



**DEPARTMENT OF MATHEMATICS**

**UNIT II**  
**PART – C**

1. Solve :  $(3D^2 - D + 14)y = 8e^{2x} + \cos 4x.$

2. Solve :  $(D^2 - 4D + 13)y = e^{2x} \sin 3x.$

3. Solve :  $\frac{d^2y}{dx^2} + \frac{dy}{dx} + y = xe^x.$

4. Solve :  $y'' + y = \sin^2 x.$

5. Solve :  $(D^2 + 4)y = 4e^{2x} \sin 3x.$

6. Solve :  $(D^2 - 3D + 2)y = e^x + x^2.$

7. Solve :  $(D^2 - 2D + 1)y = e^x \sin 3x.$

8. Solve :  $(D^2 + 4D + 3)y = 2e^{-x}(x^2 + 2).$

9. Solve :  $\frac{dx}{dt} + 2y = \sin 2t, \frac{dy}{dt} - 2x = \cos 2t.$

10. Solve :  $(x^2 D^2 - 7xD + 12)y = x.$

11. Solve :  $x^2 \frac{d^2y}{dx^2} + x \frac{dy}{dx} + y = \log x \sin(\log x).$

12. Solve :  $x^2 \frac{d^2y}{dx^2} + 5x \frac{dy}{dx} + 4y = x^2.$

13. Solve :  $x^2 \frac{d^2y}{dx^2} + 4x \frac{dy}{dx} + 2y = x \log x.$

14. Solve :  $(x^2 D^2 + xD + 1)y = \sin(2\log x) \sin(\log x).$

15. Solve :  $\frac{d^2y}{dx^2} + 4 \frac{dy}{dx} + 4y = e^{-2x} + e^{3x} \sin x.$

16. Solve :  $\frac{dx}{dy} - y = t, \frac{dy}{dt} + x = t^2$ .

17. Solve :  $\frac{d^2y}{dx^2} - 4\frac{dy}{dx} - 4y = e^{2x} + \cos 2x$ .

18. Solve :  $\frac{d^2y}{dx^2} + y = \sec x$ .

19. Solve :  $\frac{d^2y}{dx^2} + a^2y = \tan ax$ .

20. Solve the equation  $\frac{d^2y}{dx^2} + 4y = \tan 2x$  by the method of variation of parameters.

21. Solve :  $\frac{d^2y}{dx^2} - y = \frac{2}{1+e^x}$  using the method of variation of parameters.

22. Find the particular integral of  $y'' + 7y' - 8y = e^{2x}$  by the method of variation of parameters.

23. Solve  $\frac{d^2y}{dx^2} + y = x \cos x$  by the method of variation of parameters.

24. Solve :  $y'' + 9y = \cot 3x$ .

25. Solve :  $(D^2 - 4D + 13)y = e^{2x} \sin 3x$ .

26. Solve :  $y'' + 2y' + y = x \cos x$ .

27. Solve :  $y'' + 9y = \cot 3x$ .

28. Solve :  $(x^2 D^2 - 3xD + 5)y = x^2 \sin(\log x)$ .

29. Solve :  $(x^2 D^2 - xD + 1)y = \left(\frac{\log x}{x}\right)^2$ .

30. Solve :  $x^2 y'' - 2xy' - 4y = x^4$ .

31. Solve :  $x^2 \frac{d^2y}{dx^2} - 3x \frac{dy}{dx} - 5y = \sin(\log x)$ .

32. Solve :  $x^2 \frac{d^2y}{dx^2} + x \frac{dy}{dx} + y = 4 \sin(\log x)$ .

33. Solve :  $(x^2 D^2 - 2xD - 4)y = 32(\log x)^2$ .

34. Solve :  $(D^2 - 1)y = x^2 + e^{-2x} \sin 2x$ .

35. Solve the system of equation  $\frac{dx}{dt} + 5x - 2y = t, \frac{dy}{dt} + 2x + y = 0$ .

36. Solve the system of equation  $\frac{dx}{dt} + y = e^t, x - \frac{dy}{dt} = t$ .

37. Solve :  $\frac{dx}{dt} - \frac{dy}{dt} - y = e^{-t}; x + \frac{dy}{dt} - y = e^{2t}$ .

38. Solve :  $\frac{dx}{dt} + 2x - 3y = t, \frac{dy}{dt} - 3x + 2y = e^{2t}$ .

39. Solve the system of equation  $\frac{dx}{dt} + 2y = -\sin t, \frac{dy}{dt} - 2x = \cos t$ .

40. Solve the simultaneous equation  $\frac{dx}{dt} - \frac{dy}{dt} + 2y = \cos 2t, \frac{dx}{dt} + \frac{dy}{dt} - 2x = \sin 2t$ .

41. Solve the simultaneous equation  $Dx + y = \sin 2t; -x + Dy = \cos 2t$ .

42. Solve the simultaneous equation  $\frac{dx}{dt} + 2x - 3y = 5t, \frac{dy}{dt} - 3x + 2y = 2e^{2t}$ .

43. Solve  $\frac{dx}{dt} + y = \sin t, \frac{dy}{dt} + x = \cos t$  given that  $x = 2, y = 0$  when  $t = 0$ .

44. Solve  $\frac{dx}{dt} + 2y = 5e^t, \frac{dy}{dt} - 2x = 5e^t$ .

++++++