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UNIT-IV FOURIER SERIES AND FOURIER TRANSFORM

FOURIER TRANSFORM

Fowlier Transform Day:

The foundier transform of 2(20 % gvi. by

$$F(s) = \frac{1}{\sqrt{\alpha \pi}} \int_{-\infty}^{\infty} J(x) e^{i\theta x} dx \rightarrow (1)$$

Then the function fix 9s the Inverse

Foweller transform of F(5) is given by

$$\delta(x) = \frac{1}{\sqrt{2\pi}} \int_{-\infty}^{\infty} F(s) e^{-isx} ds \rightarrow (2)$$

The above egns. (1) and (2) are forntly called Foroiser transform Pair.

Self Respeccal function:

If the focular transform of f(x) 98 equal to F(S), then be said to be reapposal frunction under focuser transform.

Passeval's Identity on Rayleigh's Theorem:

If FC) 98 the fourier transform of & (b)

then
$$\int_{-\infty}^{\infty} |g(x)|^2 dx = \int_{-\infty}^{\infty} |F(s)|^2 ds$$

Results:
$$e^{ix} + e^{ix}$$

i). $\cos x = \frac{e^{ix} + e^{-ix}}{2}$

ii). $\sin x = \frac{e^{ix} - e^{-ix}}{2}$





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Problems:

J. Find the FT of
$$\frac{1}{1}$$
 (or) = $\frac{1}{1}$ (or) = $\frac{1}{1}$





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$$= \sqrt{2\pi} \left[0 + 2\pi i \int_{0}^{\pi} x \, S^{2} n \, C \, x \, dx \right]$$

$$= \sqrt{2\pi} \left[2\pi i \left[2\pi \left(-\frac{\cos S x}{S} \right) - 1 \left(-\frac{G^{2} n \, S x}{S^{2}} \right) + 0 \right] \right]$$

$$= \sqrt{2\pi} \left[2\pi i \left[2\pi \left(-\frac{\cos S x}{S} \right) - 1 \left(-\frac{G^{2} n \, S x}{S^{2}} \right) + 0 \right] \right]$$

$$= \sqrt{2\pi} \left[2\pi i \left[2\pi \left(-\frac{\cos S x}{S} \right) - \frac{G^{2} n \, S x}{S^{2}} \right) - 0 \right]$$

$$= \sqrt{2\pi} \left[2\pi i \left[2\pi \left(-\frac{\cos S x}{S} \right) - \frac{G^{2} n \, S x}{S^{2}} \right) - 0 \right]$$

$$= \sqrt{2\pi} \left[2\pi i \left[2\pi \left(-\frac{\cos S x}{S} \right) - \frac{G^{2} n \, S x}{S^{2}} \right) - 0 \right]$$

$$= \sqrt{2\pi} \left[2\pi i \left[2\pi \left(-\frac{\cos S x}{S} \right) - \frac{G^{2} n \, S x}{S^{2}} \right) - 0 \right]$$

$$= \sqrt{2\pi} \left[2\pi i \left[2\pi \left(-\frac{\cos S x}{S} \right) - \frac{G^{2} n \, S x}{S^{2}} \right) - 0 \right]$$

$$= \sqrt{2\pi} \left[2\pi i \left[2\pi i \left[2\pi \left(-\frac{\cos S x}{S} \right) - \frac{G^{2} n \, S x}{S^{2}} \right] \right]$$

3). Show that becodes transform of
$$\begin{cases}
f(\pi) = \begin{cases} a^2 - x^2, & |\pi|/4 \\
0, & |\pi|/4 \\
0, & |\pi|/4 \end{cases}
\end{cases}$$
and hence find that
$$\begin{cases}
\sqrt{\frac{2}{\pi}} \left[\frac{89naS - aS \cos aS}{2^3} \right]. \text{ Hence deduce that} \\
\sqrt{\frac{2}{\pi}} \left[\frac{99nt - t \cot t}{t^3} \right] dt = \frac{7}{4}. \text{ Using P.I. Show that} \\
0 \left(\frac{99nt - t \cot t}{t^3} \right) dt = \frac{7}{15}.$$

$$\begin{cases}
|S(x)| = \begin{cases}
\alpha^2 - x^2, & -\alpha < x < \alpha \\
0, & -\infty < x < -\alpha & \alpha < x < \infty
\end{cases}$$

$$\begin{cases}
F(s) = \begin{cases}
1 & \alpha^2 - x^2, \\
0, & -\infty < x < -\alpha & \alpha < x < \infty
\end{cases}$$

$$\begin{cases}
F(s) = \frac{1}{\sqrt{2\pi}} \int_{-\alpha}^{\alpha} (\alpha^2 - x^2) \left(\cos Sx + \frac{2\pi}{2} \cos x \right) dx
\end{cases}$$

$$F(s) = \sqrt{\frac{1}{2\pi \pi}} \int_{-a}^{a} (a^{2} - x^{2}) \left[\cos 3x + i \sin 2x \right] dx$$

$$= \sqrt{\frac{1}{2\pi \pi}} \left[\int_{-a}^{a} (a^{2} - x^{2}) \cos 3x \, dx + i \int_{-a}^{a} (a^{2} - x^{2}) \sin 3x \, dx \right]$$

$$= \sqrt{\frac{1}{2\pi \pi}} \left[\int_{-a}^{a} (a^{2} - x^{2}) \cos 3x \, dx + i \int_{-a}^{a} (a^{2} - x^{2}) \sin 3x \, dx \right]$$

$$= \sqrt{\frac{1}{2\pi \pi}} \left[\int_{-a}^{a} (a^{2} - x^{2}) \cos 3x \, dx + i \int_{-a}^{a} (a^{2} - x^{2}) \sin 3x \, dx \right]$$

$$= \sqrt{\frac{1}{2\pi \pi}} \left[\int_{-a}^{a} (a^{2} - x^{2}) \cos 3x \, dx + i \int_{-a}^{a} (a^{2} - x^{2}) \sin 3x \, dx \right]$$



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$$= \frac{1}{\sqrt{2\pi}} e \int_{0}^{\infty} (a^{2} - x^{2}) \cos s \, dx + i(0)$$

$$= \sqrt{2\pi} \left[(a^{2} - x^{2}) \frac{3^{2}n \, 2x}{c} - (-2x) \left(\frac{\cos s \, x}{c^{2}} \right) + (-2) \left(\frac{s^{2}n \, x}{c^{2}} \right) \right]$$

$$= \sqrt{2\pi} \left[(a^{2} - x^{2}) \frac{3^{2}n \, 2x}{c} - (-2x) \left(\frac{\cos s \, x}{c^{2}} \right) + (-2) \left(\frac{s^{2}n \, x}{c^{2}} \right) \right]$$

$$= \sqrt{2\pi} \left[-2x \frac{\cos s \, x}{c^{2}} + \frac{2}{c^{2}} \frac{\sin s \, x}{c} \right]$$

$$= \sqrt{2\pi} \left[-2x \frac{\cos s \, x}{c^{2}} + \frac{2}{c^{2}} \frac{\sin s \, x}{c} \right]$$

$$= \sqrt{2\pi} \left[\frac{3^{2}n \, s \, x}{c^{2}} - \frac{3}{c^{2}} \cos s \, x \right]$$

$$= \sqrt{2\pi} \left[\frac{3^{2}n \, s \, x}{c^{2}} - \frac{3}{c^{2}} \cos s \, x \right]$$

$$= \sqrt{2\pi} \left[\frac{3^{2}n \, s \, x}{c^{2}} - \frac{3}{c^{2}} \cos s \, x \right]$$

$$= \sqrt{2\pi} \int_{0}^{\infty} e \left[\frac{5^{2}n \, s \, - s \, \cos s}{c^{2}} \right] \cos s \, x \, ds$$

$$= \sqrt{2\pi} \left[\frac{3^{2}n \, s \, x}{c^{2}} - \frac{3}{c^{2}} \cos s \, x \right] \cos s \, x$$

$$= \sqrt{2\pi} \left[\frac{3^{2}n \, s \, x}{c^{2}} - \frac{3}{c^{2}} \cos s \, x \right] \cos s \, x$$

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$$= \sqrt{2\pi} \left[\frac{3^{2}n \, s \, x}{c^{2}} - \frac{3^{2}n \, s \, x}{c^{2}} - \frac{3^{2}n \, s \, x}{c^{2}} \right] \cos s \, x$$

$$= \sqrt{2\pi} \left[\frac{3^{2}n \, s \, x}{c^{2}} - \frac{3^{2}n \, s \, x}{c^{2}} \right] \cos s \, x$$

$$= \sqrt{2\pi} \left[\frac{3^{2}n \, s \, x}{c^{2}} - \frac{3^{2}n \, s \, x}{c^{2}} \right] \cos s \, x$$

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ii). Using Paiceval's Identity,

$$\int_{0}^{\infty} |3(x)|^{2} dx = \int_{0}^{\infty} |F(s)|^{2} ds$$

$$\int_{0}^{\infty} |3(x)|^{2} dx = \int_{0}^{\infty} |F(s)|^{2} ds$$

$$\int_{0}^{\infty} (1-x^{2})^{2} dx = \int_{0}^{\infty} |3\pi s - 3\cos \frac{s}{2}|^{2} ds$$

$$\int_{0}^{\infty} (1+x^{2})^{-2}x^{2} dx = \int_{0}^{\infty} |3\pi s - 3\cos \frac{s}{2}|^{2} ds$$

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$$\int_{0}^{\infty} (3\pi s - 3\cos \frac{s}{2})^{2} ds = \int_{0}^{\infty} |3\pi s - 3\cos \frac{s}{2}|^{2} ds$$

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$$g(x) = \begin{cases} a - |x|, & -a < x < a \\ 0, & -\infty < x < -a \end{cases} & a < x < 0 \end{cases}$$

$$F(S) = \begin{cases} 1 - x \end{cases} & a < x < -a \end{cases} & a < x < 0$$

$$F(S) = \frac{1}{\sqrt{2\pi}} \int_{0}^{a} (a - |x|) \left[\cos x + \sin x \right] dx$$

$$= \frac{2}{\sqrt{2\pi}} \int_{0}^{a} (a - x) \cos x dx + 0$$

$$= \sqrt{2\pi} \left[(a - x) \frac{\sin x}{\sin x} - (-1) \left(-\frac{\cos x}{\sin x} \right) \right] dx$$

$$= \sqrt{2\pi} \left[-\frac{\cos x}{\sin x} \right] - (-1) \left(-\frac{\cos x}{\sin x} \right) dx$$

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$$= \sqrt{2\pi} \left[-\frac{$$





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Put
$$x=0$$
, $a=2$

$$\delta(0) = \frac{1}{H} \int_{0}^{\infty} \frac{g_{1}n^{2}}{g^{2}} ds$$

$$\int_{0}^{\infty} \frac{(g_{1}n)^{2}}{g^{2}} ds = \frac{\pi}{4} \delta(0) = \frac{\pi}{4} (3-101)$$

$$\int_{0}^{\infty} \frac{(g_{1}n)^{2}}{g^{2}} ds = \frac{\pi}{4} \delta(0) = \frac{\pi}{4} (3-101)$$

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$$\int_{0}^{\infty} \frac{(g_{1}n)^{2}}{g^{2}} ds = \frac{\pi}{4} \delta(0)$$

$$\int_{0}^{\infty} \frac{(g_{1}n)^{2}}{g^{2}}$$





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3) Find the fourier fearcherm of
$$f(x) = \begin{cases} 1-|x|, |x|/x \\ 0, |x|/x \end{cases}$$
 and deduce that
$$\int_{0}^{\infty} \left(\frac{Sn}{t} \right)^{2} dt \text{ and } \int_{0}^{\infty} \left(\frac{Sn}{t} \right)^{4} dt$$

$$f(x) = \begin{cases} 1-|x|, -1 < x < 1 \\ 0, -\infty < x < -1 \end{cases} \text{ and } 1 < x < \infty$$

$$F(8) = \frac{1}{\sqrt{2\pi}} \int_{0}^{\infty} f(x) e^{-\frac{1}{2}x} dx$$

$$= \frac{1}{\sqrt{2\pi}} \int_{0}^{\infty} (1-|x|) \left(\cos Sx + \frac{1}{2} \cos Sx \right) dx$$

$$= \frac{1}{\sqrt{2\pi}} \int_{0}^{\infty} (1-|x|) \left(\cos Sx + \frac{1}{2} \cos Sx \right) dx$$

$$= \frac{1}{\sqrt{2\pi}} \int_{0}^{\infty} (1-|x|) \left(\cos Sx + \frac{1}{2} \cos Sx \right) dx$$

$$= \frac{1}{\sqrt{2\pi}} \left[\int_{0}^{\infty} (1-x) \cos Sx dx + o \right]$$

$$= \int_{0}^{\infty} \left[\int_{0}^{\infty} (1-x) \cos Sx dx + o \right]$$

$$= \int_{0}^{\infty} \left[\int_{0}^{\infty} \cos Sx - \int_{0}^{\infty} \cos Sx - \int_{0}^{\infty} \cos Sx \right] ds$$

$$= \int_{0}^{\infty} \int_{0}^{\infty} \left[\int_{0}^{\infty} \cos Sx - \int_{0}^{\infty} \cos Sx \right] ds$$

$$= \int_{0}^{\infty} \int_{0}^{\infty} \left[\int_{0}^{\infty} \cos Sx - \int_{0}^{\infty} \cos Sx \right] ds$$

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$$= \int_{0}^{\infty} \int_{0}^{\infty} \left[\int_{0}^{\infty} \cos Sx - \int_{0}^{\infty} \cos Sx - \int_{0}^{\infty} \cos Sx \right] ds$$





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$$=\frac{1}{\pi}\int_{-\infty}^{\infty}\frac{1-\cos s}{s^{2}}\cos s \times ds$$

$$=\frac{1-\cos s}{s^{2}}\cos s \times ds$$

$$=\frac{1-$$





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Using priceval's Identity
$$\int_{-\infty}^{\infty} 18 (x)^{2} dx = \int_{-\infty}^{\infty} 1 F(x)^{2} dx$$

$$\int_{-\infty}^{\infty} (1-1x)^{2} dx = \frac{2}{\pi} \int_{-\infty}^{\infty} \left(\frac{1-\cos c}{2^{2}}\right)^{2} dx$$

$$= \frac{2}{\pi} \int_{-\infty}^{\infty} \frac{(1-\cos c)}{2^{2}} dx$$

$$= \frac{2}{\pi} \int_{-\infty}^{\infty} \frac{3\pi f^{2} \sqrt{2}}{2^{2}} dx$$

$$= \frac{3\pi f^{2} \sqrt{2}}$$





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Publishers on FT:

AJ. Find the Focuser teansform of
$$f(x)$$
 of

AJ. Find the Focuser teansform of $f(x)$ of

 $f(x) = \int_{-\infty}^{\infty} \frac{g(x)}{x} dx = \frac{g(x)}{x}$
 $f(x) = \int_{-\infty}^{\infty} \frac{g(x)}{x} dx = \frac{g(x)}{x}$

Soln:

we already find $f(x) = \int_{-\infty}^{\infty} \frac{g(x)}{x} dx = \frac{g(x)}{x}$
 $f(x) = \int_{-\infty}^{\infty} \frac{g(x)}{x} dx = \frac{g(x)}{x}$





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$$= \frac{1}{\sqrt{2\pi}} \int_{-\infty}^{\infty} \frac{\sqrt{3\pi as}}{\sqrt{\pi}} \frac{\sqrt{3\pi as}}{\sqrt{2}} e \cos sx - 9c9ns x) ds$$

$$= \frac{1}{\pi} \int_{-\infty}^{\infty} \frac{\sqrt{3\pi as}}{\sqrt{s}} \cos sx ds - i \int_{-\infty}^{\infty} \frac{\sqrt{3\pi as}}{\sqrt{s}} \frac{\sqrt{3\pi as}}{\sqrt{s}} \frac{\sqrt{3\pi as}}{\sqrt{s}} \frac{\sqrt{3\pi as}}{\sqrt{s}} \frac{\sqrt{3\pi as}}{\sqrt{s}} \frac{\sqrt{3\pi as}}{\sqrt{s}} \cos sx ds = \frac{\pi}{2} \sqrt{3\pi as}$$

$$= \frac{\pi}{2} \int_{-\infty}^{\infty} \frac{\sqrt{3\pi as}}{\sqrt{s}} \cos sx ds - i (0)$$

$$= \frac{\pi}{2} \int_{-\infty}^{\infty} \frac{\sqrt{3\pi as}}{\sqrt{s}} ds = \frac{\pi}{2} \sqrt{3\pi as} \int_{-\infty}^{\infty} \frac{\sqrt{3\pi as}}{\sqrt{s}} ds$$

$$= \frac{\pi}{2} \int_{-\infty}^{\infty} \sqrt{3\pi as} ds = \frac{\pi}{2} \int_{-\infty}^{\infty} \sqrt{3\pi as} ds$$

$$= \frac{\pi}{2} \int_{-\infty}^{\infty} \sqrt{3\pi as} ds$$





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$$aa \frac{\pi}{2} = a \int \frac{(sqn as)^{2}}{2} de$$

$$\int_{0}^{\infty} \frac{(sqn as)^{2}}{2} ds = \frac{\pi}{2} a$$

$$\int_{0}^{\infty} \frac{(sqn s)^{2}}{2} ds = \frac{\pi}{2} a$$

$$\int_{0}^{\infty} \frac{(sqn t)^{2}}{2} dt = \frac{\pi}{2} a$$

$$\int_{0}^{\infty} \frac{(sqn t)^{2}}{2} dt = \frac{\pi}{2}$$



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Transforms of simple functions:

J. Find the foreign transform of

$$|x| = \begin{cases} 1-x^2, |x| < 1 \end{cases}$$
 and hence prove that

 $|x| = \begin{cases} 1-x^2, |x| < 1 \end{cases}$ and hence prove that

 $|x| = \begin{cases} \frac{\sin x}{3} - x \cos x \\ \cos x \end{vmatrix} = \frac{3\pi}{16}$

Soh:

 $|x| = \frac{1}{\sqrt{2\pi}} \int_{-1}^{1} (1-x^2) e^{-\frac{1}{2}x} dx$
 $|x| = \frac{1}{\sqrt{2\pi}} \int_{-1}^{1} (1-x^2) (\cos x + 9.5\% x) dx$
 $|x| = \frac{1}{\sqrt{2\pi}} \int_{-1}^{1} (1-x^2) (\cos x + 9.5\% x) dx$
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 $|x| = \frac{1}{\sqrt{2\pi}} \int_{-1}^{1$





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Figure 1 Test of Sins - Stocs of Cos series as

$$= \frac{1}{\sqrt{2\pi T}} \int_{-\infty}^{\infty} 2 \sqrt{\frac{2}{TT}} \int_{-\infty}^{\infty} F(s) e^{-9s \cdot x} ds$$

$$= \frac{2}{\sqrt{2\pi T}} \int_{-\infty}^{\infty} 2 \sqrt{\frac{2}{TT}} \int_{-\infty}^{\infty} \frac{Sins - Stocs}{S^{2}} (\cos sx - 9 Sin Sx) ds$$

$$= \frac{2}{\sqrt{2}} \int_{-\infty}^{\infty} (\frac{Sins - Stocs}{S^{2}}) (\cos sx ds)$$

$$- i \int_{-\infty}^{\infty} (\frac{Sins - Stocs}{S^{2}}) (\cos sx ds)$$

$$= \frac{4}{\sqrt{2}} \int_{-\infty}^{\infty} (\frac{Sins - Stocs}{S^{2}}) (\cos sx ds)$$

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$$= \frac{4}{\sqrt{2}} \int_{-\infty}^{\infty} (\frac{Sins - Stocs}{S^{2}}) (\cos sx ds)$$

$$= \frac{3T}{\sqrt{2}} \int_{-\infty}^{\infty} (\frac{Sins - Stocs}{S^{2}}) (\cos sx ds)$$

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