

SNS COLLEGE OF TECHNOLOGY



(An Autonomous Institution)
Coimbatore – 35

DEPARTMENT OF MATHEMATICS

UNIT -V LAPLACE TRANSFORM

CONVOLUTION :

Defn.

If f(t) and g(t) are two functions defined

for $t \ge 0$ then the convolution of f(t) & g(t) is

defined as $f(t) * g(t) = (f * g)(t) = \int_{0}^{t} f(u) g(t-u) du$

NOTE: \$ (t) * 9 (t) = 9 (t) * 7 (t)

CONVOLUTION THEOREM :

If \$1t) & g(t) are two laplace transformable functions defined for t >0 then



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Occurrence Convolution theorem find
$$1 + \left[\frac{3}{(S^2+\alpha^2)^2}\right]$$

$$= 2 + \left[\frac{3}{(S^2+\alpha^2)^2}\right] = 2 + \left[\frac{3}{(S^2+\alpha^2)^2}\right]$$

$$= 2 + \left[\frac{3}{(S^2+\alpha^2)^2}\right] + \left[\frac{3}{(S^2+\alpha^2)^2}\right]$$

$$= 2 + \left[\frac{3}{(S^2+\alpha^2)^2}\right]$$

$$= 2 + \left[\frac{3}{(S^2+\alpha^2)^2}\right]$$

$$= 2 + \left[\frac{3}{(S^2+\alpha^2)^2}\right$$



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Ind the inverse LT by convolution thm.
$$\frac{1}{s^{2}(3+5)}$$

$$1^{-1} \left[\frac{1}{s^{2}(s+5)} \right] = 1^{-1} \left[\frac{1}{s^{2}} \right] \cdot 1^{-1} \left[\frac{1}{s+5} \right]$$

$$= 1^{-1} \left[\frac{1}{s^{2}(s+5)} \right] = 1^{-1} \left[\frac{1}{s^{2}} \right] \cdot 1^{-1} \left[\frac{1}{s+5} \right]$$

$$= 1^{-1} \left[\frac{1}{s^{2}(s+5)} \right] = 1^{-1} \left[\frac{1}{s^{2}} \right] \cdot 1^{-1} \left[\frac{1}{s+5} \right]$$

$$= 1^{-1} \left[\frac{1}{s^{2}(s+5)} \right] = 1^{-1} \left[\frac{1}{s^{2}(s+5)} \right] =$$

3) using convolution theorem find

(i)
$$\frac{1}{(s^2+a^2)^2}$$
 soln: $\frac{1}{2a^2} \int \frac{\sin at}{a} - t \cos at \int \frac{1}{a} \int \frac{1}{a}$