



SNS COLLEGE OF TECHNOLOGY, COIMBATORE –35



P, NP and NP Complete Problems



P Problem

- Solvable in polynomial time
→ solved in time $O(n^2)$
 n → size of input
 K → Constant

Eg:

$$X \leftarrow A$$

$$TC = O(n^2)$$

A → alg - time complexity solve 'x'!

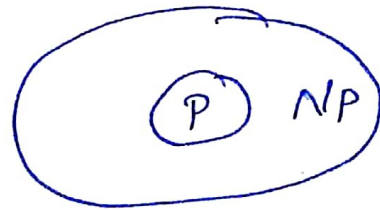
$$X \rightarrow i/p$$



NP Problem

NP - Problems

→ Verifiable in polynomial time



X - Problem
s - solution
A - Algorithm

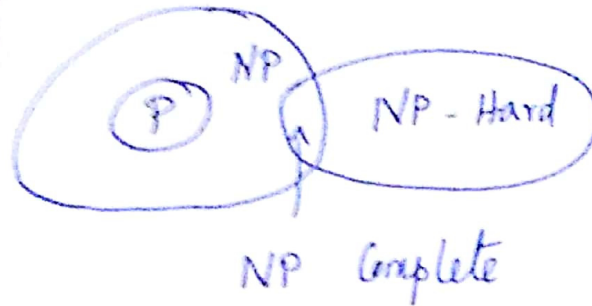
X s
 A

NP - Hard Problem

→ There is no known polynomial time solution



NP Complete Problem



- Not solvable in polynomial time
- solution can be verified/verifiable.

subset sum problem:

'S' is a set of integers. find a subset of 'S' such that sum of elements of that subset is $\in \mathbb{N}$



NP Complete Problem

$$S = \{-1, 2, 7, 10, 6, 2, 1\}$$

$$N = 5$$

$$A = \{-1, 6\}, B = \{2, 6\}$$

- It is solvable in polynomial time, so it comes under NP-Hard
- If solution is given, it could be verified.
- Subset $A = \{-1, 6\}$ it is in 'S' so it is solvable in polynomial time
- $B = \{2, 6\}$, verify with polynomial time