



SNS COLLEGE OF TECHNOLOGY



Coimbatore-35

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DEPARTMENT OF INFORMATION TECHNOLOGY

19CSE303 - ARTIFICIAL INTELLIGENCE

III YEAR IV SEM

UNIT II – LOGICAL REASONING

TOPIC – GraphPlan



GraphPlan

<http://www.cs.cmu.edu/~avrim/graphplan.html>



- Many planning systems use ideas from Graphplan:
 - ▲ IPP, STAN, SGP, Blackbox, Medic, FF, FastDownward
- History
 - ▲ Before GraphPlan appeared in 1995, most planning researchers were working under the framework of “plan-space search” (we will not cover this topic)
 - ▲ GraphPlan outperformed those prior planners by orders of magnitude
 - ▲ GraphPlan started researchers thinking about fundamentally different frameworks
- Recent planning algorithms are much more effective than GraphPlan
 - ▲ However, many have been influenced by GraphPlan



Big Picture



- A big source of inefficiency in search algorithms is the large branching factor
- GraphPlan reduces the branching factor by searching in a special data structure

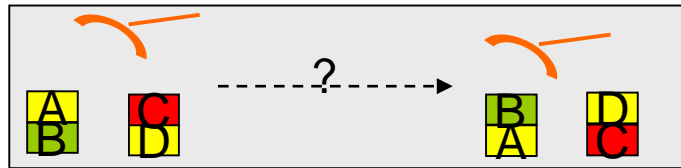
- Phase 1 – Create a Planning Graph
 - ▲ built from initial state
 - ▲ contains actions and propositions that are possibly reachable from initial state
 - ▲ does not include unreachable actions or propositions
- Phase 2 - Solution Extraction
 - ▲ Backward search for the solution in the planning graph
 - backward from goal



Layered Plans



- Graphplan searches for **layered plans** (often called parallel plans)
- A layered plan is a sequence of **sets** of actions
 - ▲ actions in the same set must be **compatible**
 - a1 and a2 are compatible iff a1 does not delete preconditions or positive effects of a2 (and vice versa)
 - ▲ all sequential orderings of compatible actions gives same result



Layered Plan: (a two layer plan)

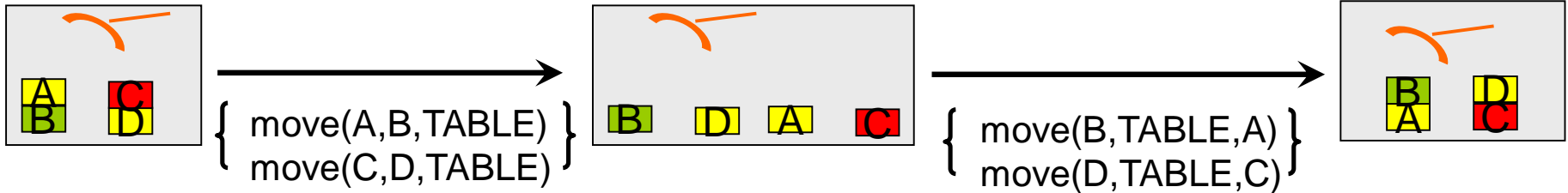
$$\left\{ \begin{array}{l} \text{move}(A,B,\text{TABLE}) \\ \text{move}(C,D,\text{TABLE}) \end{array} \right\} ; \left\{ \begin{array}{l} \text{move}(B,\text{TABLE},A) \\ \text{move}(D,\text{TABLE},C) \end{array} \right\}$$



Executing a Layered Plans



- A set of actions is applicable in a state if all the actions are applicable.
- Executing an applicable set of actions yields a new state that results from executing each individual action (order does not matter)





Planning Graph



*A **literal** is just a positive or negative proposition*

- A planning graph has a sequence of levels that correspond to time-steps in the plan:
 - ▲ Each level contains a set of literals and a set of actions
 - ▲ Literals are those that could possibly be true at the time step
 - ▲ Actions are those that their preconditions could be satisfied at the time step.
- Idea: construct superset of literals that could be possibly achieved after an n -level layered plan
 - ▲ Gives a compact (but approximate) representation of states that are reachable by n level plans



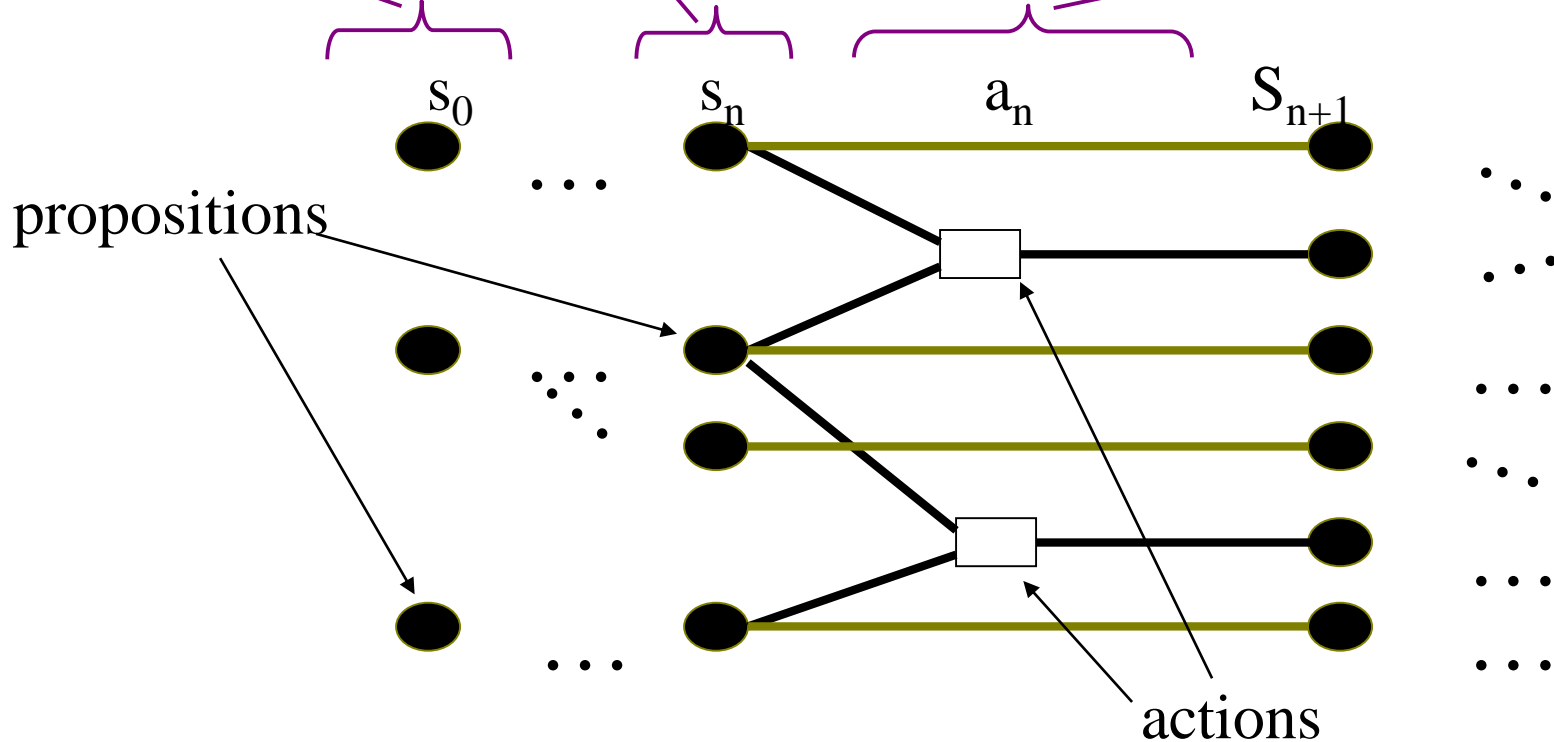
Planning Graph



state-level 0:
propositions true
in s_0

state-level n : literals that
may possibly be true after
some n level plan

action-level n : actions that
may possibly be applicable
after some n level plan

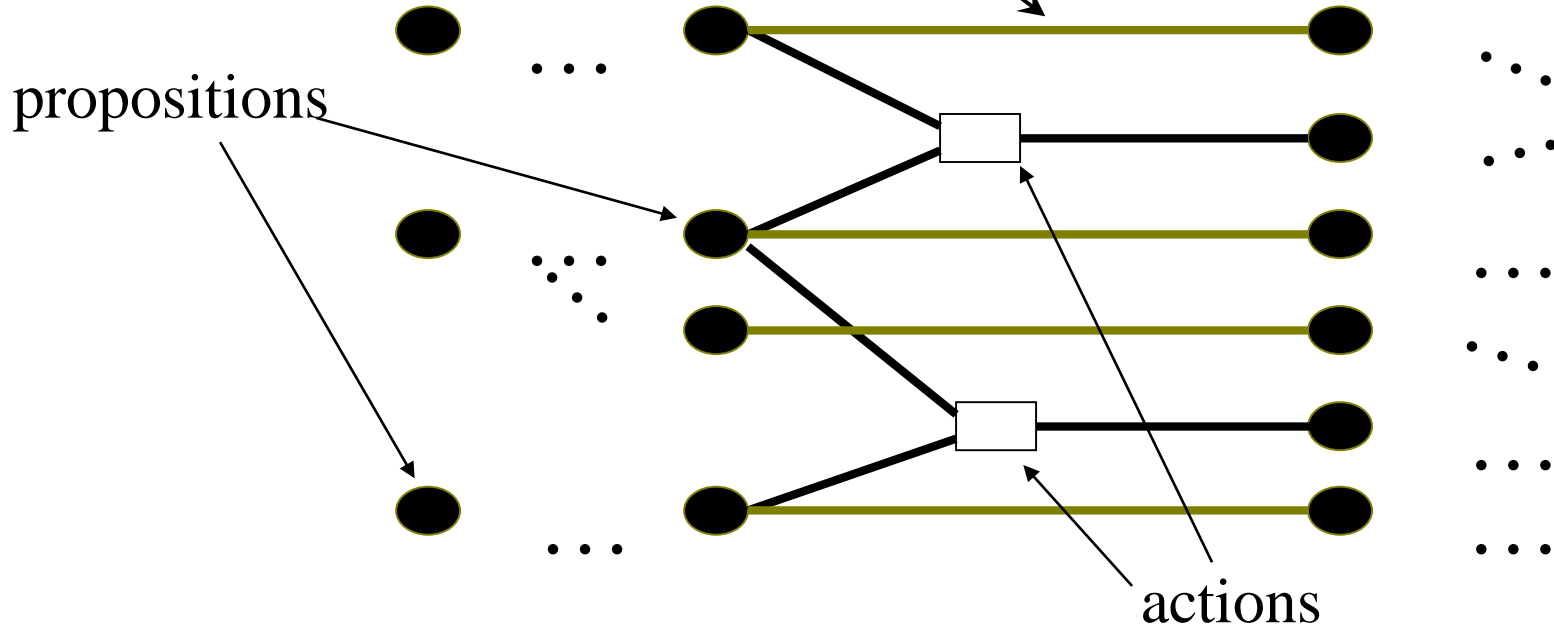




Planning Graph



- maintenance action (persistence actions)
 - ▲ represents what happens if no action affects the literal
 - ▲ include action with precondition c and effect c , for each literal c





Graph expansion

- Initial proposition layer
 - ▲ Just the propositions in the initial state
- Action layer n
 - ▲ If all of an action's preconditions are in proposition layer n , then add action to layer n
- Proposition layer $n+1$
 - ▲ For each action at layer n (including persistence actions)
 - ▲ Add all its effects (both positive and negative) at layer $n+1$
(Also allow propositions at layer n to persist to $n+1$)
- Propagate mutex information
(we'll talk about this in a moment)



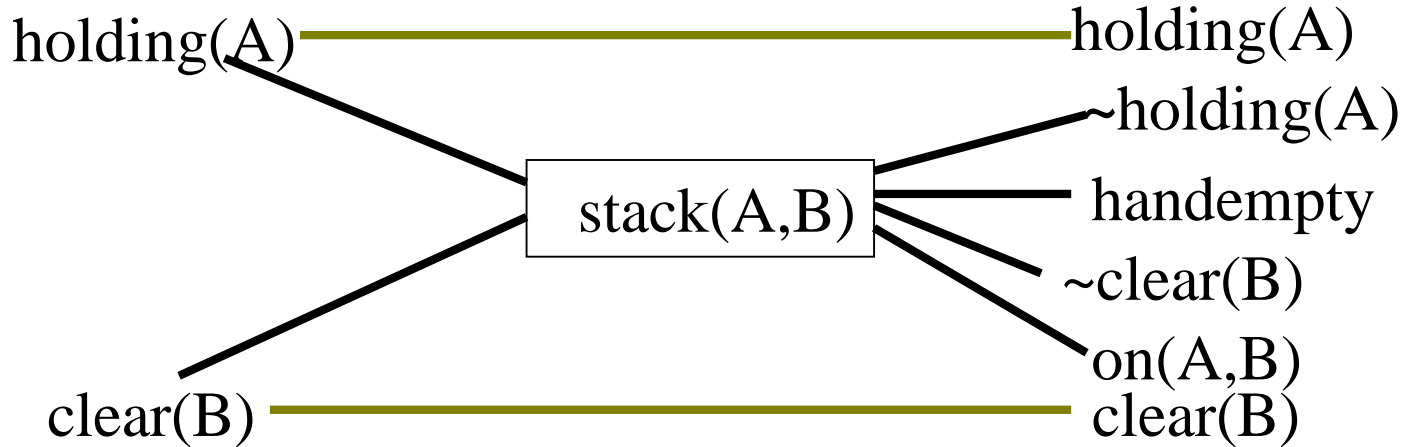
Example



stack(A,B)

precondition: holding(A), clear(B)

effect: \sim holding(A), \sim clear(B), on(A,B), clear(B), handempty





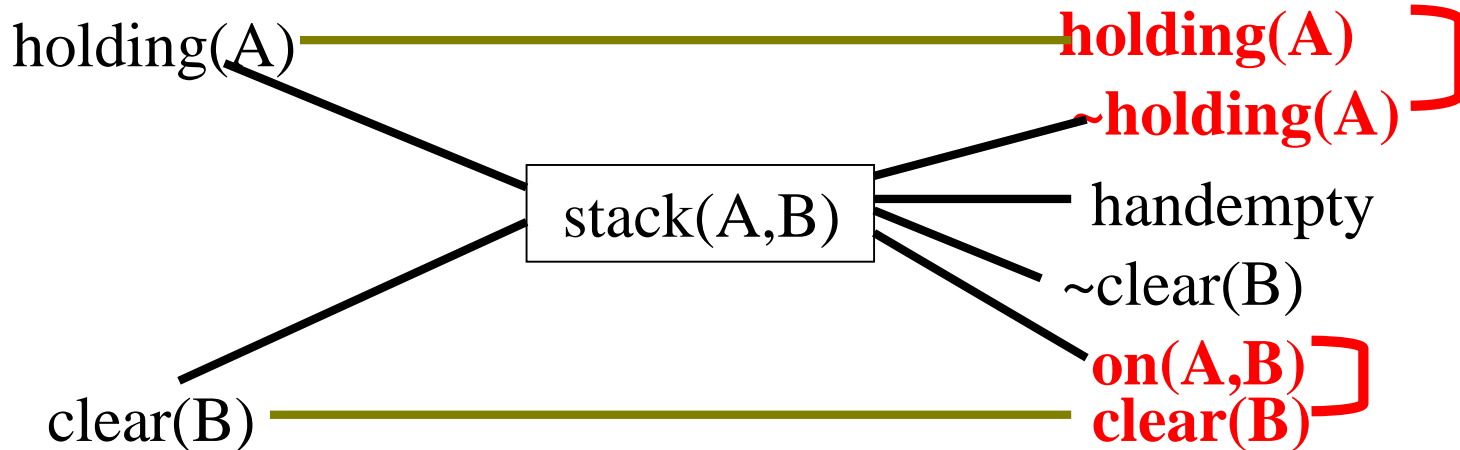
Example



stack(A,B)

precondition: holding(A), clear(B)

effect: \sim holding(A), \sim clear(B), on(A,B), clear(B), handempty



Notice that not all literals in s1 can be made true simultaneously after 1 level:
e.g. holding(A), \sim holding(A) and on(A,B), clear(B)



Mutual Exclusion (Mutex)



- Mutex between pairs of actions at layer n means
 - ▲ no valid plan could contain both actions at layer n
 - ▲ E.g., `stack(a,b)`, `unstack(a,b)`
- Mutex between pairs of literals at layer n means
 - ▲ no valid plan could produce both at layer n
 - ▲ E.g., `clear(a)`, `~clear(a)`
`on(a,b)`, `clear(b)`
- GraphPlan checks pairs only
 - ▲ mutex relationships can help rule out possibilities during search in phase 2 of Graphplan



Action Mutex: condition 1

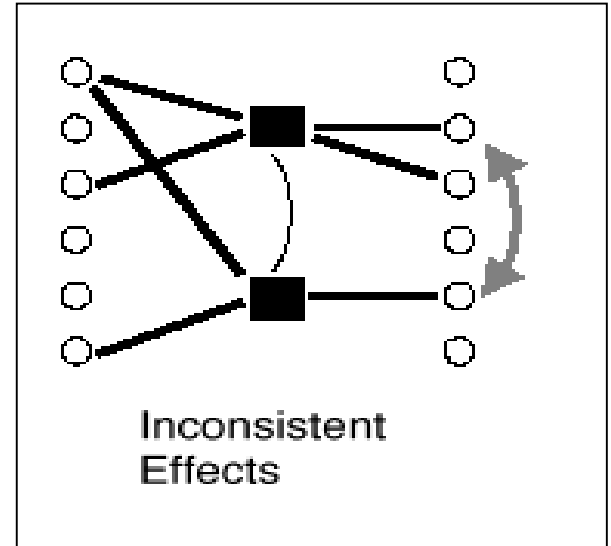
- Inconsistent effects

- ▶ an effect of one negates an effect of the other

- E.g., $\text{stack}(a,b)$ & $\text{unstack}(a,b)$

add handempty

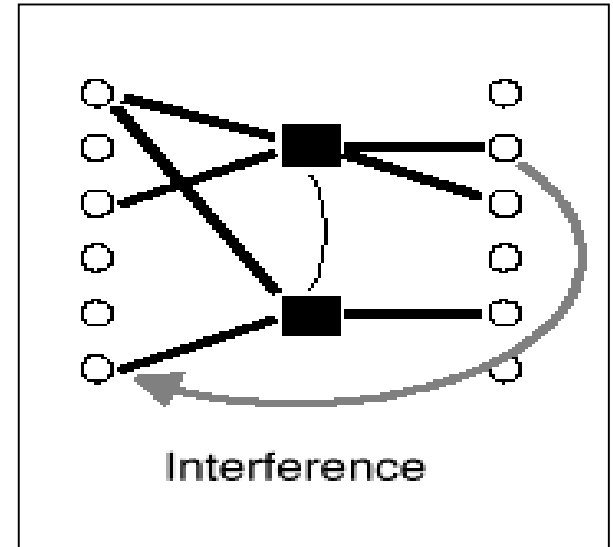
delete handempty
(add \sim handempty)





Action Mutex: condition 2

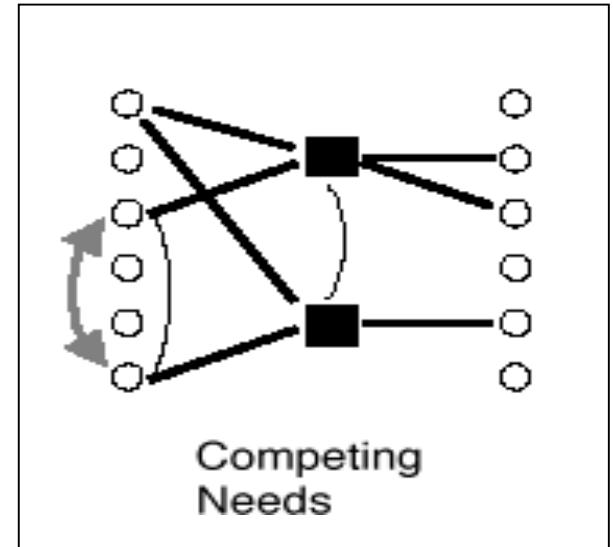
- *Interference* :
 - ▶ one deletes a precondition of the other
- E.g., $\text{stack}(a,b)$ & $\text{putdown}(a)$
 - ↓ deletes holding(a)
 - ↓ needs holding(a)





Action Mutex: condition 3

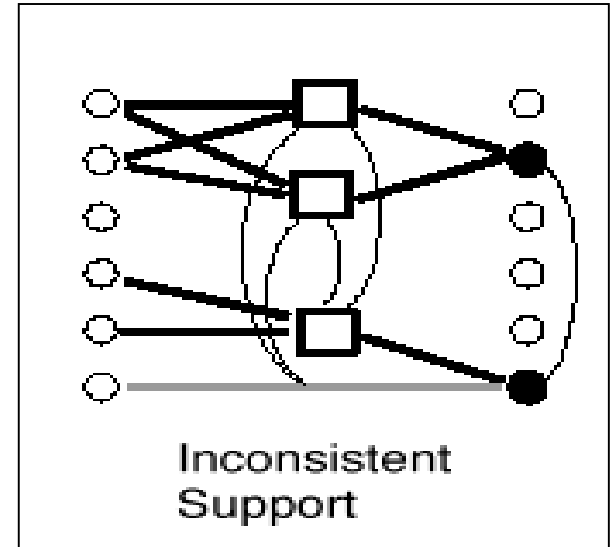
- *Competing needs:*
 - ▶ they have mutually exclusive preconditions
 - ▶ Their preconditions can't be true at the same time





Literal Mutex: two conditions

- *Inconsistent support* :
 - ▶ one is the negation of the other
E.g., handempty and \sim handempty
 - ▶ or all ways of achieving them via actions are pairwise mutex





Example – Dinner Date



- Suppose you want to prepare dinner as a surprise for your sweetheart (who is asleep)
 - ▶ Initial State: {cleanHands, quiet, garbage}
 - ▶ Goal: {dinner, present, ~garbage}
 - ▶ **Action Preconditions** **Effects**

cook	cleanHands	dinner
wrap	quiet	present
carry	<i>none</i>	~garbage, ~cleanHands
dolly	<i>none</i>	~garbage, ~quiet
- Also have the “maintenance actions”



Example – Plan Graph Construction



s0

a0

garbage

carry

cleanhands

dolly

quiet

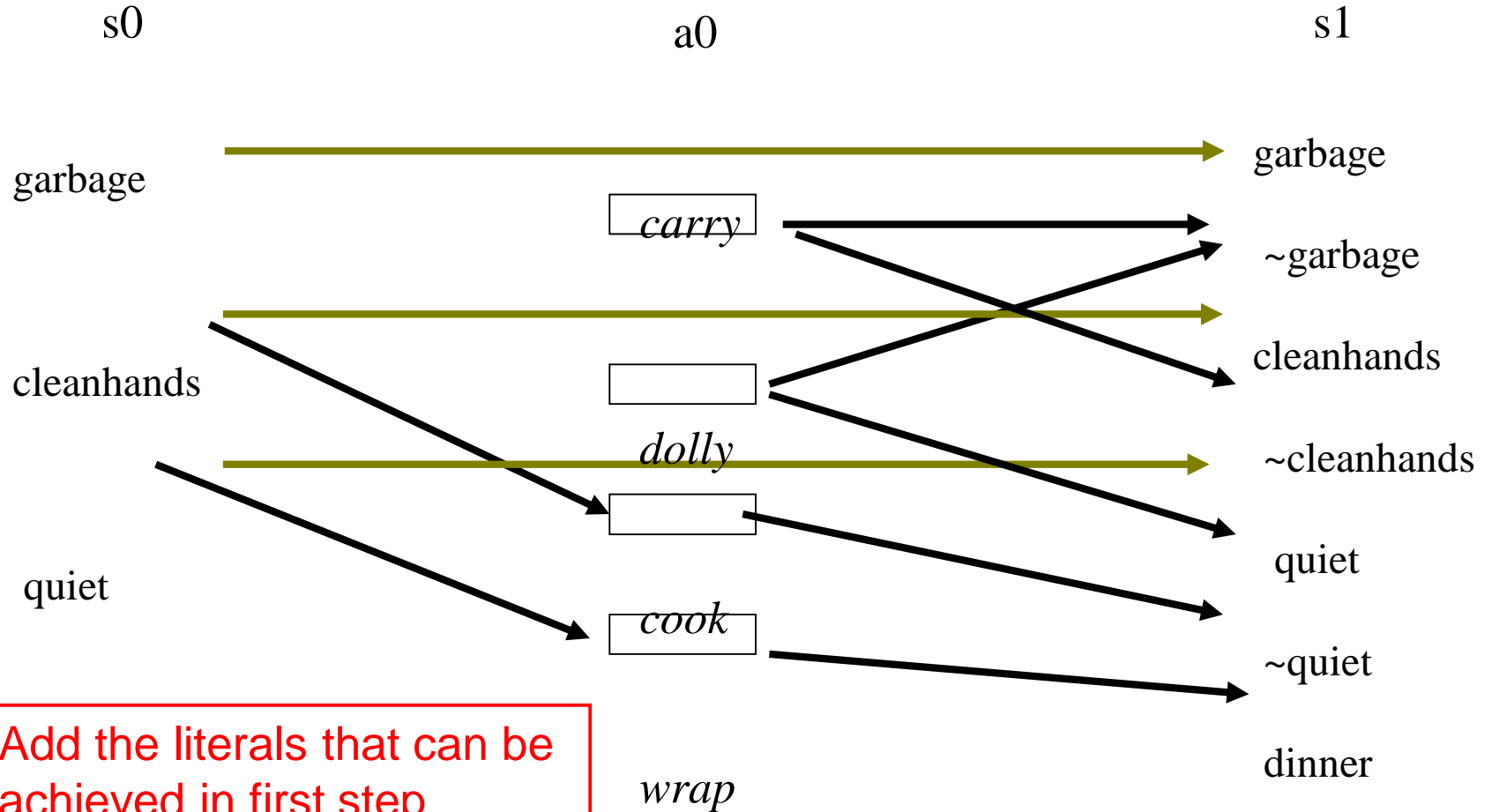
cook

wrap

Add the actions that can be executed in initial state

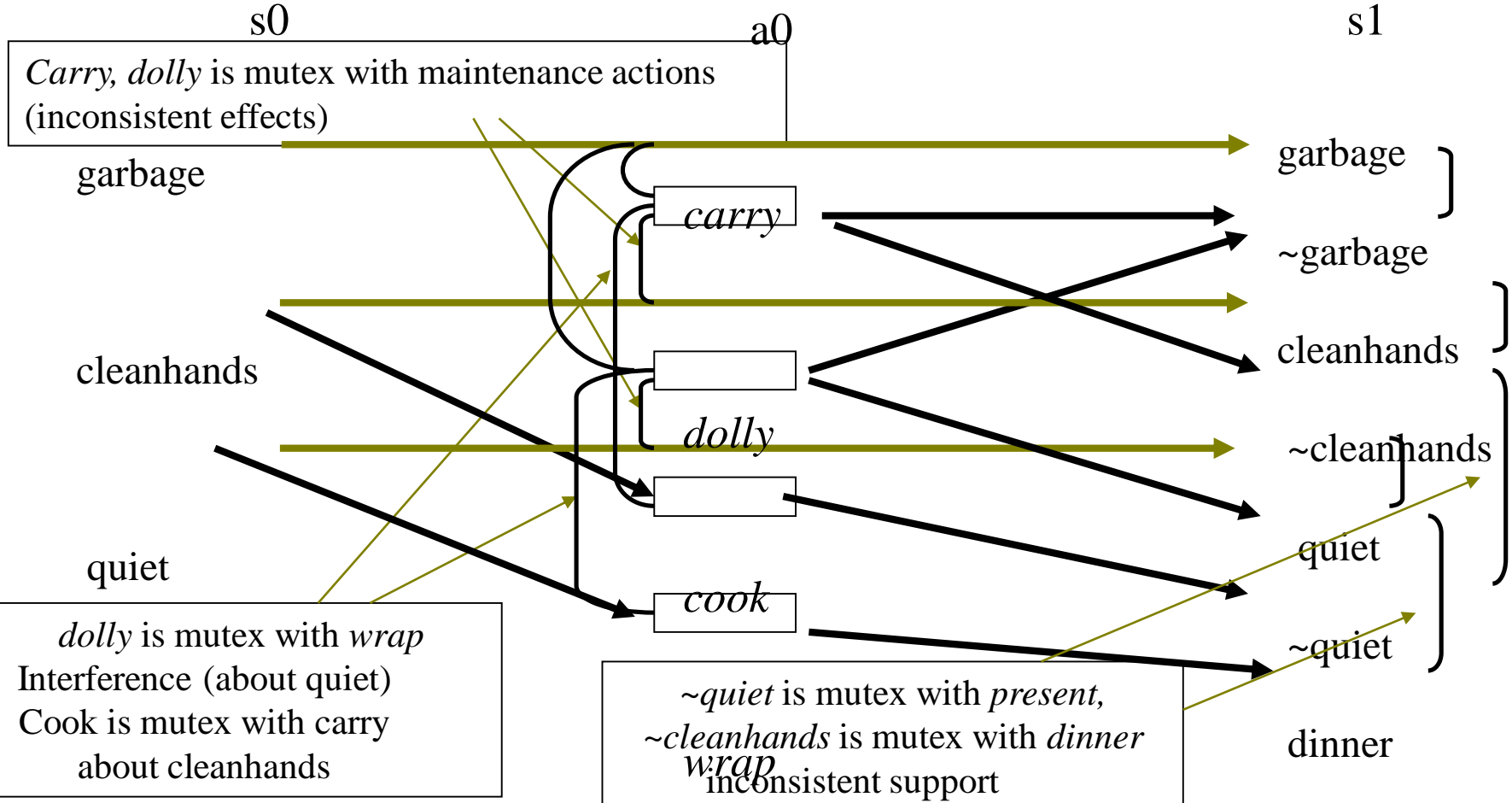


Example - continued





Example - continued

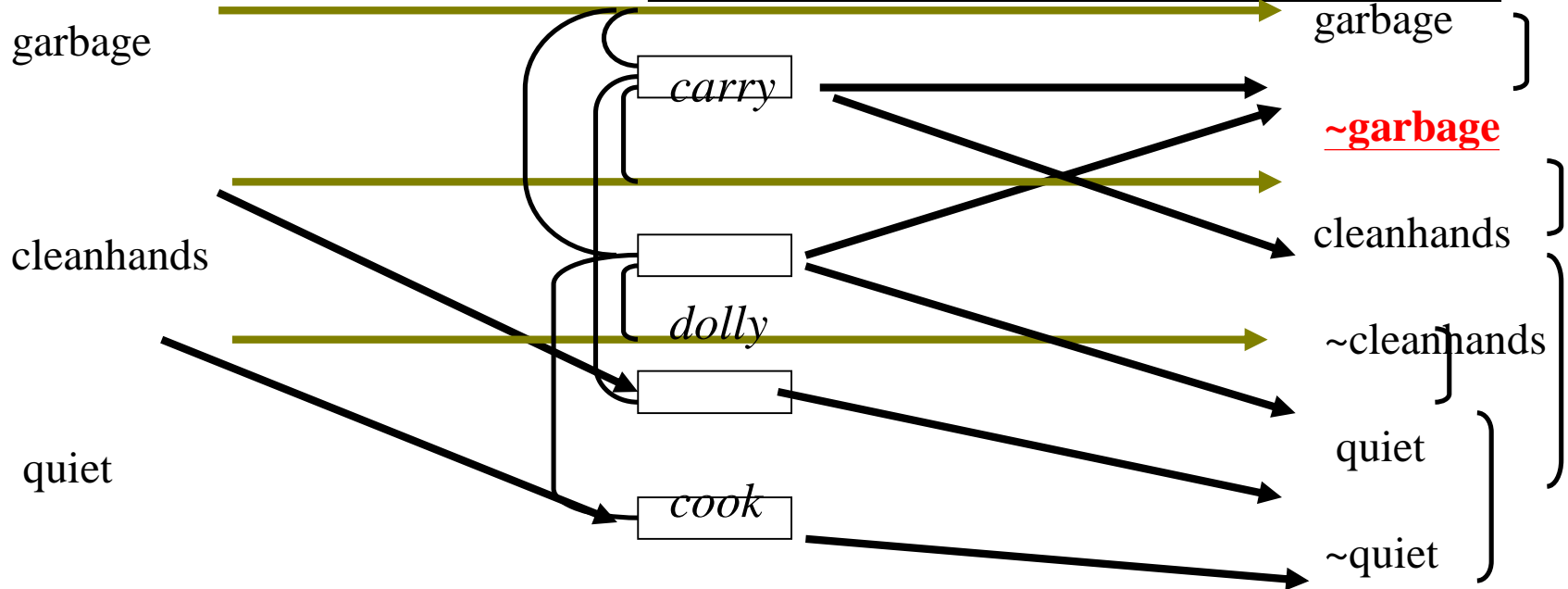




Do we have a solution?



The goal is: {**dinner**, **present**, **~garbage**}
 All are possible in layer s1
 None are mutex with each other



There is a chance that a plan exists
 Now try to find it – solution extraction

wrap

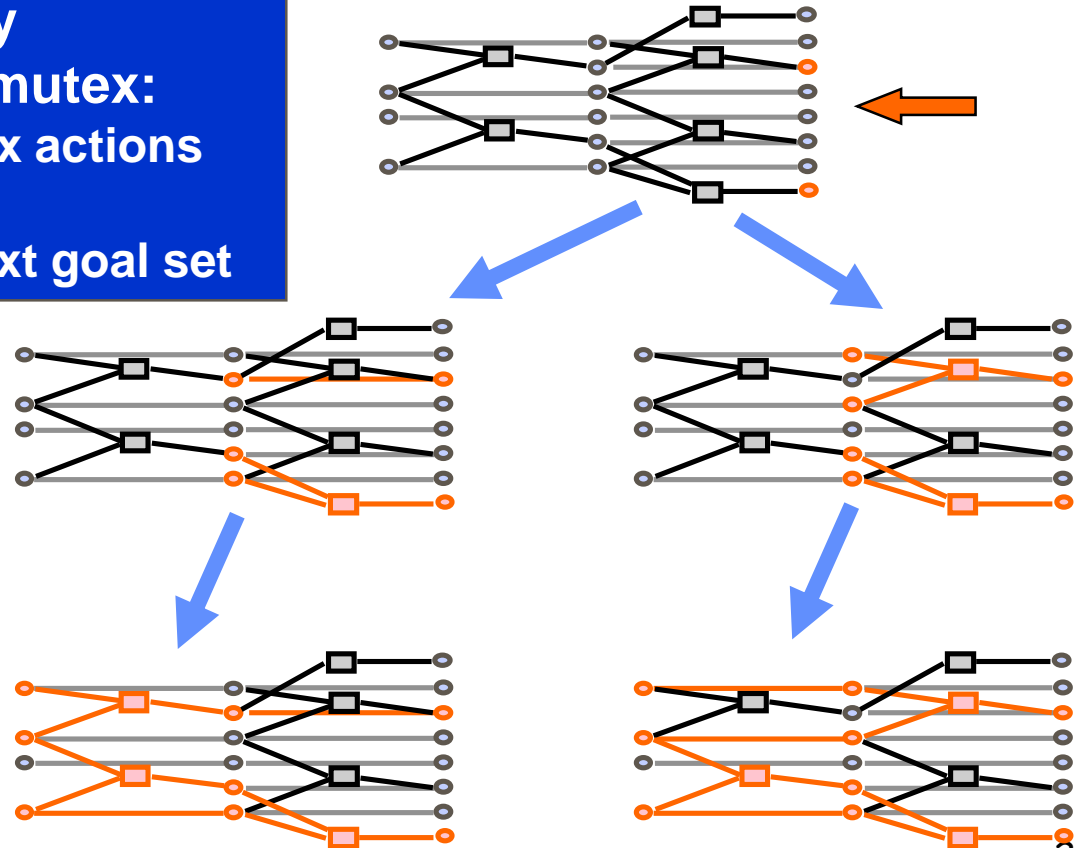
dinner

Solution Extraction: Backward Search

Repeat until goal set is empty

If goals are present & non-mutex:

- 1) Choose set of non-mutex actions to achieve each goal
- 2) Add preconditions to next goal set





Searching for a solution plan



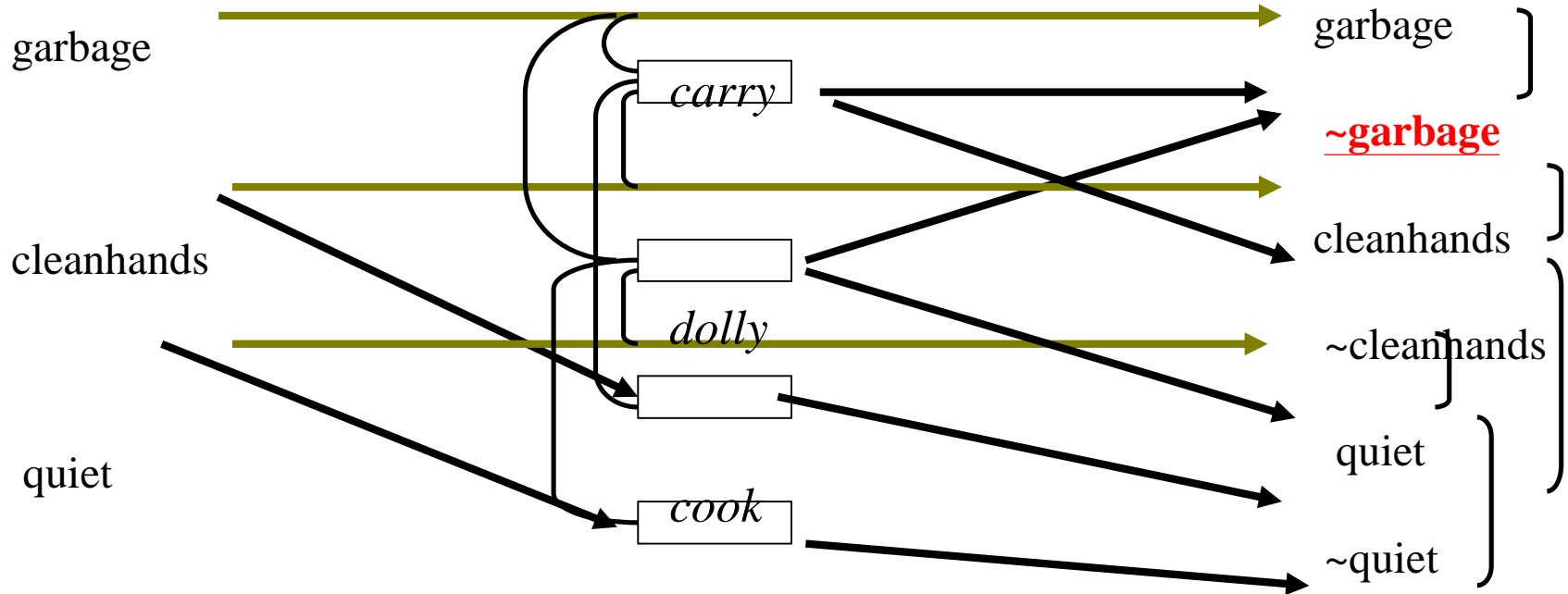
- Backward chain on the planning graph
- Achieve goals level by level
- At level k , pick a subset of non-mutex actions to achieve current goals. Their preconditions become the goals for $k-1$ level.
- Build goal subset by picking each goal and choosing an action to add. Use one already selected if possible (backtrack if can't pick non-mutex action)
- If we reach the initial proposition level and the current goals are in that level (i.e. they are true in the initial state) then we have found a successful layered plan



Possible Solutions



- Two possible sets of actions for the goals at layer s1:
 {wrap, cook, dolly} and {wrap, cook, carry}
- Neither set works -- both sets contain actions that are mutex

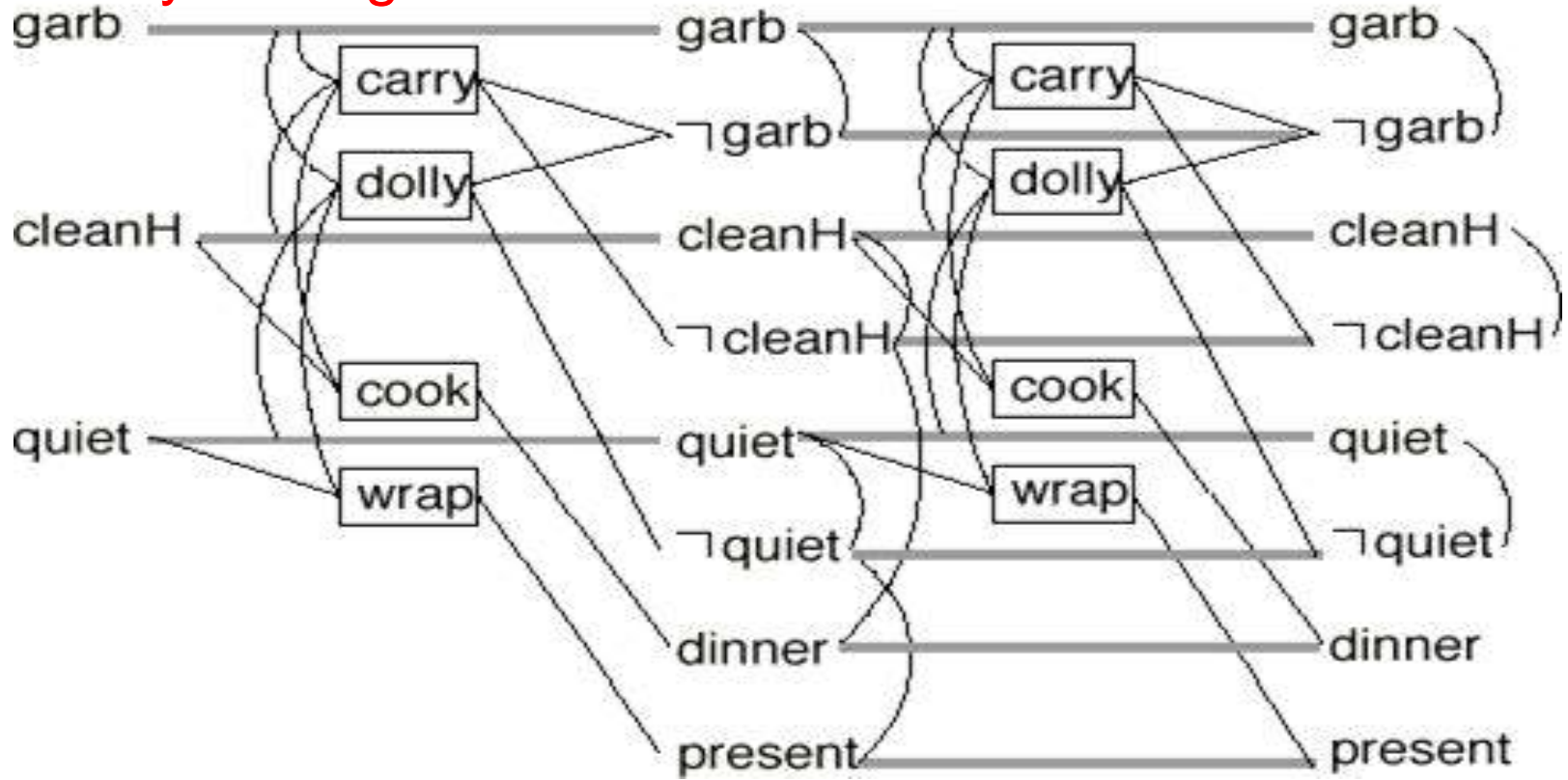




Add new layer...



Adding a layer provided new ways to achieve propositions
This may allow goals to be achieved with non-mutex actions





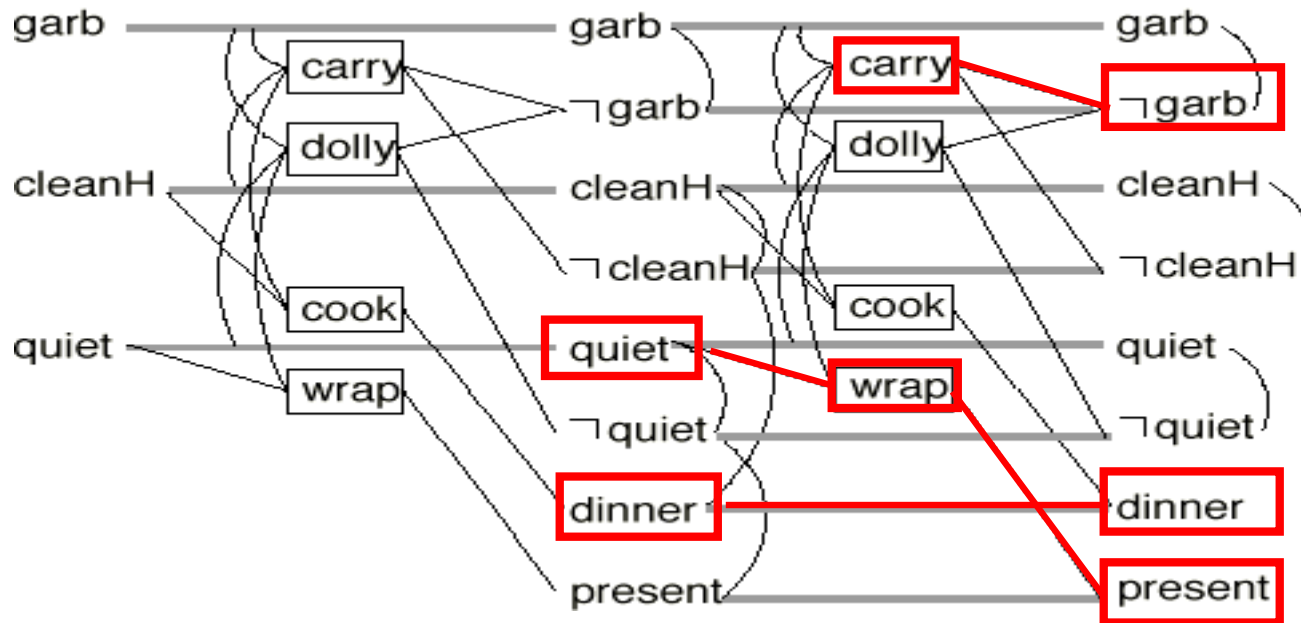
Do we have a solution?



Several action sets look OK at layer 2

Here's one of them

We now need to satisfy their preconditions



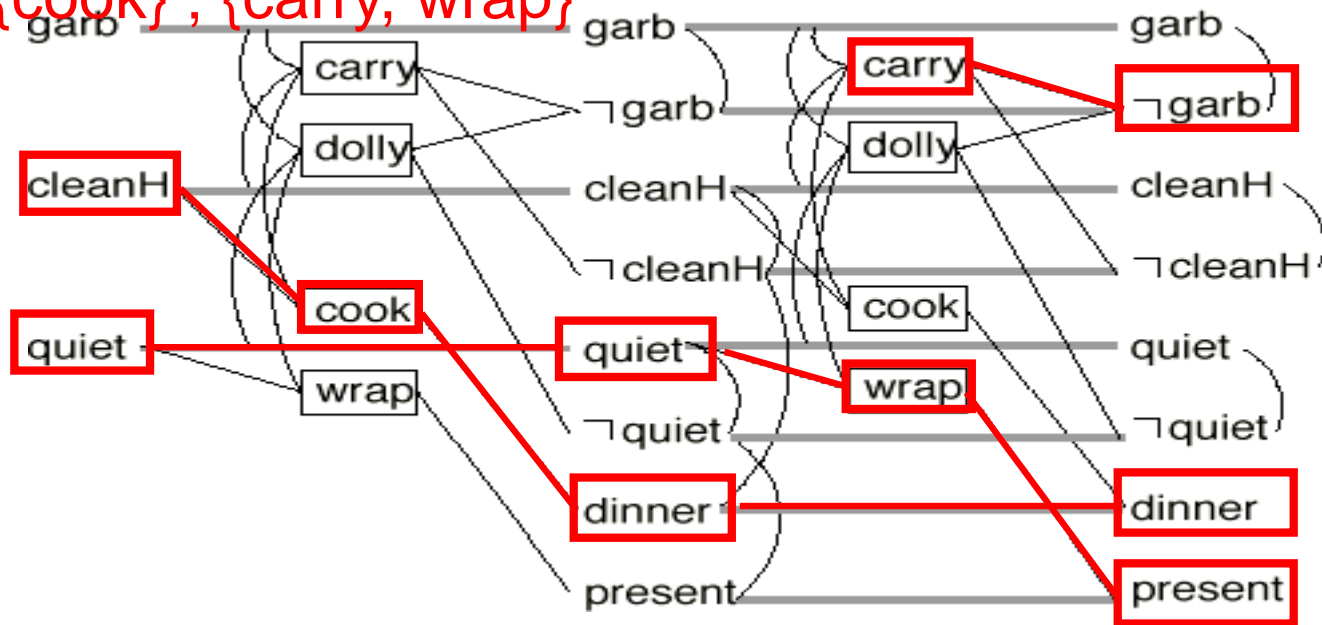


Do we have a solution?



The action set {cook, quite} at layer 1 supports preconditions
 Their preconditions are satisfied in initial state
 So we have found a solution:

{cook} ; {carry, wrap}

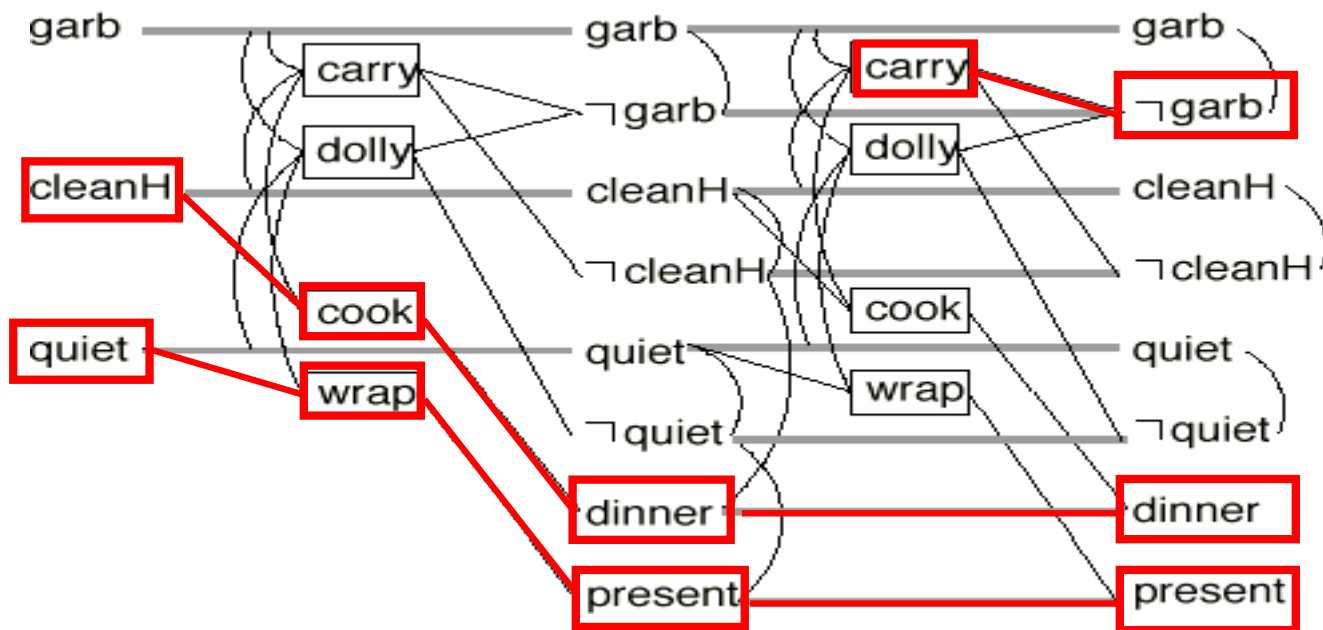




Another solution:



{cook,wrap} ; {carry}





GraphPlan algorithm



- Grow the planning graph (PG) to a level n such that all goals are reachable and not mutex
 - ▲ necessary but **insufficient** condition for the existence of an n level plan that achieves the goals
 - ▲ if PG levels off before non-mutex goals are achieved then fail
- Search the PG for a valid plan
- If none found, add a level to the PG and try again
- If the PG levels off and still no valid plan found, then return failure

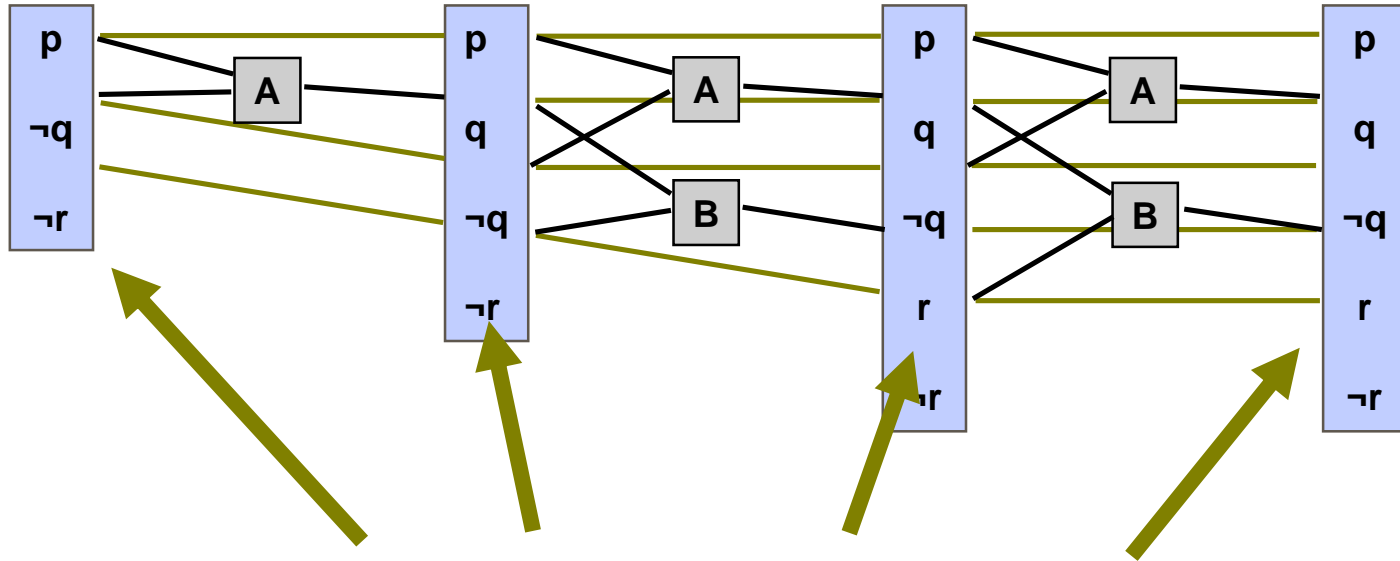
Termination is guaranteed by PG properties

This termination condition does not guarantee completeness. Why?

A more complex termination condition exists that does, but we won't cover in class (see book material on termination)



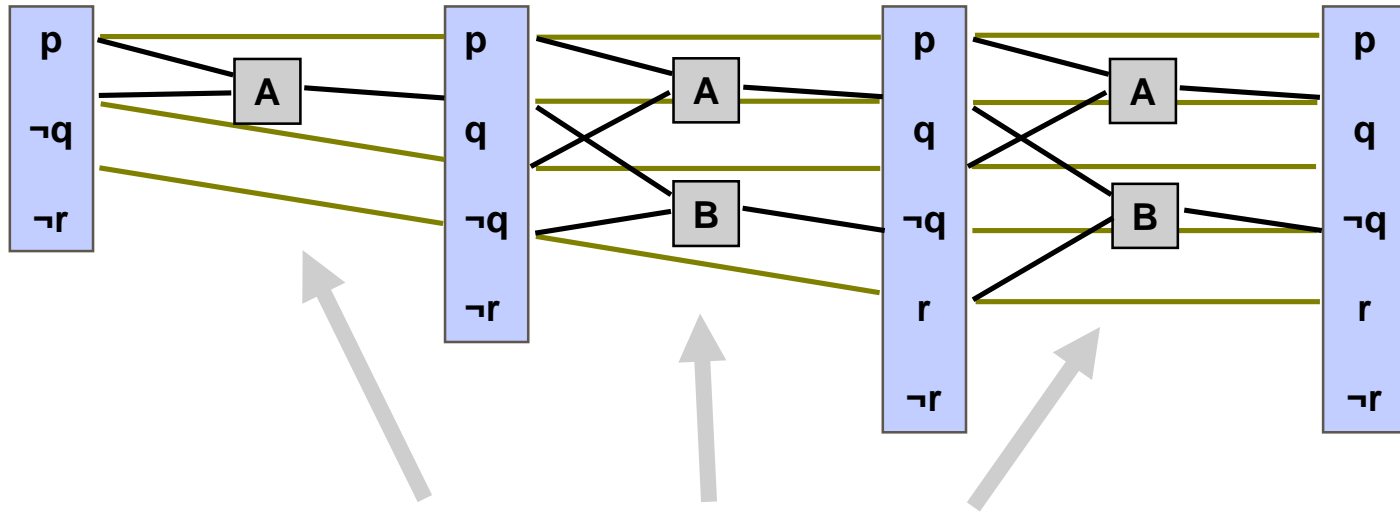
Property 1



Propositions monotonically increase
(always carried forward by no-ops)



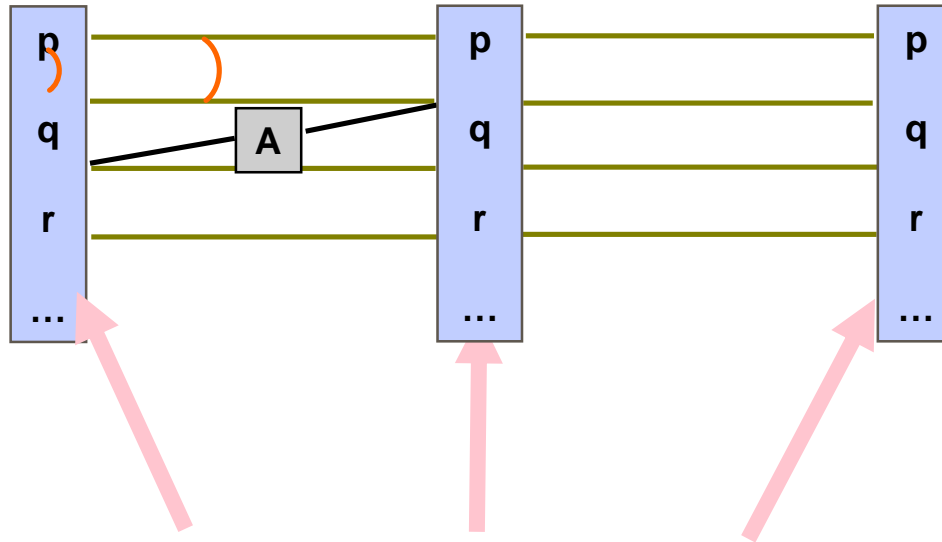
Property 2



Actions monotonically increase



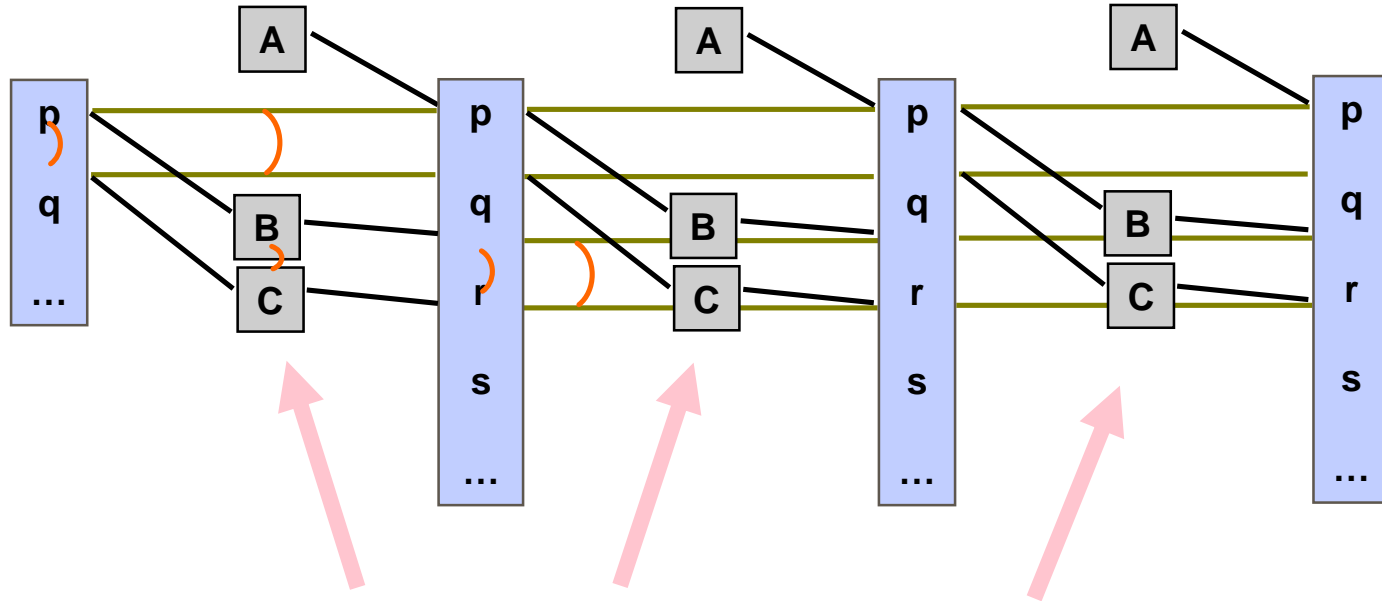
Properties 3



- Proposition mutex relationships monotonically decrease
- Specifically, if p and q are in layer n and are not mutex then they will not be mutex in future layers.



Properties 4



Action mutex relationships monotonically decrease



Properties 5



Planning Graph 'levels off'.

- After some time k all levels are identical
 - ▲ In terms of propositions, actions, mutexes
- This is because there are a finite number of propositions and actions, the set of literals never decreases and mutexes don't reappear.



Important Ideas



- Plan graph construction is polynomial time
 - ▲ Though construction can be expensive when there are many “objects” and hence many propositions
- The plan graph captures important properties of the planning problem
 - ▲ Necessarily unreachable literals and actions
 - ▲ Possibly reachable literals and actions
 - ▲ Mutually exclusive literals and actions
- Significantly prunes search space compared to previously considered planners
- Plan graphs can also be used for deriving admissible (and good non-admissible) heuristics

Planning Graphs for Heuristic Search

- After GraphPlan was introduced, researchers found other uses for planning graphs.
- One use was to compute heuristic functions for guiding a search from the initial state to goal
 - ▲ Sect. 10.3.1 of book discusses some approaches
- First lets review the basic idea behind heuristic search



Planning as heuristic search



- Use standard search techniques, e.g. A^* , best-first, hill-climbing etc.
 - ▲ Find a path from the initial state to a goal
 - ▲ Performance depends very much on the quality of the “heuristic” state evaluator
- Attempt to extract heuristic state evaluator automatically from the Strips encoding of the domain
- The planning graph has inspired a number of such heuristics



Review: Heuristic Search



- A* search is a best-first search using node evaluation

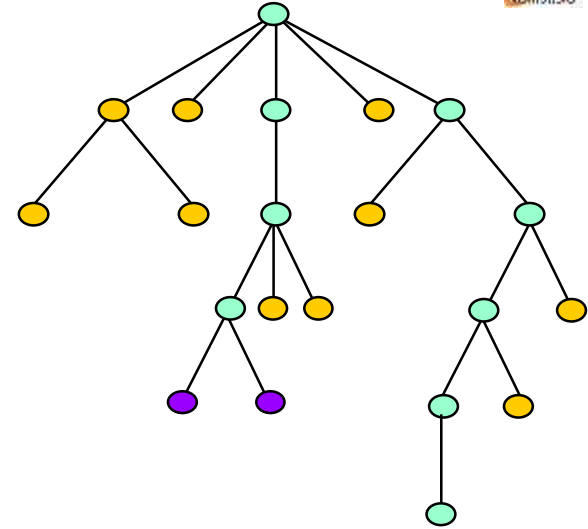
$$f(s) = g(s) + h(s)$$

where

$g(s)$ = accumulated cost/number of actions

$h(s)$ = estimate of future cost/distance to goal

- $h(s)$ is **admissible** if it does not overestimate the cost to goal
- For admissible $h(s)$, A* returns optimal solutions





Simple Planning Graph Heuristics



- Given a state s , we want to compute a heuristic $h(s)$.
- **Approach 1:** Build planning graph from s until all goal facts are present w/o mutexes between them
 - ▲ Return the # of graph levels as $h(s)$
 - Admissible. Why?
 - Can sometimes grossly underestimate distance to goal
- **Approach 2:** Repeat above but for a “sequential planning graph” where only one action is allowed to be taken at any time
 - ▲ Implement by including mutexes between all actions
 - ▲ Still admissible, but more accurate.



Relaxed Plan Heuristics



- Computing those heuristics requires “only” polynomial time, but must be done many times during search (think millions)
 - ▲ Mutex computation is quite expensive and adds up
 - ▲ Limits how many states can be searched
- *A very popular approach is to ignore mutexes*
 - ▲ Compute heuristics based on **relaxed problem** by assuming no delete effects
 - ▲ Much more efficient computation
- This is the idea behind the very well-known planner FF (for FastForward)
 - ▲ Many state-of-the-art planners derive from FF



Heuristic from Relaxed Problem



- Relaxed problem ignores delete lists on actions

PutDown(A,B):

PRE: { holding(A), clear(B) }

ADD: { on(A,B), handEmpty, clear(A) }

DEL: { holding(A), clear(B) }

PutDown(B,A):

PRE: { holding(B), clear(A) }

ADD: { on(B,A), handEmpty, clear(B) }

DEL: { holding(B), clear(A) }



Problem Relaxation

PutDown(A,B):

PRE: { holding(A), clear(B) }

ADD: { on(A,B), handEmpty, clear(A) }

DEL: { }

PutDown(B,A):

PRE: { holding(B), clear(A) }

ADD: { on(B,A), handEmpty, clear(B) }

DEL: { }



Heuristic from Relaxed Problem



- BUT – still finding optimal solution to relaxed problem is NP-hard
 - ▲ So we will approximate it
 - ▲ and do so very quickly

- One way is to explicitly search for a relaxed plan
 - ▲ Finding a relaxed plan can be done in polynomial time using a planning graph
 - ▲ Take relaxed-plan length to be the heuristic value
 - ▲ FF (for FastForward) uses this approach



FF Planner: finding relaxed plans

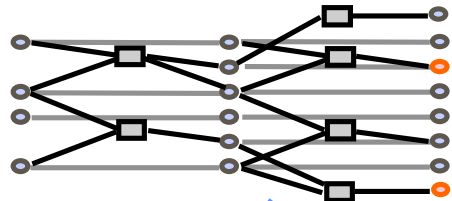


- Consider running Graphplan while ignoring the delete lists
 - ▲ No mutexes (avoid computing these altogether)
 - ▲ Implies no backtracking during solution extraction search!
 - ▲ So we can find a relaxed solutions efficiently
- After running the “no-delete-list Graphplan” then the # of actions in layered plan is the heuristic value
 - ▲ Different choices in solution extraction can lead to different heuristic values
- The planner FastForward (FF) uses this heuristic in forward state-space best-first search
 - ▲ Also includes several improvements over this

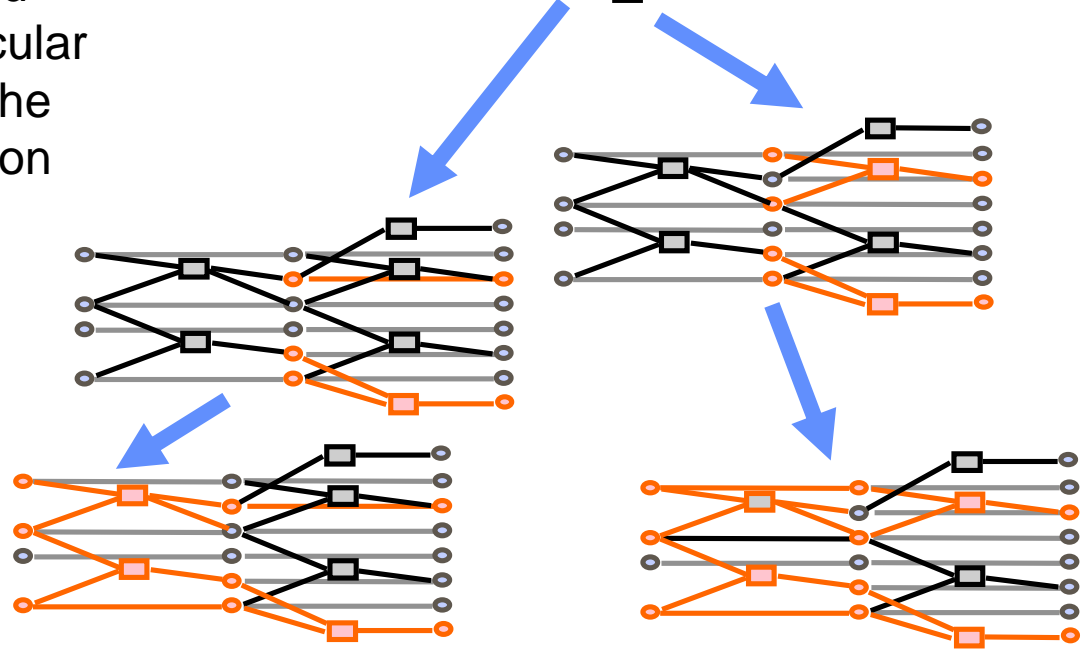
Example: Finding Relaxed Plans



The value returned depends on particular choices made in the backward extraction



Relaxed plan graph (no mutexes)



Heuristic value = 3

Heuristic value = 4



Summary



- Many of the state-of-the-art planners today are based on heuristic search
 - ▲ Popularized by the planner FF, which computes relaxed plans with blazing speed
- Lots of work on make heuristics more accurate without increasing the computation time too much
 - ▲ Trade-off between heuristic computation time vs. heuristic accuracy
- Most of these planners are not optimal
 - ▲ The most effective optimal planners tend to use different frameworks (e.g. planning as satisfiability)



Endgame Logistics



- Final Project Presentations
 - ▲ Tuesday, March 19, 3-5, KEC2057
 - ▲ Powerpoint suggested (email to me before class)
 - Can use your own laptop if necessary (e.g. demo)
 - ▲ 10 minutes of presentation per project
 - Not including questions
- Final Project Reports
 - ▲ Due: Friday, March 22, 12 noon

THANK YOU