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UNIT-III COMPLEX DIFFERENTIATION

Construction of Analytic functions

construct con of Analytec function: Malne's Thomson method i) To fend b(x), when use given  $f(x) = \int [\phi_i(x,0) - i\phi_i(x,0)] dx$ where  $\phi_1(x,0) = \left(\frac{\partial u}{\partial x}\right) = axd$  $\phi_{\mathcal{D}}(x,0) = \left(\frac{\partial u}{\partial y}\right)(x,0)$ ii). To find f(x), when V & given f(x)= [f,(x,0)+ide(x,0)]dx where  $\phi_i(x,0) = \left(\frac{\partial V}{\partial y}\right)$  and  $\phi^{(x,0)} = \left(\frac{\partial x}{\partial x}\right)^{x}$ 111). If U-V or U+V & given, then to find Take f(x) = u+iv 1+1x) = 14-4

If find the analytic function 
$$f(z)$$
 whose seal part is  $u = 3x^2y + 2x^2 - y^3 - 2y^2$  solo.

Creen  $u = 3x^2y + 2x^2 - y^3 - 2y^2$ 

$$\frac{\partial y}{\partial x} = 6xy + 4x$$

23MAT102-COMPLEX ANALYSIS AND DIFFERENTIAL EQUATIONS V.SANDHYA/AP/MATHS





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UNIT-III COMPLEX DIFFERENTIATION

$$\frac{\partial u}{\partial x} = 8x^{2} - 3y^{2} - 4y$$

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$$\frac{\partial u}{\partial y} = 9x^{2}$$

$$\frac{\partial u}{\partial y} = 9x^{2} - 10x^{2}$$

$$\frac{\partial u}{\partial x} = \frac{4x^{2}}{3} - 10x^{2} + C$$

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$$\frac{\partial u}{\partial x} = \frac{2x^{2}}{3} - 10x^{2} + C$$

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$$\frac{\partial u}{\partial x} = \frac{2x^{2}}{3} + C$$

$$\frac$$





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UNIT-III COMPLEX DIFFERENTIATION

$$= -xe^{x} \cos y - e^{-x} y e^{y} ny + xe^{-x} \cos y$$

$$= -xe^{x} \cos y + xe^{-x} \cos y + e^{-x} y syny$$

$$= -xe^{x} \cos y + xe^{-x} \cos y + e^{-x} y syny$$

$$= -xe^{x} \cos y - e^{-x} y syny + xe^{-x} \cos y$$

$$= -xe^{x} \cos y - e^{-x} y syny + xe^{-x} \cos y$$
Hence  $y = -xe^{x} \cos y - e^{-x} \cos y$ 

$$= -xe^{x} \cos y - e^{-x} \cos y + e^{-x} \cos y$$

$$= -xe^{x} \sin y + e^{-x} y \cos y + e^{-x} \sin y$$

$$= -xe^{x} \sin y + e^{-x} y \cos y + e^{-x} \sin y$$

$$= -xe^{x} \sin y + e^{-x} y \cos y + e^{-x} \sin y$$

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$$= -xe^{x} \cos y + e^{-x} \cos y + e^{-x} \cos y + e^{-x} \sin y$$

$$= -xe^{x} \cos y + e^{-x} \cos y +$$





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UNIT-III COMPLEX DIFFERENTIATION

By Milne's Thomson method,

$$F(x) = \int [\phi_{1}(x,0) - i \phi_{2}(x,0)] dx$$

$$= \int (e^{x} + i e^{x}) dx$$

$$= (i+i) \int e^{x} dx$$

$$(i+i) f(x) = (i+i) e^{x} + c$$

$$f(x) = e^{x} +$$





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UNIT-III COMPLEX DIFFERENTIATION

By writners Thomson method,

$$f(x) = \int [d_1(x, 0) - i d_2(x, 0)] dx$$

$$= \int [-\cos^2 x - i(0)] dx$$

$$= -\int \cos^2 x dx$$

$$f(x) = \cot x + C$$

All the analytic function  $f(x) = u + iv$ 
where  $u - v = e^x(\cos y - \sin y)$ 
solo.

Let  $f(x) = u + iv + m$ 

$$if(x) = iu - v + m$$

$$(1+ix) f(x) = u + iv + iu - v$$

$$(1+ix) f(x) = u + iv + iu - v$$

$$(1+ix) f(x) = u + iv + iu - v$$

$$(1+ix) f(x) = (u - v) + i(u + v)$$

$$F(x) = U + iv$$

$$U = u - u$$

$$V = u + v$$

$$Caven U = u - v = e^x(u \cos y - \sin y)$$

$$\frac{\partial u}{\partial x} = e^x[u \cos y - \sin y]$$

$$\frac{\partial u}{\partial x} = e^x[1 - o] = e^x$$

$$\frac{\partial u}{\partial x} = e^x[1 - o] = e^x$$

$$\frac{\partial u}{\partial x} = e^x[1 - o] = e^x$$

$$\frac{\partial u}{\partial x} = e^x[1 - o] = e^x$$

$$\frac{\partial u}{\partial x} = e^x[0 + i] = -e^x$$





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But 1 is 
$$\frac{Sh}{2x}$$
  $\frac{2x}{\cos h \, 2y} = \frac{Sh}{2x}$   $\frac{2x}{\cos h \, 2x} = \frac{Sh}{2x}$   $\frac{2x}{\sin h \, 2$ 





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$$= \frac{2\cos 3x - 2(1+\cos 2x)}{1-\cos 3x}$$

$$= \frac{2\cos 3x - 1-\cos 3x}{1-\cos 3x}$$

$$= \frac{-2}{1-\cos 2x} = \frac{-1}{1-\cos 2x}$$

$$= \frac{-2}{1-\cos 2x} = \frac{-1}{2\cos 2x}$$

$$= \frac{-3\cos 2x}{2\cos 2x} = \frac{-1}{2\cos 2x}$$

$$= \frac{-3\cos 2x}{2\cos 2x} = \frac{-1}{2\cos 2x}$$

$$= -2\sin 2x - 1$$

$$= -2\sin 2x - 1$$

$$= \cos 2$$