UNIT II – Brute Force and Divide and Conquer

Brute Force Design Technique

- Selection Sort
- Bubble Sort
- Sequential Search
- Closest pair and Convex hull problem
- Travelling Salesman problem
- Knapsack problem
- Assignment problem

Sequential Search – Traditional method

- Worst case O(n) element not found/ search element is in last position of list
- Best case O(1) element found at 1^{st} position
- Average case element found at mid position of the list

```
#include<stdio.h>
void main()
    int a[100],n,i;
    printf("\n enter the array elements");
    scanf ("%d", &n);
    for(i=0;i<n;i++)
        scanf("%d", &a[i]);
    printf("\n enter the element to search");
    scanf ("%d", &n);
    printf("\n searching");
    for(i=0;i<n;i++)
        if(a[i]==n)
            printf("\n Element found %d at position %d",a[i],i+1);
            exit(0);
```

Sequential Search

• Extra trick in implementing sequential search – append the search element to the last position in the list

55	60	70	32	23	89	32
A[0]	A[1]	A[2]	A[3]	A[4]	A[5]	Search key A[n]

```
ALGORITHM SequentialSearch2(A[0..n], K)

//Implements sequential search with a search key as a sentinel

//Input: An array A of n elements and a search key K

//Output: The index of the first element in A[0..n − 1] whose value is

// equal to K or −1 if no such element is found

A[n] ← K

i ← 0

while A[i] ≠ K do

i ← i + 1

if i < n return i

else return −1
```

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Brute Force Design Technique

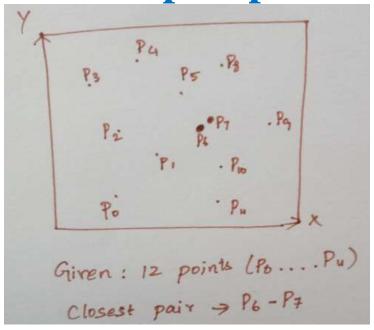
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Closest pair problem

- Geometric problem
- Straight forward approach Finite set of points in the plane
- Applications: computational geometry and operations research
- Google map- nearby restaurants
- Problem statement: find the two closest points in a set of points
- Solution:
- Assumption:
 - 2-dimensional space
 - (x,y) Cartesian coordinates
 - Distance between 2 points $P_i=(x_i,y_i)$, $P_j=(x_i,y_i)$ Euclidean distance

$$d(p_i, p_j) = \sqrt{(x_i - x_j)^2 + (y_i - y_j)^2}.$$

Closest pair problem



ALGORITHM BruteForceClosestPair(P)

```
//Finds distance between two closest points in the plane by brute force //Input: A list P of n (n \ge 2) points p_1(x_1, y_1), \ldots, p_n(x_n, y_n) //Output: The distance between the closest pair of points d \leftarrow \infty for i \leftarrow 1 to n-1 do for j \leftarrow i+1 to n do d \leftarrow \min(d, sqnt((x_i-x_j)^2+(y_i-y_j)^2)) //sqnt is square root return d
```

Analysis of Closest-pair problem

- 1. Problem size: n
- 2. Basic operation: Euclidean Distance
- 3. Count of basic operation-----→
- 4. Efficiency worst case

Cheese pair problem — count of basic operation

$$C(n) = \sum_{i=1}^{n-1} \frac{1}{j-i+1}^{2}$$

Distance
$$= 2 \sum_{i=1}^{n-1} (n-i+1) + 1$$

$$= 2 \left[n \left(\frac{n-1}{i+1} \right) - \left(\frac{n-1}{i+1} \right) \right]$$

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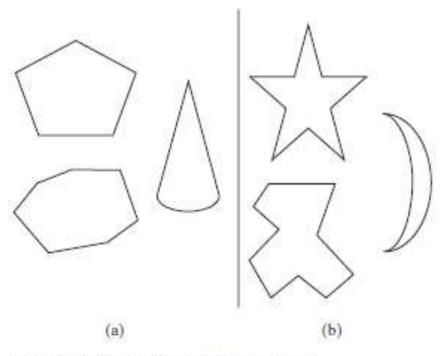
$$= 2 \left[n \left(\frac{n-1}{i+1} \right) - \frac{n(n-1)}{2} \right]$$

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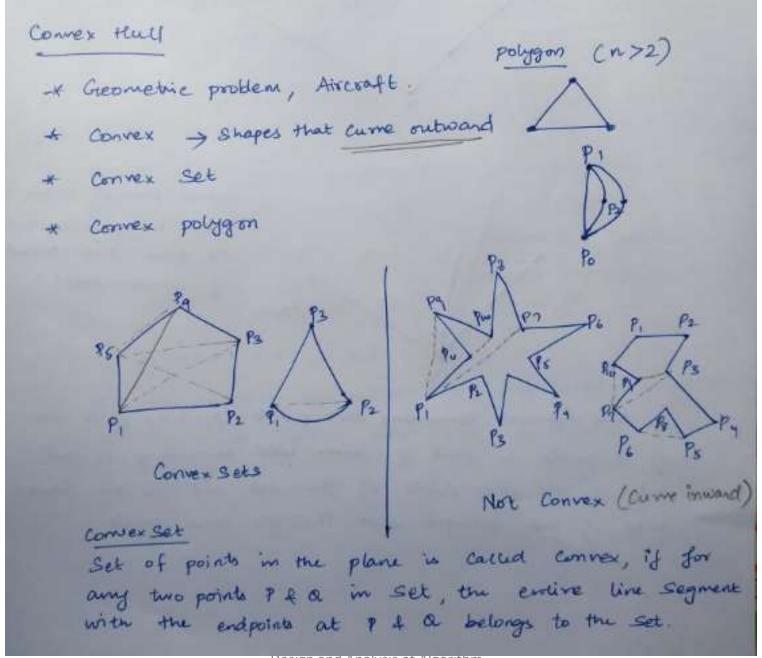
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Design and Analysis of Algorithm

All richula = $n - n = (n-1)n \in O(n^2)$

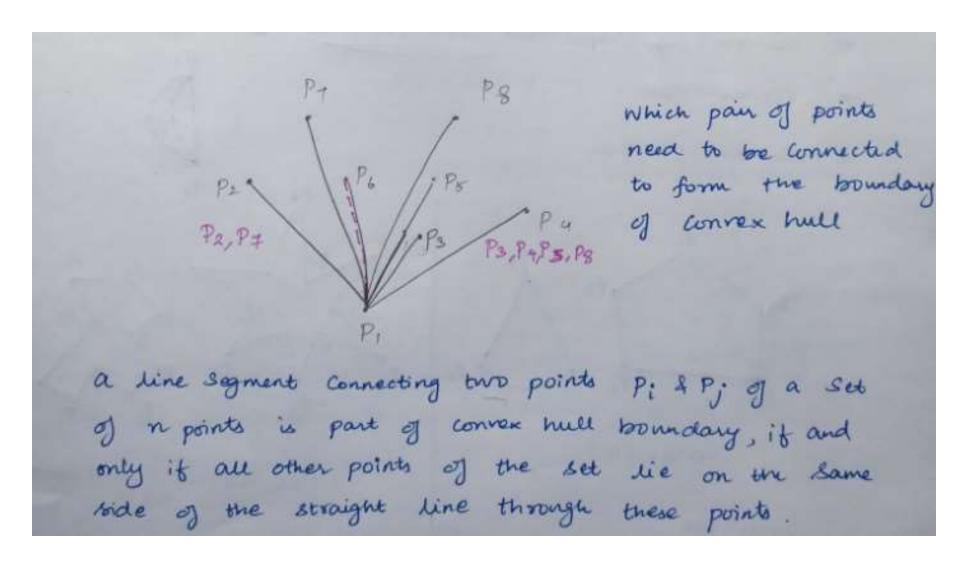
Convex Hull



(a) Convex sets. (b) Sets that are not convex.



Convex hull of Set S of points is the Smallest convex Set Containing 5. * Convex polygon -> Vertices. -> extreme points Should not be a middle point of any line segment



Straigne line - a points (2, y1) (2, y2) ax +by - C Here a = y2 - y, b = 24 - x2 C = 24,42 - 4,22 all points above the line -> ax + by > c]-(P, P2) all points below the line -> ax + by < c]-(P, P2) forms boun Algorithm for each point P_i for each point P_j where $P_j \neq P_i$ line Segment (Pi, Pj.)
(Pa. Pa, Ps, ... PR) for all other points Pk (Pk # PifPj) if each Pk is on one side of line Segment, I Pi, Pj & Convex hull boundary PIPE (boundary of Convex hull)

Convex Hull - Analysis

- Input size n (set of points)
- Basic operation
- Count of basic operation $O(n^3)$
- Worst case