



# SNS COLLEGE OF TECHNOLOGY, COIMBATORE –35



## P, NP and NP Complete Problems



# P Problem

P:

→ Solvable in polynomial time

→ solved in time  $O(n^2)$

$n$  → size of input

$K$  → Constant

Eg:

$X \leftarrow A$

TC =  $O(n^2)$

$A$  → alg - time complexity solve 'x'!

$X$  → i/p

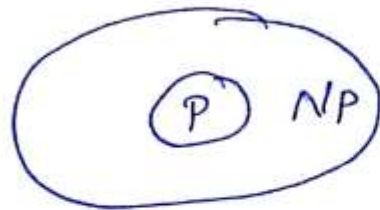


# NP Problem



NP - Problems

→ Verifiable in polynomial time



X - Problem  
s - solution  
A - Algorithm

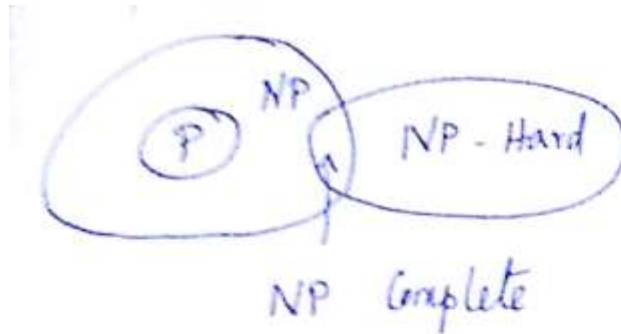
X    s  
      A

NP - Hard Problem

→ There is no known polynomial time solution



# NP Complete Problem



- Not solvable in polynomial time
- solution can be verified/verifiable.

subset sum problem:

'S' is a set of integers. find a subset of 'S' such that sum of elements of that subset is  $\in \mathbb{N}$



# NP Complete Problem

$$S = \{-1, 2, 7, 10, 6, 2, 1\}$$

$$N = 5$$

$$A = \{-1, 6\}, B = \{2, 6\}$$

- It is solvable in polynomial time, so it comes under NP-Hard.
- If solution is given, it could be verified.
- Subset  $A = \{-1, 6\}$  is in 'S' so it is solvable in polynomial time.
- $B = \{2, 6\}$ , verify with polynomial time.