Fundamentals of the Analysis of Algorithm Efficiency

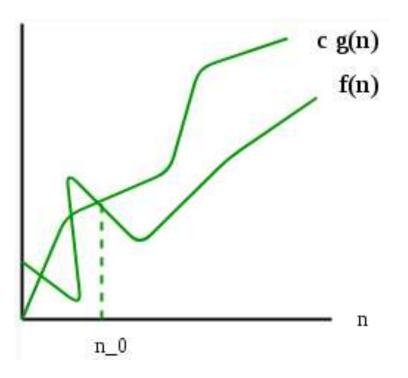
- Analysis Framework
- Asymptotic Notations and its properties
- Mathematical analysis of Recursive algorithms
- Mathematical analysis of Non Recursive algorithms

# Asymptotic Notations and its properties

- Analysis framework Efficiency order of growth
- Order of growth change in order of input size
- Study of performance changes of algorithm with change in order of input → Asymptotic Analysis
- Compare and Rank order of growth  $\rightarrow$  3 Notations
- Mathematical tool to represent the time complexity of algorithm for Asymptotic Analysis is *Asymptotic Notation*
- <u>Notations</u>
  - Big O Notation (Worst-case efficiency)
  - Big  $\Omega$  Notation (Best-case efficiency)
  - Big Θ Notation (Average-case efficiency)

## Big O Notation (Worst-case efficiency)

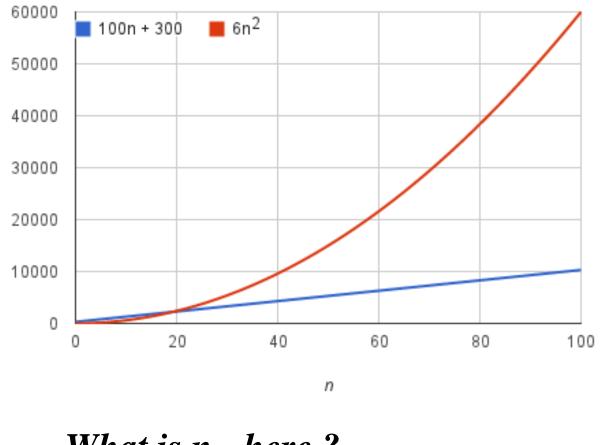
- Upper bound of the running time of an algorithm
- O(g(n)) = { f(n): there exist positive constants c and n0 such that 0 ≤ f(n) ≤ cg(n) for all n ≥ n0 }
- $f(n) \in O(g(n))$



## Big O Notation (Worst-case efficiency)

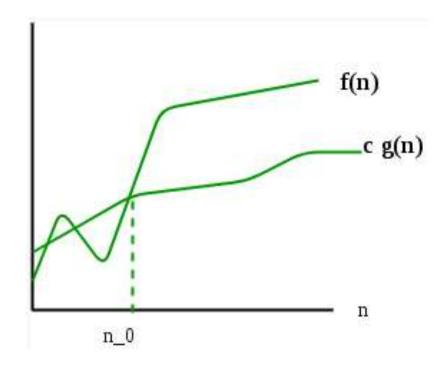
n	f(n) = 100n + 300	$g(n) = 6n^2$
1	400	6
2	500	24
3	600	54
4	700	96
5	800	150
•		
•		
10	1300	600
•		
15	1800	1350
20	2300	2400
21	2400	2646
22	2500	2904
23	2600 Design and Analysis of Algorithm -	3174
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## Big O Notation (Worst-case efficiency) - Example



## Big $\Omega$ Notation (Best-case efficiency)

- lower bound of the running time of the algorithm
- $\Omega(g(n)) = \{ f(n): \text{ there exist positive constants } c \text{ and } n_0 \text{ such that} \\ 0 \le cg(n) \le f(n) \text{ for all } n \ge n_0 \}$



## Big $\Theta$ Notation (Average-case efficiency)

- Encloses the function from above and below
- upper and the lower bound of the running time of algorithm
- Θ(g(n)) = { f(n): there exist positive constants c1, c2 and n0 such that 0 ≤ c1g(n) ≤ f(n) ≤ c2g(n) for all n ≥ n0 }

