# DEPARTMENT OF INFORMATION TECHNOLOGY 

19ITT101-PROGRAMMING IN C AND DATA STRUCTURES
I YEAR - II SEM

UNIT 4 - STACK AND QUEUE
TOPIC 6 - Expression Parsing

## Expression Parsing

The way to write arithmetic expression is known as a notation. An arithmetic expression can be written in three different but equivalent notations, i.e., without changing the essence or output of an expression.
$>$ These notations are -
$>$ Infix Notation
$>$ Prefix Notation
$>$ Postfix Notation

## Infix Notation

$>$ infix notation, where operators are used in-between operands.
$>$ It is easy for us humans to read, write, and speak in infix notation but the same does not go well with computing devices.
$>$ An algorithm to process infix notation could be difficult and costly in terms of time and space consumption.

$$
\begin{aligned}
& >\mathrm{a}-\mathrm{b}+\mathrm{c} \\
& >\mathrm{a}, \mathrm{~b}, \mathrm{c} \rightarrow \text { operands } \\
& >-,+\rightarrow \text { operator }
\end{aligned}
$$

## Prefix Notation

$>$ In this notation, operator is prefixed to operands, i.e. operator is written ahead of operands.
$>$ For example, + ab.
$>$ This is equivalent to its infix notation $\mathrm{a}+\mathrm{b}$. Prefix notation is also known as Polish Notation.

## Postfix Notation

$>$ This notation style is known as Reversed Polish Notation.
$>$ In this notation style, the operator is postfixed to the operands i.e., the operator is written after the operands.
$>$ For example, $a b+$. This is equivalent to its infix notation $a+b$.

## Precedence

$>$ When an operand is in between two different operators, which operator will take the operand first, is decided by the precedence of an operator over others.

$$
a+b^{*} c \rightarrow a+\left(b^{*} c\right)
$$

$>$ multiplication operation has precedence over addition, $\mathrm{b} * \mathrm{c}$ will be evaluated first. A table of operator precedence is provided later.

## Associativity

$>$ Associativity describes the rule where operators with the same precedence appear in an expression.
$>$ For example, in expression $\mathrm{a}+\mathrm{b}-\mathrm{c}$, both + and - have the same precedence, then which part of the expression will be evaluated first, is determined by associativity of those operators.
$>$ Here, both + and - are left associative, so the expression will be evaluated as (a $+\mathrm{b})-\mathrm{c}$.

$$
\begin{aligned}
& >\mathrm{a}+\mathrm{b}-\mathrm{c} \rightarrow(\mathrm{a}+\mathrm{b})-\mathrm{c} \\
& >\mathrm{a}+\mathrm{b}^{*} \mathrm{c} \rightarrow(\mathrm{a}+\mathrm{b})^{*} \mathrm{c}
\end{aligned}
$$

$>\mathrm{a}+\mathrm{b}^{*} \mathrm{c}$, the expression part $\mathrm{b}^{*} \mathrm{c}$ will be evaluated first, with multiplication as precedence over addition. We here use parenthesis for $\mathrm{a}+\mathrm{b}$ to be evaluated first, like $(a+b) * c$

| Sr.No. | Operator | Precedence | Associativity |
| :---: | :---: | :---: | :---: |
| 1 | Exponentiation ^ | Highest | Right Associative |
| 2 | Multiplication (*) \& Division (/) | Second Highest | Left Associative |
| 3 | Addition $(+) \&$ Subtraction ( - ) | Lowest | Left Associative |

## Infix to post fix and prefix

| Sr.No. | Infix Notation | Prefix Notation | Postfix Notation |
| :---: | :---: | :---: | :---: |
| 1 | $a+b$ | $+a b$ | $a b+$ |
| 2 | $(a+b) * c$ | $*+a b c$ | $a b+c *$ |
| 3 | $a *(b+c)$ | $* a+b c$ | $a b c+*$ |
| 4 | $a / b+c / d$ | $+/ a b / c d$ | $a b / c d /+$ |
| 5 | $(a+b) *(c+d)$ | $*+a b+c d$ | $a b+c d+*$ |
| 6 | $((a+b) * c)-d$ | $-*+a b c d$ | $a b+c * d-$ |

