



(An Autonomous Institution)
Coimbatore-641035.

#### UNIT-IV FOURIER SERIES AND FOURIER TRANSFORM

PROBLEMS ON  $(0,2\pi)$ 

Foweren Soules

5. Sqn 
$$n\pi = 0$$
 ; Sqn  $(n+1)2\pi = 0$  ; Sqn  $(n+1)\pi = 0$ 

8. 
$$\cos n\pi = (-1)^n$$
.

9. 
$$\cos(n+1)2\pi = 1$$

11. 
$$\cos A \ SPO B = \frac{1}{a} \left[ SPO (A+B) - SPO (A-B) \right]$$

12. 
$$\cos \theta \cos \theta = \frac{1}{2} \left[\cos (\theta + \theta) + \cos (\theta - \theta)\right]$$

13. Sin A Sin B = 
$$\frac{1}{2}$$
 [  $\cos(A - B) - \cos(A + B)$ ]

15. 
$$\int e^{ax} \cos bx dx = \frac{e^{ax}}{a^2 + b^2} \left[a\cos bx + b\sin bx\right]$$

$$\int e^{ax} \operatorname{gen} bx \, dx = \frac{e^{ax}}{a^2 + b^2} \left[ a \operatorname{gen} bx - b \cos bx \right]$$



SIS

(An Autonomous Institution)
Coimbatore-641035.

UNIT-IV FOURIER SERIES AND FOURIER TRANSFORM

PROBLEMS ON  $(0,2\pi)$ 

Perhodic function:

A function fix is said to be provided with Possible (p), 92 for all x, f(x+P) = f(x)where p is a possitive constant, the leastvalue of pro which is called the possed of f(x).

Eg:  $f(x) = S9n \times S9n (x+2\pi) = S9n (x+4\pi) = ...$ So,  $67n \times 15$  a possed of  $2\pi$ 

Disablet' à condition:

Any Sunction for can be developed as founder series  $\frac{\alpha_0}{2} + \frac{\epsilon}{\epsilon} \left[\alpha_n \cos nx + b_n \cos nx\right]$  where  $\alpha_0$ , an and be are constants, provided.

1) for is periodic, single valued and finite.

1) for has a finite no of finite also wet in without and no infinite discontinuity.

Founder sources:

A function f(x) is possedic and satisfies producted a understant term it can be represented by an infinite series is called the fourier series as  $f(x) = \frac{a_0}{2} + \frac{2}{n-1} \left[ a_n \cos nx + b_n \sin nx \right]^n$  where  $a_0$ , an and  $b_n$  are boursen well-cents.





(An Autonomous Institution) Coimbatore-641035.

#### UNIT-IV FOURIER SERIES AND FOURIER TRANSFORM

PROBLEMS ON  $(0,2\pi)$ 

Euler's Formula:

If a function for defined in CXXXC+2TT can be

If a function for defined in  $C \times X \times C + \alpha II$  expanded as the 9nfn9te trignometric seedes.

blow =  $\frac{a_0}{a} + \frac{2}{2} [a_0 \cos nx + b_0 \sin nx]$ where  $a_0 = \frac{1}{2} \int_C b(x) dx$ ;  $a_0 = \frac{1}{2} \int_C b(x) \cos nx dx$   $b_0 = \frac{1}{2} \int_C b(x) \sin nx dx$ 

Pstoblems based on Beginoully's footmula:

I. Fand Sa sina da.

Soln.:  $\int uv \, dx = uv_1 - u'v_2 + u''v_3 - u'''v_4 + \dots$   $\int u' = 1 \quad v_1 = -\cos x$   $\int u' = 1 \quad v_2 = -\sin x$   $\int u' = 0 \quad u' = 1$   $\int u' = 0 \quad u' = -\sin x$   $= \left[ x \left( -\cos x \right) - 1 \left( -\sin x \right) + 0 \right]$   $= \left[ x \left( -\cos x \right) - 1 \left( -\sin x \right) - 0 \right]$   $= \left[ -x \cos x + \sin x \right]$   $= \left[ -x \cos x + \sin x \right]$   $= \left[ -x \cos x + \sin x \right]$   $= \left[ -x \cos x + \sin x \right]$   $= \left[ -x \cos x + \sin x \right]$   $= \left[ -x \cos x + \sin x \right]$   $= \left[ -x \cos x + \sin x \right]$   $= \left[ -x \cos x + \sin x \right]$   $= \left[ -x \cos x + \sin x \right]$   $= \left[ -x \cos x + \sin x \right]$   $= \left[ -x \cos x + \sin x \right]$   $= \left[ -x \cos x + \sin x \right]$   $= \left[ -x \cos x + \sin x \right]$   $= \left[ -x \cos x + \sin x \right]$   $= \left[ -x \cos x + \sin x \right]$   $= \left[ -x \cos x + \sin x \right]$   $= \left[ -x \cos x + \sin x \right]$   $= \left[ -x \cos x + \cos x \right]$  =

2]. Evaluate ∫ (x+x2) cosnx dx

Soln :





(An Autonomous Institution) Coimbatore-641035.

### UNIT-IV FOURIER SERIES AND FOURIER TRANSFORM

PROBLEMS ON  $(0,2\pi)$ 

$$\int uv \, dx = uv_1 - u'v_2 + u''v_3 - u'''v_4 + \dots$$

$$\int \pi (\pi + \pi^2) \cos n\pi \, dx$$

$$= \int (\pi + \pi^2) \frac{\sin n\pi}{n} - (1 + 2\pi) \left( -\frac{\cos n\pi}{n^2} \right) + 2 \left( -\frac{\sin n\pi}{n^3} \right) - 0 \right]$$

$$= \left[ (\pi + \pi^2) \frac{87nn\pi}{n} + (1 + 2\pi) \frac{\cos n\pi}{n^2} - 2 \frac{88nn\pi}{n^3} \right]$$

$$= \left[ (0 + (1 + 2\pi) \frac{\cos n\pi}{n^2} - 0) - (0 + (1 - 2\pi) \frac{\cos + n\pi}{n^2} - 0) \right]$$

$$= (1 + 2\pi) \frac{(-1)^n}{n^2} - (1 - 2\pi) \frac{(-1)^n}{n^2} \cos n\pi = (-1)^n$$

$$= (1 + 2\pi) + 2\pi \frac{(-1)^n}{n^2}$$

$$= 4\pi \frac{(-1)^n}{n^2}$$

$$= 4\pi \frac{(-1)^n}{n^2}$$

$$= 4\pi \frac{(-1)^n}{n^2}$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

$$= 0$$

Psioblems on 10,27)

Frommula:
$$\int_{(x)} \int_{0}^{2\pi} \frac{\alpha_0}{2\pi} + \int_{n=1}^{2\pi} \left[ \alpha_n \cos nx + b_n \sin nx \right]$$

$$\alpha_0 = \frac{1}{\pi} \int_{0}^{2\pi} \delta(x) dx$$

$$\alpha_n = \frac{1}{\pi} \int_{0}^{2\pi} \delta(x) \cos nx dx$$

$$b_n = \frac{1}{\pi} \int_{0}^{2\pi} \delta(x) \sin nx dx$$

J. Determine the Fowler serves for  $f(x) = x^2$  $\int_{(\mathcal{H})} = \frac{\alpha_0}{2} + \sum_{n=1}^{\infty} \left[ a_n \cos n\pi + b_n \frac{\partial n}{\partial n} n\pi \right]$ 





(An Autonomous Institution) Coimbatore-641035.

### UNIT-IV FOURIER SERIES AND FOURIER TRANSFORM

$$-\Omega_0 = \frac{1}{\pi} \int_0^{2\pi} \frac{1}{3} \ln dx$$

$$= \frac{1}{\pi} \int_0^{2\pi} x^2 dx$$

$$= \frac{1}{\pi} \int_0^{2\pi$$





(An Autonomous Institution)
Coimbatore-641035.

UNIT-IV FOURIER SERIES AND FOURIER TRANSFORM

$$= \frac{1}{\Pi} \left[ \chi^2 \left( -\frac{(05 \, \text{n} \chi)}{\text{n}} \right) - 2\chi \left( -\frac{35 \, \text{n} \, \text{n} \chi}{\text{n}^2} \right) + 2 \left( \frac{\cos n \chi}{\text{n}^3} \right) - 0 \right]^{2\pi} \right]^2$$

$$= \frac{1}{\Pi} \left[ -\chi^2 \left( \frac{(05 \, \text{n} \chi)}{\text{n}} + 2\chi + \frac{59 \, \text{n} \, \text{n} \chi}{\text{n}^2} \right) + 2 \left( \frac{\cos n \chi}{\text{n}^3} \right)^{2\pi} \right]$$

$$= \frac{1}{\Pi} \left[ -\frac{4\pi^2}{\text{n}} + 0 + \frac{2}{\text{n}^3} \right) - \left( 0 + 0 + \frac{2}{\text{n}^3} \right) \right]$$

$$= \frac{1}{\Pi} \left[ -\frac{4\pi^2}{\text{n}} + \frac{2}{\text{n}^3} - \frac{2}{\text{n}^3} \right]$$

$$= \frac{1}{\Pi} \left[ -\frac{4\pi^2}{\text{n}} + \frac{2}{\text{n}^3} - \frac{2}{\text{n}^3} \right]$$

$$= \frac{1}{\Pi} \left[ -\frac{4\pi^2}{\text{n}} + \frac{2}{\text{n}^3} - \frac{2}{\text{n}^3} \right]$$

$$= \frac{4}{3} \pi^2 + \frac{2}{12} \left[ -\frac{4\pi^2}{\text{n}^3} + \frac{2}{\text{n}^3} - \frac{2}{\text{n}^3} \right]$$

$$= \frac{4}{3} \pi^2 + \frac{2}{12} \left[ -\frac{4\pi^2}{\text{n}^3} + \frac{2}{\text{n}^3} - \frac{2}{\text{n}^3} \right]$$

$$= \frac{4}{3} \pi^2 + \frac{2}{12} \left[ -\frac{4\pi^2}{\text{n}^3} + \frac{2}{\text{n}^3} - \frac{2}{\text{n}^3} \right]$$

$$= \frac{4}{3} \pi^2 + \frac{2}{12} \left[ -\frac{4\pi^2}{\text{n}^3} + \frac{2}{\text{n}^3} - \frac{2}{\text{n}^3} \right]$$

$$= \frac{4}{3} \pi^2 + \frac{2}{12} \left[ -\frac{2}{12} \pi^2 + \frac{2}{12} + \frac{2}{12} \pi^3 \right]$$

$$= \frac{4}{3} \pi^3 + \frac{2}{12} \left[ -\frac{2}{12} \pi^3 + \frac{2}{12} \pi^3 \right]$$

$$= \frac{4}{3} \pi^3 + \frac{2}{12} \left[ -\frac{2}{12} \pi^3 \right]$$

$$= \frac{1}{4\pi} \left[ \frac{(\pi - 2)^3}{-3} \right]^{2\pi} = -\frac{1}{12\pi} \left[ -\frac{3}{12} \pi^3 \right]$$

$$= \frac{1}{4\pi} \left[ \frac{(\pi - 2)^3}{-3} \right]^{2\pi} = -\frac{1}{12\pi} \left[ -\frac{3}{12} \pi^3 \right]$$

$$= \frac{1}{12\pi} \left[ -2\pi^3 \right]$$

$$= \frac{\pi^2}{6}$$



(An Autonomous Institution)
Coimbatore-641035.



#### UNIT-IV FOURIER SERIES AND FOURIER TRANSFORM

$$a_{n} = \frac{1}{\pi \int_{0}^{2\pi} \frac{1}{(\pi - x)^{2}} \cos nx \, dx}$$

$$= \frac{1}{\pi \int_{0}^{2\pi} \frac{1}{(\pi - x)^{2}} \cos nx \, dx}$$

$$= \frac{1}{4\pi \int_{0}^{2\pi} \frac{1}{(\pi - x)^{2}} \cos nx \, dx}$$

$$= \frac{1}{4\pi \int_{0}^{2\pi} \frac{1}{(\pi - x)^{2}} \cos nx \, dx}$$

$$u = (\pi - x)^{2} \quad \forall cos nx$$

$$u' = -2(-1) = 2$$

$$u'' = -2(\pi - x)$$

$$u'' = -2(-1) = 2$$

$$u''' = -2(-1) = 2$$

$$v' = \frac{\sin nx}{n^{2}}$$

$$= \frac{1}{4\pi \int_{0}^{2\pi} \frac{\sin nx}{n^{2}} - 2(\pi - x) \left(\frac{\cos nx}{n^{2}}\right) - 2\frac{\sin nx}{n^{2}} - 2\frac{\sin nx}{n^{2}}$$

$$= \frac{1}{4\pi \int_{0}^{2\pi} \frac{2\pi}{n^{2}} + \frac{2\pi}{n^{2}}$$

$$= \frac{1}{4\pi \int_{0}^{2\pi} \frac{2\pi}{n^{2}} + \frac{2\pi}{n^{2}} + \frac{2\pi}{n^{2}} + \frac{2\pi}{n^{2}}$$

$$= \frac{1}{4\pi \int_{0}^{2\pi} \frac{2\pi}{n^{2}} + \frac{2\pi}{$$





(An Autonomous Institution Coimbatore-641035.

#### UNIT-IV FOURIER SERIES AND FOURIER TRANSFORM

$$= \frac{1}{4\pi} \left[ (\pi - \varkappa)^{2} \left( \frac{-\cos n\varkappa}{n} \right) - \left( -2 \left( \pi - \varkappa \right) \right) \left( -\frac{\sin n\varkappa}{n^{2}} \right) \right.$$

$$= \frac{1}{4\pi} \left[ -\left( \pi - \varkappa\right)^{2} \frac{(\cos n\varkappa}{n} - 2 \left( \pi - \varkappa\right) \frac{8inn\varkappa}{n^{2}} + 2 \frac{\cos n\varkappa}{n^{3}} \right]^{2\pi}$$

$$= \frac{1}{4\pi} \left[ \left( -\frac{\pi^{2}}{n} + 2\pi io \right) + \frac{2}{n^{3}} \right) - \left( -\frac{\pi^{2}}{n} - o + \frac{2}{n^{3}} \right) \right]$$

$$= \frac{1}{4\pi} \left[ -\frac{\pi^{2}}{n} + \frac{2}{n^{3}} + \frac{\pi^{2}}{n^{3}} - \frac{2}{n^{3}} \right]$$

$$b_{n} = 0$$

$$\therefore (n) \Rightarrow \sqrt{3}(n) = \frac{\pi^{2}/6}{2} + \sum_{n=1}^{\infty} \left[ \frac{1}{n^{2}} \cos nx + 0 \right]$$

$$= \frac{\pi^{2}}{12} + \sum_{n=1}^{\infty} \frac{1}{n^{2}} \cos nx$$

3]. IPRM the folicies seeses for 
$$f(\pi) = \begin{cases} x & 0 < x < \pi \\ 3\pi - x & \pi < x < \pi \end{cases}$$

$$30 \ln \frac{\pi}{2} = \frac{\alpha_0}{2} + \sum_{n=1}^{\infty} \left[ \alpha_n \cos nx + b_n \sin nx \right] \rightarrow 0)$$

$$\alpha_0 = \frac{1}{\pi} \int_0^{2\pi} f(x) dx$$

$$= \frac{1}{\pi} \left[ \int_0^{\pi} x dx + \int_0^{\pi} (2\pi - x) dx \right]$$

$$= \frac{1}{\pi} \left[ \left( \frac{x^2}{2} \right)^{\pi} + \left( 2\pi x - \frac{x^2}{2} \right)^{2\pi} \right]$$

$$= \frac{1}{\pi} \left[ \frac{1}{2} (\pi^2 - 0) + \left( 4\pi^2 - \frac{4\pi^2}{2} \right) - \left( 2\pi^2 - \frac{\pi^2}{2} \right) \right]$$

$$= \frac{1}{\pi} \left[ \frac{\pi^2}{2} + (2\pi^2 - 2\pi^2 + \frac{\pi^2}{2}) \right] = \frac{1}{\pi} \left[ \frac{2\pi^2}{2} \right]$$

$$\alpha_0 = \pi$$





(An Autonomous Institution Coimbatore-641035.

#### UNIT-IV FOURIER SERIES AND FOURIER TRANSFORM

$$\begin{array}{l}
a_{n} = \frac{1}{11} \int_{0}^{\infty} f(x) & (66 \text{ nx}) \, dx \\
= \frac{1}{11} \int_{0}^{\infty} x & (66 \text{ nx}) \, dx + \int_{0}^{\infty} (2\pi - x) & (66 \text{ nx}) \, dx
\end{array}$$

$$\begin{array}{l}
a_{1} = \frac{1}{11} \int_{0}^{\infty} x & (66 \text{ nx}) \, dx + \int_{0}^{\infty} (2\pi - x) & (66 \text{ nx}) \, dx
\end{array}$$

$$\begin{array}{l}
a_{1} = \frac{1}{11} \int_{0}^{\infty} x & (66 \text{ nx}) \, dx + \int_{0}^{\infty} (2\pi - x) & (66 \text{ nx}) \, dx
\end{array}$$

$$\begin{array}{l}
a_{1} = \frac{1}{11} \int_{0}^{\infty} x & (66 \text{ nx}) \, dx
\end{array}$$

$$\begin{array}{l}
a_{1} = \frac{1}{11} \int_{0}^{\infty} x & (66 \text{ nx}) \, dx
\end{array}$$

$$\begin{array}{l}
a_{1} = \frac{1}{11} \int_{0}^{\infty} x & (66 \text{ nx}) \, dx
\end{array}$$

$$\begin{array}{l}
a_{1} = \frac{1}{11} \int_{0}^{\infty} x & (66 \text{ nx}) \, dx
\end{array}$$

$$\begin{array}{l}
a_{1} = \frac{1}{11} \int_{0}^{\infty} x & (66 \text{ nx}) \, dx
\end{array}$$

$$\begin{array}{l}
a_{1} = \frac{1}{11} \int_{0}^{\infty} x & (66 \text{ nx}) \, dx
\end{array}$$

$$\begin{array}{l}
a_{1} = \frac{1}{11} \int_{0}^{\infty} x & (66 \text{ nx}) \, dx
\end{array}$$

$$\begin{array}{l}
a_{1} = \frac{1}{11} \int_{0}^{\infty} x & (66 \text{ nx}) \, dx
\end{array}$$

$$\begin{array}{l}
a_{1} = \frac{1}{11} \int_{0}^{\infty} x & (66 \text{ nx}) \, dx
\end{array}$$

$$\begin{array}{l}
a_{1} = \frac{1}{11} \int_{0}^{\infty} x & (66 \text{ nx}) \, dx
\end{array}$$

$$\begin{array}{l}
a_{1} = \frac{1}{11} \int_{0}^{\infty} x & (66 \text{ nx}) \, dx
\end{array}$$

$$\begin{array}{l}
a_{1} = \frac{1}{11} \int_{0}^{\infty} x & (66 \text{ nx}) \, dx
\end{array}$$

$$\begin{array}{l}
a_{1} = \frac{1}{11} \int_{0}^{\infty} x & (66 \text{ nx}) \, dx
\end{array}$$

$$\begin{array}{l}
a_{1} = \frac{1}{11} \int_{0}^{\infty} x & (66 \text{ nx}) \, dx
\end{array}$$

$$\begin{array}{l}
a_{1} = \frac{1}{11} \int_{0}^{\infty} x & (66 \text{ nx}) \, dx
\end{array}$$

$$\begin{array}{l}
a_{1} = \frac{1}{11} \int_{0}^{\infty} x & (66 \text{ nx}) \, dx
\end{array}$$

$$\begin{array}{l}
a_{1} = \frac{1}{11} \int_{0}^{\infty} x & (66 \text{ nx}) \, dx
\end{array}$$

$$\begin{array}{l}
a_{1} = \frac{1}{11} \int_{0}^{\infty} x & (66 \text{ nx}) \, dx
\end{array}$$

$$\begin{array}{l}
a_{1} = \frac{1}{11} \int_{0}^{\infty} x & (66 \text{ nx}) \, dx
\end{array}$$

$$\begin{array}{l}
a_{1} = \frac{1}{11} \int_{0}^{\infty} x & (66 \text{ nx}) \, dx
\end{array}$$

$$\begin{array}{l}
a_{1} = \frac{1}{11} \int_{0}^{\infty} x & (66 \text{ nx}) \, dx
\end{array}$$

$$\begin{array}{l}
a_{1} = \frac{1}{11} \int_{0}^{\infty} x & (66 \text{ nx}) \, dx
\end{array}$$

$$\begin{array}{l}
a_{1} = \frac{1}{11} \int_{0}^{\infty} x & (66 \text{ nx}) \, dx
\end{array}$$

$$\begin{array}{l}
a_{1} = \frac{1}{11} \int_{0}^{\infty} x & (66 \text{ nx}) \, dx
\end{array}$$

$$\begin{array}{l}
a_{1} = \frac{1}{11} \int_{0}^{\infty} x & (66 \text{ nx}) \, dx$$

$$\begin{array}{l}
a_{1} = \frac{1}{11} \int_{0}^{\infty} x & (66 \text{ nx}) \, dx
\end{array}$$

$$\begin{array}{l}
a_{1} = \frac{1}{11} \int_{0}^{\infty} x & (66 \text{ nx}) \, dx$$

$$\begin{array}{l}
a_{1} = \frac{1}{11} \int_{0}^{\infty} x & (66 \text{ nx}) \, dx
\end{array}$$

$$\begin{array}{l}
a_{1} = \frac{1}{11} \int_{0}^{\infty} x & (66 \text{ nx}) \, d$$





(An Autonomous Institution) Coimbatore-641035.

UNIT-IV FOURIER SERIES AND FOURIER TRANSFORM

$$\int_{0}^{1}(x) = \frac{\pi}{2} + \frac{2}{n-1} \frac{2}{\pi n^{2}} \left[ (-1)^{n} - 1 \right] \left( \cos nx + 0 \right) \\
= \frac{\pi}{2} + \frac{2}{\pi} \frac{2}{n-1} \left[ (-1)^{n} - 1 \right] \left( \cos nx \right) \\
= \frac{\pi}{2} + \frac{2}{\pi} \frac{2}{n-1} \left[ (-1)^{n} - 1 \right] \left( \cos nx \right) \\
= \frac{\pi}{2} + \frac{2}{\pi} \frac{2}{n-1} \left[ (-1)^{n} - 1 \right] \left( \cos nx \right) \\
= \frac{\pi}{2} + \frac{2}{\pi} \frac{2}{n-1} \left[ (-1)^{n} - 1 \right] \left( \cos nx \right) \\
= \frac{\pi}{2} + \frac{2}{\pi} \frac{2}{n-1} \left[ (-1)^{n} - 1 \right] \left( \cos nx \right) \\
= \frac{\pi}{2} + \frac{2}{\pi} \frac{2}{n-1} \left[ (-1)^{n} - 1 \right] \left( \cos nx \right) \\
= \frac{\pi}{2} + \frac{2}{\pi} \frac{2}{n-1} \left[ (-1)^{n} - 1 \right] \left( \cos nx \right) \\
= \frac{\pi}{2} + \frac{2}{\pi} \frac{2}{n-1} \left[ (-1)^{n} - 1 \right] \left( \cos nx \right) \\
= \frac{\pi}{2} + \frac{2}{\pi} \frac{2}{n-1} \left[ (-1)^{n} - 1 \right] \left( \cos nx \right) \\
= \frac{\pi}{2} + \frac{2}{\pi} \frac{2}{n-1} \left[ (-1)^{n} + 1 \right] \left( \cos nx \right) \\
= \frac{\pi}{2} + \frac{2}{\pi} \frac{2}{n-1} \left[ (-1)^{n} + 1 \right] \left( \cos nx \right) \\
= \frac{\pi}{2} + \frac{2}{\pi} \frac{2}{n-1} \left[ (-1)^{n} + 1 \right] \left( \cos nx \right) \\
= \frac{\pi}{2} + \frac{2}{\pi} \frac{2}{n-1} \left[ (-1)^{n} + 1 \right] \left( \cos nx \right) \\
= \frac{\pi}{2} + \frac{2}{\pi} \frac{2}{n-1} \left[ (-1)^{n} + 1 \right] \left( \cos nx \right) \\
= \frac{\pi}{2} + \frac{2}{\pi} \frac{2}{n-1} \left[ (-1)^{n} + 1 \right] \left( \cos nx \right) \\
= \frac{\pi}{2} + \frac{2}{\pi} \frac{2}{n-1} \left[ (-1)^{n} + 1 \right] \left( \cos nx \right) \\
= \frac{\pi}{2} + \frac{2}{\pi} \frac{2}{n-1} \left[ (-1)^{n} + 1 \right] \left( \cos nx \right) \\
= \frac{\pi}{2} + \frac{\pi}{2} \frac{2}{n-1} \left[ (-1)^{n} + 1 \right] \left( \cos nx \right) \\
= \frac{\pi}{2} + \frac{\pi}{2} \frac{2}{n-1} \left[ (-1)^{n} + 1 \right] \left( \cos nx \right) \\
= \frac{\pi}{2} + \frac{\pi}{2} \frac{2}{n-1} \left[ (-1)^{n} + 1 \right] \left( \cos nx \right) \\
= \frac{\pi}{2} + \frac{\pi}{2} \frac{2}{n-1} \left[ (-1)^{n} + 1 \right] \left( \cos nx \right) \\
= \frac{\pi}{2} + \frac{\pi}{2} \frac{2}{n-1} \left[ (-1)^{n} + 1 \right] \left( \cos nx \right) \\
= \frac{\pi}{2} + \frac{\pi}{2} \frac{2}{n-1} \left[ (-1)^{n} + 1 \right] \left( \cos nx \right) \\
= \frac{\pi}{2} + \frac{\pi}{2} \frac{2}{n-1} \left( \cos nx \right) \\
= \frac{\pi}{2} + \frac{\pi}{2} \frac{\pi}{2} \left[ (-1)^{n} + 1 \right] \left( \cos nx \right) \\
= \frac{\pi}{2} + \frac{\pi}{2} \frac{\pi}{2} \left[ (-1)^{n} + 1 \right] \left( \cos nx \right) \\
= \frac{\pi}{2} + \frac{\pi}{2} \frac{\pi}{2} \left[ (-1)^{n} + 1 \right] \left( \cos nx \right) \\
= \frac{\pi}{2} + \frac{\pi}{2} \frac{\pi}{2} \left[ (-1)^{n} + 1 \right] \left( \cos nx \right) \\
= \frac{\pi}{2} + \frac{\pi}{2} \frac{\pi}{2} \left[ (-1)^{n} + 1 \right] \left( \cos nx \right) \\
= \frac{\pi}{2} + \frac{\pi}{2} \frac{\pi}{2} \left[ (-1)^{n} + 1 \right] \left( \cos nx \right) \\
= \frac{\pi}{2} + \frac{\pi}{2} \frac{\pi}{2} \left[ (-1)^{n} + 1 \right] \left( \cos nx \right) \\
= \frac{\pi}{2} + \frac{\pi}{2} \frac{\pi}{2} \left[ (-1)^{n} + 1 \right] \left( \cos nx \right) \\
= \frac{\pi}{2}$$





(An Autonomous Institution)
Coimbatore-641035.

UNIT-IV FOURIER SERIES AND FOURIER TRANSFORM

$$= \frac{1}{2\pi l} \left( \frac{(3)\left(\frac{\cos(n+1)2l}{n+1}\right)}{n+1} - \frac{(-\sin(n+1)2l)}{(n+0)^2} \right)^{2\pi l} - \frac{(3)\left(\frac{\cos(n+1)2l}{n+1}\right)}{(n+0)^2} - \frac{(3)\left(\frac{\cos(n+1)2l}{n+1}\right)}{(n+0)^2} \right)^{2\pi l}$$

$$= \frac{1}{2\pi l} \left[ \frac{(3)\left(\frac{\cos(n+1)2l}{n+1}\right)}{n+1} + \frac{(3)\left(\frac{\cos(n+1)2l}{n+1}\right)}{(n+0)^2} + \frac{(3)\left(\frac{\cos(n+1)2l}{n+1}\right)}{(n+0)^2} \right]$$

$$= \frac{1}{2\pi l} \left[ \frac{-2\pi l}{n+1} + \frac{2\pi l}{n+1} \right]$$

$$= \frac{1}{2\pi l} \left[ \frac{-2\pi l}{n+1} + \frac{2\pi l}{n+1} \right]$$

$$= \frac{1}{2\pi l} \left[ \frac{-2\pi l}{n+1} + \frac{2\pi l}{n+1} \right]$$

$$= \frac{1}{2\pi l} \left[ \frac{-2\pi l}{n+1} + \frac{2\pi l}{n+1} \right]$$

$$= \frac{1}{2\pi l} \left[ \frac{-2\pi l}{n+1} + \frac{2\pi l}{n+1} \right]$$

$$= \frac{1}{2\pi l} \left[ \frac{-2\pi l}{n+1} + \frac{2\pi l}{n+1} \right]$$

$$= \frac{1}{2\pi l} \left[ \frac{-2\pi l}{n+1} + \frac{2\pi l}{n+1} \right]$$

$$= \frac{1}{2\pi l} \left[ \frac{-2\pi l}{n+1} + \frac{2\pi l}{n+1} \right]$$

$$= \frac{1}{2\pi l} \left[ \frac{-2\pi l}{n+1} + \frac{2\pi l}{n+1} \right]$$

$$= \frac{1}{2\pi l} \left[ \frac{-2\pi l}{n+1} + \frac{2\pi l}{n+1} \right]$$

$$= \frac{1}{2\pi l} \left[ \frac{-2\pi l}{n+1} + \frac{2\pi l}{n+1} \right]$$

$$= \frac{1}{2\pi l} \left[ \frac{-2\pi l}{n+1} + \frac{2\pi l}{n+1} \right]$$

$$= \frac{1}{2\pi l} \left[ \frac{-2\pi l}{n+1} + \frac{2\pi l}{n+1} + \frac{2\pi l}{n+1} \right]$$

$$= \frac{1}{2\pi l} \left[ \frac{-2\pi l}{n+1} + \frac{2\pi l}{n+1} + \frac{2\pi l}{n+1} \right]$$

$$= \frac{1}{2\pi l} \left[ \frac{-2\pi l}{n+1} + \frac{2\pi l}{n+1} + \frac{2\pi l}{n+1} + \frac{2\pi l}{n+1} \right]$$

$$= \frac{1}{2\pi l} \left[ \frac{-2\pi l}{n+1} + \frac{2\pi l}{n+1} + \frac{2\pi l}{n+1} + \frac{2\pi l}{n+1} \right]$$

$$= \frac{1}{2\pi l} \left[ \frac{-2\pi l}{n+1} + \frac{2\pi l}{n+1} + \frac{2\pi l}{n+1} + \frac{2\pi l}{n+1} + \frac{2\pi l}{n+1} \right]$$

$$= \frac{1}{2\pi l} \left[ \frac{-2\pi l}{n+1} + \frac{2\pi l}{n+1} + \frac{2$$





(An Autonomous Institution) Coimbatore-641035.

#### UNIT-IV FOURIER SERIES AND FOURIER TRANSFORM





(An Autonomous Institution)
Coimbatore-641035.

### UNIT-IV FOURIER SERIES AND FOURIER TRANSFORM

$$8[\pi] = \frac{-2}{2} + a_1 \cos x + \frac{8}{5} a_n \cos n\pi + b_1 \sin x + \frac{8}{5} b_n \sin nx + \frac{8}{5} b_n$$





(An Autonomous Institution) Coimbatore-641035.

UNIT-IV FOURIER SERIES AND FOURIER TRANSFORM

PROBLEMS ON  $(0,2\pi)$ 

Method of Vourgation of Parameters The second order 19 near differential egn. 95 The Section  $\frac{d^2y}{dx^2} + P \frac{dy}{dx} + Q = X$  where X is a  $\frac{d^2y}{dx^2} + P \frac{dy}{dx} + Q = X$  where X is a  $\frac{d^2y}{dx^2} + P \frac{dy}{dx} + Q = X$ 

OF  $C_1$  for  $C_1$ ,  $C_2$  are functions of x.

PI = Pf, + f f2

where  $P = -\int \frac{f_2 \times}{f_1 f_2' - f_1' f_2} dx$   $Q = \int \frac{f_2 \times f_1' f_2' - f_1' f_2}{f_1 f_2' - f_1' f_2} dx$   $Q = \int \frac{f_2 \times f_1' f_2' - f_1' f_2}{f_1 f_2' - f_1' f_2} dx$ 

J. Solve  $\frac{d^2y}{dx^2} + 4y = 4 \tan 2x$  using method of Voration of paramoters. Soln.

Gaven  $(3^2+4)y=4\tan 2x$  where  $x=4\tan 2x$ AE m2+4=0 m3=-4 の=± ái

CF = A; Cos 2x + C 890 2x PI = Pfi+9fo

Here  $f_1 = \cos ax$   $f_2 = \sin ax$   $f_3 = a \cos ax$ = cos ax [a cos ax] - S9n ax (- a s9n ax) = 2 cas 2x + 2 Sin 2 2x = a [cos2 ax + S9n2 ax]

Scanne = val(1) = 2 CamScanner





(An Autonomous Institution) Coimbatore-641035.

UNIT-IV FOURIER SERIES AND FOURIER TRANSFORM

$$P = -\int \frac{f_3 x}{w} dx$$

$$= -\int \frac{s_1^2 x}{s_2^2} dx + \tan \frac{s_2^2 x}{s_2^2} dx$$

$$= -\partial \int \frac{s_1^2 x}{s_2^2} dx + \sin \frac{s_2^2 x}{s_2^2} dx$$

$$= -\partial \int \frac{s_1^2 x}{s_2^2} dx + \sin \frac{s_2^2 x}{s_2^2} dx - \int \cos \frac{s_2^2 x}{s_2^2} dx$$

$$= -\partial \int \int \frac{s_1^2 x}{s_2^2} dx + \cos \frac{s_2^2 x}{s_2^2} dx - \int \cos \frac{s_2^2 x}{s_2^2} dx$$

$$= -\partial \int \int \frac{s_1^2 x}{s_2^2} dx + \cos \frac{s_2^2 x}{s_2^2} dx$$

$$= -\partial \int \int \frac{s_1^2 x}{s_2^2} dx + \cos \frac{s_2^2 x}{s_2^2} dx$$

$$= -\partial \int \int \frac{s_1^2 x}{s_2^2} dx + \cos \frac{s_2^2 x}{s_2^2} dx$$

$$= -\partial \int \int \frac{s_1^2 x}{s_2^2} dx + \cos \frac{s_2^2 x}{s_2^2} dx$$

$$= -\partial \int \int \frac{s_1^2 x}{s_2^2} dx + \cos \frac{s_2^2 x}{s_2^2} dx$$

$$= -\partial \int \int \frac{s_1^2 x}{s_2^2} dx + \cos \frac{s_2^2 x}{s_2^2} dx$$

$$= -\partial \int \int \frac{s_1^2 x}{s_2^2} dx + \cos \frac{s_2^2 x}{s_2^2} dx$$

$$= -\partial \int \int \frac{s_1^2 x}{s_2^2} dx + \cos \frac{s_2^2 x}{s_2^2} dx$$

$$= -\partial \int \int \frac{s_1^2 x}{s_2^2} dx + \cos \frac{s_2^2 x}{s_2^2} dx$$

$$= -\partial \int \int \frac{s_1^2 x}{s_2^2} dx + \cos \frac{s_2^2 x}{s_2^2} dx$$

$$= -\partial \int \int \frac{s_1^2 x}{s_2^2} dx + \cos \frac{s_2^2 x}{s_2^2} dx$$

$$= -\partial \int \int \frac{s_1^2 x}{s_2^2} dx + \cos \frac{s_2^2 x}{s_2^2} dx$$

$$= -\partial \int \int \frac{s_1^2 x}{s_2^2} dx + \cos \frac{s_2^2 x}{s_2^2} dx$$

$$= -\partial \int \int \frac{s_1^2 x}{s_2^2} dx + \cos \frac{s_2^2 x}{s_2^2} dx$$

$$= -\partial \int \int \frac{s_1^2 x}{s_2^2} dx + \cos \frac{s_2^2 x}{s_2^2} dx$$

$$= -\partial \int \int \frac{s_1^2 x}{s_2^2} dx + \cos \frac{s_2^2 x}{s_2^2} dx$$

$$= -\partial \int \int \frac{s_1^2 x}{s_2^2} dx + \cos \frac{s_2^2 x}{s_2^2} dx$$

$$= -\partial \int \int \frac{s_1^2 x}{s_2^2} dx + \cos \frac{s_2^2 x}{s_2^2} dx$$

$$= -\partial \int \int \frac{s_1^2 x}{s_2^2} dx + \cos \frac{s_2^2 x}{s_2^2} dx$$

$$= -\partial \int \int \frac{s_1^2 x}{s_2^2} dx + \cos \frac{s_2^2 x}{s_2^2} dx$$

$$= -\partial \int \int \frac{s_1^2 x}{s_2^2} dx + \cos \frac{s_2^2 x}{s_2^2} dx$$

$$= -\partial \int \int \frac{s_1^2 x}{s_2^2} dx + \cos \frac{s_2^2 x}{s_2^2} dx$$

$$= -\partial \int \int \frac{s_1^2 x}{s_2^2} dx + \cos \frac{s_2^2 x}{s_2^2} dx$$

$$= -\partial \int \int \frac{s_1^2 x}{s_2^2} dx + \cos \frac{s_2^2 x}{s_2^2} dx$$

$$= -\partial \int \int \frac{s_1^2 x}{s_2^2} dx + \cos \frac{s_2^2 x}{s_2^2} dx$$

$$= -\partial \int \int \frac{s_1^2 x}{s_2^2} dx + \cos \frac{s_2^2 x}{s_2^2} dx$$

$$= -\partial \int \int \frac{s_1^2 x}{s_2^2} dx + \cos \frac{s_2^2 x}{s_2^2} dx$$

$$= -\partial \int \int \frac{s_1^2 x}{s_2^2} dx + \cos \frac{s_2^2 x}{s_2^2} dx$$

$$= -\partial \int \int \frac{s_1^2 x}{s_2^2} dx + \cos \frac{s_1^2 x}{s_2^2} dx$$

$$= -\partial \int \int \frac{s_1^2 x}{s_2^2} dx + \cos \frac{s_1^2 x}{s_2^2} dx$$

$$= -\partial \int \int \frac{s_1^2 x}{s_2^2} dx + \cos \frac{$$