

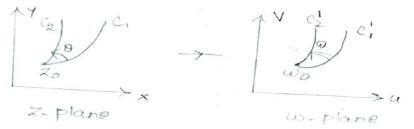
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UNIT-III COMPLEX DIFFERENTIATION

Conformal mapping

Conformal mapping:

A transformation that preserves angles between every pair of curives through a point both 9n magnifule and sense, is said to be conformal at that point.



Isogonal mapping:

A transformation under which angles between every pour of curves through a point are preserved in magnifule, but different in derection.



coppedal point: The point to 95 sand to be confical Point of the transfermation w= f(x) of f(x) is not conformal at to. The cirtical popul is defend by,

$$\frac{dw}{dx} = 0 \text{ and } \frac{dx}{dw} = 0$$





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UNIT-III COMPLEX DIFFERENTIATION

Conformal mapping

Find the coffical point of the transform J. $\omega = x + \frac{1}{x}$ Soln. arven w= x+ 1 $\frac{d\omega}{dx} = 1 - \frac{1}{x^2} = \frac{x^2 - 1}{x^2}$ $\frac{dx}{d\omega} = \frac{x^2}{\sqrt{2}}$ Now $\frac{dw}{dx} = 0 \Rightarrow \frac{x^2}{x^2} = 0$ and $\frac{dx}{dw} = 0 \Rightarrow \frac{x^2}{x^2} = 0 \Rightarrow x^2 = 0$ The offfical points are s. ±1. E]. Find the couffical point of wa = (x-a) (x-B) Soin. (Aver wa = (z-a) (x-b) Differentiate wir to Z, $2w \frac{dw}{dz} = (z-\alpha)(1) + (z-\beta)(1)$ = (z-a) + (z-B) $\frac{d\omega}{dx} = \frac{2x - (\alpha + \beta)}{2\omega}$ and $\frac{dx}{dw} = \frac{2w}{2x - (x+B)}$ Now $\frac{d\omega}{d\tau} = 0 \Rightarrow \frac{2\pi - (\alpha + \beta)}{2\omega} = 0$ 87 = X+B $x = \frac{\alpha + \beta}{3}$



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UNIT-III COMPLEX DIFFERENTIATION

Conformal mapping

and
$$\frac{dx}{dw} = 0 \Rightarrow \frac{8w}{8x}$$
 when $= 0$
 $\frac{dw}{dw} = 0 \Rightarrow \frac{8w}{8x}$ when $= 0$
 $\frac{dw}{dw} = 0$
 \frac{dw}

How I was ree X





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UNIT-III COMPLEX DIFFERENTIATION

Conformal mapping

A point z=a & said to be freed point of a mapping w= f(x) % its image under f(x) is etself. ie., f(x) = x find the invariant points of w= 1+2 Soln. Given $w = \frac{1+\chi}{1-\chi}$ The Privariant points are,

 $z = \frac{1+z}{1-z}$ (: w = f(z) = z) ス(1-ス)=1+ス ス-2 = 1+ Z マースペーリースニロ

2]. Frod the freed points of w= Soln.

Cirver w= 27+6 The flored points are, $z = \frac{2z+6}{z+7}$ X(x+7) = 2x+6 2+72-22-6=0 z2+52-6=0 (z+1)(z+6)=0X=1.-6