \end{cases} = \begin{cases} 1 + (\frac{4D^{2}}{D^{2}} - \frac{4D^{2}}{D^{2}}) \\ \frac{1}{D^{2}} \end{cases} = \begin{cases} 1 + (\frac{4D^{2}}{D^{2}} - \frac{4D^{2}}{D^{2}}) \\ \frac{1}{D^{2}} \end{cases} = \begin{cases} 1 + (\frac{4D^{2}}{D^{2}} - \frac{4D^{2}}{D^{2}}) \\ \frac{1}{D^{2}} \end{cases} = \begin{cases} 1 + (\frac{4D^{2}}{D^{2}} - \frac{4D^{2}}{D^{2}}) \\ \frac{1}{D^{2}} \end{cases} = \begin{cases} 1 + (\frac{4D^{2}}{D^{2}} - \frac{4D^{2}}{D^{2}}) \\ \frac{1}{D^{2}} \end{cases} = \begin{cases} 1 + (\frac{4D^{2}}{D^{2}} - \frac{4D^{2}}{D^{2}}) \\ \frac{1}{D^{2}} \end{cases} = \begin{cases} 1 + (\frac{4D^{2}}{D^{2}} - \frac{4D^{2}}{D^{2}}) \\ \frac{1}{D^{2}} \end{cases} = \begin{cases} 1 + (\frac{4D^{2}}{D^{2}} - \frac{4D^{2}}{D^{2}}) \\ \frac{1}{D^{2}} \end{cases} = \begin{cases} 1 + (\frac{4D^{2}}{D^{2}} - \frac{4D^{2}}{D^{2}}) \\ \frac{1}{D^{2}} \end{cases} = \begin{cases} 1 + (\frac{4D^{2}}{D^{2}} - \frac{4D^{2}}{D^{2}}) \\ \frac{1}{D^{2}} \end{cases} = \begin{cases} 1 + (\frac{4D^{2}}{D^{2}} - \frac{4D^{2}}{D^{2}}) \\ \frac{1}{D^{2}}$$





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UNIT-III PARTIAL DIFFERENTIAL EQUATIONS Solution of Second Order Partial Differential Equations

$$= \frac{1}{D^{2}} \left[ xy + \frac{4D'(xy)}{D} - 0 \right]$$

$$= \frac{1}{D^{2}} \left[ xy + \frac{4}{D^{2}} xy \right]$$

$$= \frac{1}{D^{2}} xy + \frac{4}{D^{3}} x$$

$$= \frac{1}{D^{2}} xy + \frac{4}{D^{3}} x$$

$$= \frac{1}{D^{3}} xy + \frac{1}{D^{2}} \frac{x^{2}}{a} y \rightarrow \frac{x^{3}}{6} y$$

$$= \frac{x^{3}y}{6} + 4 \frac{x^{4}}{24}$$

$$= \frac{x^{3}y}{6} + \frac{x^{4}}{6}$$

$$= \frac{x^{3}y}{6} + \frac{x^{4}}{6}$$

$$\Rightarrow \text{Solution 98}, \quad x = CF + PI$$

The Solution 18, 
$$z = CF + FZ$$
  
= 8,  $(y+2x) + x = 6$   
+  $\frac{x^3y}{6} + \frac{x^4}{6}$ 

eJ. Find the PI of 
$$(D^2 - DD' - 2D'^2) = 2x + 3y$$
 soln:

$$PI = \frac{1}{D^{2} - DD' - 2D^{2}} (2x + 3y)$$

$$= \frac{1}{D^{2} \left[1 - \frac{D'}{D} - \frac{2D'^{2}}{D^{2}}\right]} (2x + 3y)$$

$$= \frac{1}{D^{2}} \left[1 - \left(\frac{D'}{D} + \frac{2D'^{2}}{D^{2}}\right)\right]^{-1} (2x + 3y)$$

$$= \frac{1}{D^{2}} \left[1 + \left(\frac{D'}{D} + \frac{2D'^{2}}{D^{2}}\right) + \dots\right] (2x + 3y)$$

$$= \frac{1}{D^{2}} \left[2x + 3y + \frac{D'}{D}(2x + 3y)\right]$$





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UNIT-III PARTIAL DIFFERENTIAL EQUATIONS Solution of Second Order Partial Differential Equations

$$\begin{aligned}
&= \frac{1}{D^2} \left[ (2x + 3y) + \frac{3}{D} \right] \\
&= \frac{1}{D^2} \left[ (2x + 3y) + \frac{3}{D^2} \right] \\
&= \frac{1}{D^2} \left( (2x + 3y) + \frac{3}{D^2} \right) \\
&= \frac{1}{D^2} \left( (2x + 3y) + \frac{3}{D^2} \right) \\
&= \frac{1}{D^2} \left( (2x + 3y) + \frac{3}{D^2} \right) \\
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&= \frac{1}{D^2} \left( (2x + 3y) + \frac{3}{D^2} \right) \\
&= \frac{1}{D^2} \left( (2x +$$





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$$\frac{1}{B^{2} - DD^{1} - 20D^{12}} = \frac{1}{B^{2} - DD^{1} - 20D^{12}} = \frac{1$$





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UNIT-III PARTIAL DIFFERENTIAL EQUATIONS Solution of Second Order Partial Differential Equations

$$= -\frac{\pi}{63} \left[ 8 \cos(4\pi - y) - \cos(4\pi - y) \right]$$

$$= -\frac{7\pi}{63} \cos(4\pi - y)$$

$$= -\frac{\pi}{63} \cos(4\pi - y)$$

$$= -\frac{\pi}{9} \cos(4\pi - y)$$

The solp is, 
$$X = CF + PE$$

$$X = \{ (9-4x) + \{ 2(9+5x) + \frac{2}{9}e^{5x+\frac{1}{9}} + \frac{2}{9}cos(4x-\frac{1}{9}) \}$$

$$\begin{array}{c} \text{HVO} \\ \text{J.} \left( D^{9} + 4DD' - 5D'^{2} \right) & \text{X} = e^{2X - 9} + \text{Spn} \left( x - 2y \right) \\ \text{2J.} \left( D^{9} - DD' - 30D'^{3} \right) & \text{X} = xy + e^{6X + 9} \end{array}$$

Solve 
$$x+3-6t = y\cos x$$
  
Solve:

Civen  $\frac{\partial^2 x}{\partial x^2} + \frac{\partial^2 x}{\partial x \partial y} + 6\frac{\partial^2 x}{\partial y^2} = y\cos x$   
 $(D^2 + DD^1 - 6D^{12})x = y\cos x$   
 $(D^2 + DD^1 - 6D^{12})x = y\cos x$   
AE  $m^2 + m - b = 0$   
 $(m+3)(m-2) = 0$   
 $m = -3, 2$   
 $CF = \frac{1}{5}, (y-3x) + \frac{1}{5}, (y+2x)$   
 $PI = \frac{1}{5}$   
 $(D^2 + DD^1, (-1)^2)$   $y\cos x$ 





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UNIT-III PARTIAL DIFFERENTIAL EQUATIONS Solution of Second Order Partial Differential Equations

$$\begin{cases} 2c + c + D - aD \end{cases}$$

$$= \frac{1}{(D+3D')} (D-aD') \qquad y \cos x \qquad p \rightarrow c$$

$$= \frac{1}{(D+3D')} \int (c-ax) \cos x \, dx$$

$$= \frac{1}{(D+3D')} \int (c-2x) S^{q} dx - (-2)(-\cos x)$$

$$= \frac{1}{(D+3D')} \int y S^{q} dx - a \cos x \int a c + a$$