



(An Autonomous Institution) Coimbatore-641035.

UNIT-IV FOURIER SERIES AND FOURIER TRANSFORM FOURIER SERIES-ODD AND EVEN FUNCTIONS  $(-\pi,\pi)$ 

Problems on (-11, 11) and (-1,1)

rodd function:

If f(x) is said to be odd, then f(-x) = -f(x). If f(x) is an all the then f(x) = -f(x) = -f(x).

Now  $g(-\pi) = -\pi = -g(\pi) \Rightarrow g(\pi)$  is odd.

Egs: 263, 890 26, tan3 26

DEVON function:

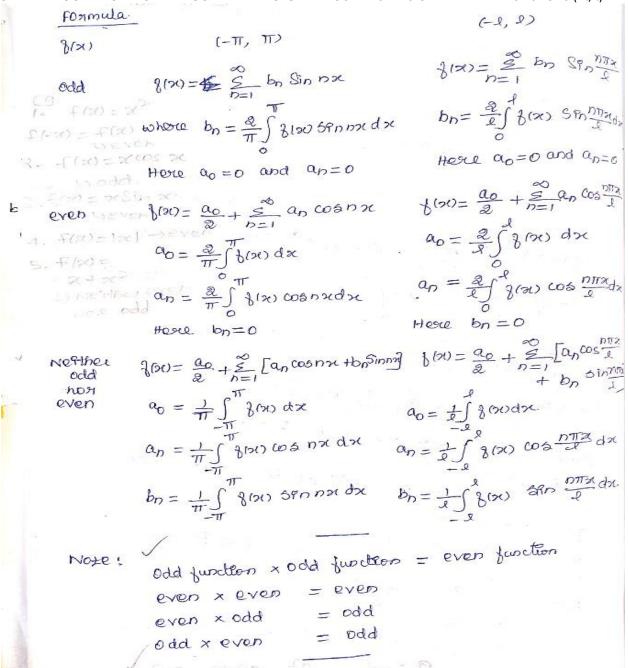
If  $3(\pi)$  is said to be even then  $3(-\pi) = 3(\pi)$ .

If  $f(\pi)$  is an even for the series of the series of  $3(\pi) = 3(\pi) = 2\pi$ , cos  $\pi$ ,  $39n^2 \times 101$ ,  $15in \times 1$ ,  $15in \times 1$ ,  $15in \times 1$ ,





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J. Find the fourier services for 
$$g(x) = 1 \times 1 \times (-\pi, \pi)$$

Solow:

 $g(x) = |x|$ 

Now  $g(-x) = 1 - x| = |x| = g(x)$ 
 $\Rightarrow g(x)$  & an even function. Hence  $b_0 = 0$ 
 $\therefore g(x) = \frac{a_0}{2} + \frac{a_0}{2} = a_0$  (as  $b \times x$ )

 $a_0 = \frac{a_0}{2} + \frac{a_0}{2} = a_0$  (be  $b \times x$ )

 $a_0 = \frac{a_0}{2} + \frac{a_0}{2} = a_0$ 
 $a_0 = \pi$ 
 $a_0$ 





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$$\frac{1}{2} \int_{0}^{2} dx = \frac{\pi}{2} + \frac{2}{n} \int_{0}^{2} \frac{1}{n^{2}} \left[ \frac{1}{n^{2}} - \frac{1}{n^{2}} \right] = \frac{\pi}{2} - \frac{4}{n^{2}} = \frac{2}{n^{2}} \int_{0}^{2} \frac{1}{n^{2}} \cos nx$$

2]. Find the foweier services for 
$$f(x) = f(\cos x)$$
, (iii)

Solo:

$$f(x) = |\cos x| = [-\cos x, \sqrt{x} + x + x]$$

Now 
$$f(-x) = |\cos (-x)| = |\cos x| = g(x)$$

$$\Rightarrow g(x) \text{ is even. } \Rightarrow b_0 = 0$$

$$\frac{1}{n} \int_{0}^{\pi} \frac{1}{2} dx = \frac{2}{n} \int_{0}^{\pi} \frac{1}{2} dx$$

$$= \frac{2}{\pi} \int_{0}^{\pi} \frac{1}{2} (2x) dx$$

$$= \frac{2}{\pi} \int_{0}^{\pi} \frac{1}{2} (2x) dx + \int_{0}^{\pi} - (29n x)^{\pi} \int_{0}^{\pi} \frac{1}{2} (29n x)^{\pi} dx$$

$$= \frac{2}{\pi} \int_{0}^{\pi} (39n x)^{\pi} - (39n x)^{\pi} \int_{0}^{\pi} \frac{1}{2} (39n x)^{\pi} dx$$

$$= \frac{2}{\pi} \left[ (89n \times)^{1/2} - (89n \times)^{1/2} \right]$$

$$= \frac{2}{\pi} \left[ (1-0) - (0-1) \right]$$

$$a_0 = \frac{4}{\pi} \pi$$

$$a_1 = \frac{3}{\pi} \int_{0}^{\pi} f(x) \cos nx \, dx$$

$$\frac{2}{\pi} \int_{0}^{\pi} f(x) \cos nx \, dx$$

$$= \frac{2}{\pi} \int_{0}^{\pi} \cos x \cos nx \, dx - \int_{0}^{\pi} \cos x \cos nx \, dx$$

$$= \frac{2}{\pi} \int_{0}^{\pi} \cos nx \cos nx \, dx - \int_{0}^{\pi} \cos nx \cos x \, dx$$

$$= \frac{2}{\pi} \int_{0}^{\pi} \cos nx \cos nx \, dx - \int_{0}^{\pi} \cos nx \cos x \, dx$$

$$= \frac{2}{2\pi} \int_{0}^{\pi} (\cos (nx + x) + \cos (nx - x)) \, dx - \int_{0}^{\pi} (\cos (nx + x) + \cos (nx - x)) \, dx$$

$$= \int_{0}^{\pi} (\cos (nx + x) + \cos (nx - x)) \, dx$$

$$\int_{2\pi}^{\pi} \left( \cos (nx+x) + \cos (nx-x) \right) dx$$

$$\int_{2\pi}^{\pi} \left( \cos (nx+x) + \cos (nx-x) \right) dx$$





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$$= \frac{1}{\pi} \left[ \frac{T_{0}}{[\cos(n+1)x]} + \frac{1}{\cos(n-1)x} \right] dx$$

$$- \int_{T_{0}}^{T_{0}} [\cos(n+1)x] + \frac{1}{\cos(n-1)x} dx$$

$$= \frac{1}{\pi} \left[ \frac{39n(n+1)x}{n+1} + \frac{3n(n-1)x}{n-1} \right] dx$$

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$$= \frac{39n(n+1)x}{n-1} + \frac{39n(n+1)x}{n-1} + \frac{39n(n+1)x}{n-1} + \frac{39n(n+1)x}{n-1} + \frac{39n(n+1)x}{n-1}$$

$$= \frac{39n(n+1)x}{n-1} + \frac{39n(n+1)x}{n-1} +$$





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If the first post 
$$f(x) = x^2$$
 (-T, T). Decluce the  $f(x) = x^2$  (-T, T). Decluce the  $f(x) = x^2$  is  $f(x) = x^2$  is  $f(x) = x^2$  and  $f(x) = x^2$  is  $f(x) = x^2$  and  $f(x) = x^2$  and  $f(x) = x^2$  for  $f(x) =$ 





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$$\pi^{2} = \frac{\pi^{2}}{3} + 4 \sum_{n=1}^{\infty} \frac{(-1)^{n}}{n^{2}} (-1)^{n}$$

$$\pi^{2} - \frac{\pi^{2}}{3} = 4 \sum_{n=1}^{\infty} \frac{(-1)^{2}}{n^{2}}$$

$$\frac{2\pi^{2}}{3(4)} = \sum_{n=1}^{\infty} \frac{1}{n^{2}}$$

$$\frac{2\pi^{2}}{3(4)} = \sum_{n=1}^{\infty} \frac{1}{n^{2}}$$

$$\frac{1}{12} + \frac{1}{2^{2}} + \dots = \frac{\pi^{2}}{16}$$

$$\vdots \quad 0 = \frac{\pi^{2}}{3} + 4 \sum_{n=1}^{\infty} \frac{(-1)^{n}}{n^{2}}$$

$$\frac{1}{12} + \frac{1}{2^{2}} = \frac{\pi^{2}}{3} + 4 \sum_{n=1}^{\infty} \frac{(-1)^{n}}{n^{2}}$$

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$$\frac{1}{12} + \frac{1}{2^{2}} = \frac{\pi^{2}}{3^{2}} + \dots = \frac{\pi^{2}}{12}$$

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$$q_0 = 0$$

$$q_0 = \frac{3}{\pi} \int_{0}^{\pi} f(x) \cos nx \, dx$$

$$= \frac{3}{\pi} \int_{0}^{\pi} \left(1 - \frac{3x}{\pi}\right) \cos nx \, dx$$

$$u' = -\frac{3x}{\pi} \int_{0}^{\pi} V - (\cos nx) \, dx$$

$$u' = -\frac{3x}{\pi} \int_{0}^{\pi} V - (\cos nx) \, dx$$

$$= \frac{3}{\pi} \left[ \left( -\frac{3x}{\pi} \right) \frac{2^{n} n n x}{n} - \frac{3}{\pi} \left( \frac{\cos nx}{n^{2}} \right) \right]_{0}^{\pi}$$

$$= \frac{3}{\pi} \left[ -\frac{3}{\pi} \left( -\frac{1}{n^{2}} \right) + \frac{3}{\pi^{2} \pi} \right] = \frac{3}{\pi} \left( \frac{3}{n^{2} \pi} \right) \left[ 1 - (-\frac{1}{n^{2}}) \right]$$

$$= \frac{4}{n^{2} \pi^{2}} \left[ 1 - (-\frac{1}{n^{2}}) \right]$$

$$a_{1} = \frac{3}{n^{2} \pi^{2}} \cdot \frac{9}{n^{2}} \cdot \frac{1}{n^{2}} \cos nx - \frac{3}{n^{2}} \cdot \frac{3}{n^{2}} \cos nx$$

$$f(x) = \frac{3}{n^{2} \pi^{2}} \cdot \frac{9}{n^{2}} \cdot \frac{1}{n^{2}} \cos nx - \frac{3}{n^{2}} \cdot \frac{3}{n^{2}} \cos nx$$

$$f(x) = \frac{3}{n^{2}} \cdot \frac{1}{n^{2}} \cos nx - \frac{3}{n^{2}} \cdot \frac{3}{n^{2}} \cos nx$$

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$$f(x) = \frac{3}{n^{2}} \cdot \frac{1}{n^{2}} \cos nx - \frac{3}{n^{2}} \cos nx - \frac{3}{$$