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Projections and Perspectives

- We have to display our 3D model
- Screen is 2D
- Transformation from 3D model coordinates to 2D pixels coordinates.



Projections

- Representation of a 3D scene, for a virtual observer
- One viewpoint:
 - position of the observer
- One direction of view:
 - direction where the observer is looking
- One "up vector":
 - vertical for the observer

Different projections

- Parallel projections:
 - no shortening due to distance
 - several kinds, depending on orientation:
 - isometric, cavalier,...
- Perspective projections:
 - shortening of objects in the distance
 - several kind, depending on orientation:
 - one, two, three vanishing points

Parallel Projection Matrix

- Parallel projection onto z=0 plane:
 x'=x, y'=y, w'=w
- Matrix for this projection:

$$\begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

Perspective Projection Matrix

 Projection onto plane z=0, with center of projection at z=-d:

1	0	0	0
0	1	0	0
0	0	1	0
0	0	1 / <i>d</i>	1

Distance to projection plane



Field of view

- Distance to projection plane not intuitive
- Easier notion: field of view
- FOV= angle, in degrees
- Expresses how wide is my vision



Homogeneous coordinates

- Essential for perspective projection
- Note the shortening of distances uses *w*

$$w' = \frac{z}{d} + w$$
$$\frac{x'}{w'} = \frac{x}{\frac{z}{d} + w}$$

• Impossible to do without homogeneous

Other viewpoints

- If we are viewing from another point?
- Translations:
 - until viewpoint is at origin
- Rotations:
 - until direction of viewing is on *z*-axis
- Back to the previous case

Canonical Coordinates



• After translation, before projection: *canonical 3D coordinates*.

Projections: discussion

- Projections have several goals:
 - exactitude (e.g. plans for architects)
 - realism (view of a scene, VR)
 - visualization
 - artistic view: non-linear perspectives (*e.g.* Rubber Soul)
- An important part of realism in 3D rendering