



DEPARTMENT OF MATHEMATICS

$$\begin{aligned} f(x_0, y_0) &= x_0 + y_0 \\ &= 0 + 1 \\ &= 1 \end{aligned}$$

2) Find $y(0.1)$ by Modified Euler

$$y' = y - \frac{2x}{y}, \quad y(0) = 1$$

Given:

$$f(x, y) = y - \frac{2x}{y}$$

$$x_0 = 0, \quad y_0 = 1$$

$$h = x_1 - x_0$$

$$= 0.1$$

$$x_1 = 0.1, \quad y_1 = ?$$

By Modified Euler Method.

$n=0$

$$y_1 = y_0 + hf \left[x_0 + \frac{h}{2}, y_0 + \frac{h}{2}, f(x_0, y_0) \right]$$

$$= 1 + 0.1 f \left[0.05, 1 + 0.05 f(0, 1) \right]$$

$$= 1 + 0.1 f \left[0.05, 1 + 0.05 \left[1 - \frac{2 \times 0}{1} \right] \right]$$

$$= 1 + 0.1 \left[1.05 - \frac{2 \times 0.05}{1.05} \right]$$

$$= 1 + 0.1 [1.05 - 0.095]$$

$$= 1 + 0.095$$

$$= 1.095$$

$$\boxed{y_1 = 1.095}$$