

# SNS COLLEGE OF TECHNOLOGY



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COIMBATORE-641 035, TAMIL NADU

## DEPARTMENT OF ELECTRONICS AND COMMUNICATION ENGINEERING

**Course Name: 23ECT203 LINEAR INTEGRATED CIRCUITS**

**II YEAR/VI SEMESTER**

**UNIT III –ANALOG MULTIPLIER AND PLLR**

**Topic :Analog Multiplier using Emitter Coupled Transistor Pair - Gilbert Multiplier cell**

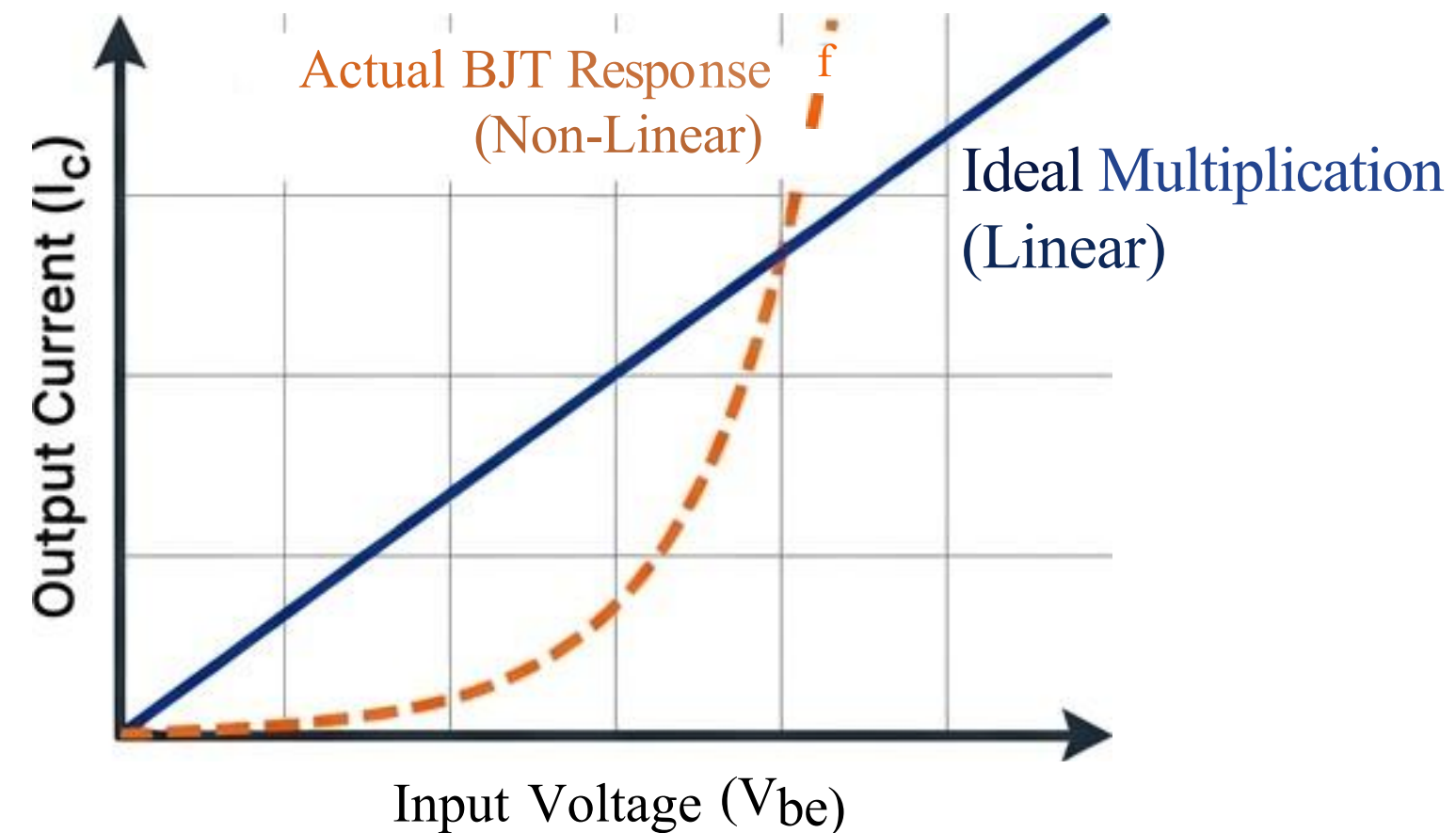
# Design Thinking Stage 1: Empathize

## The User Need in Communication Systems

- The Need: Precise control over signal amplitude and frequency mixing.
- The Context: Simple resistive or diode circuits cause signal distortion.
- The Goal: A 'Perfect Mixer' capable of handling positive and negative signals simultaneously (Four-Quadrant Operation).

# Design Thinking Stage 2: Define

## The Problem of Non-Linearity



Physics Problem: BJTs have an exponential V-I characteristic.

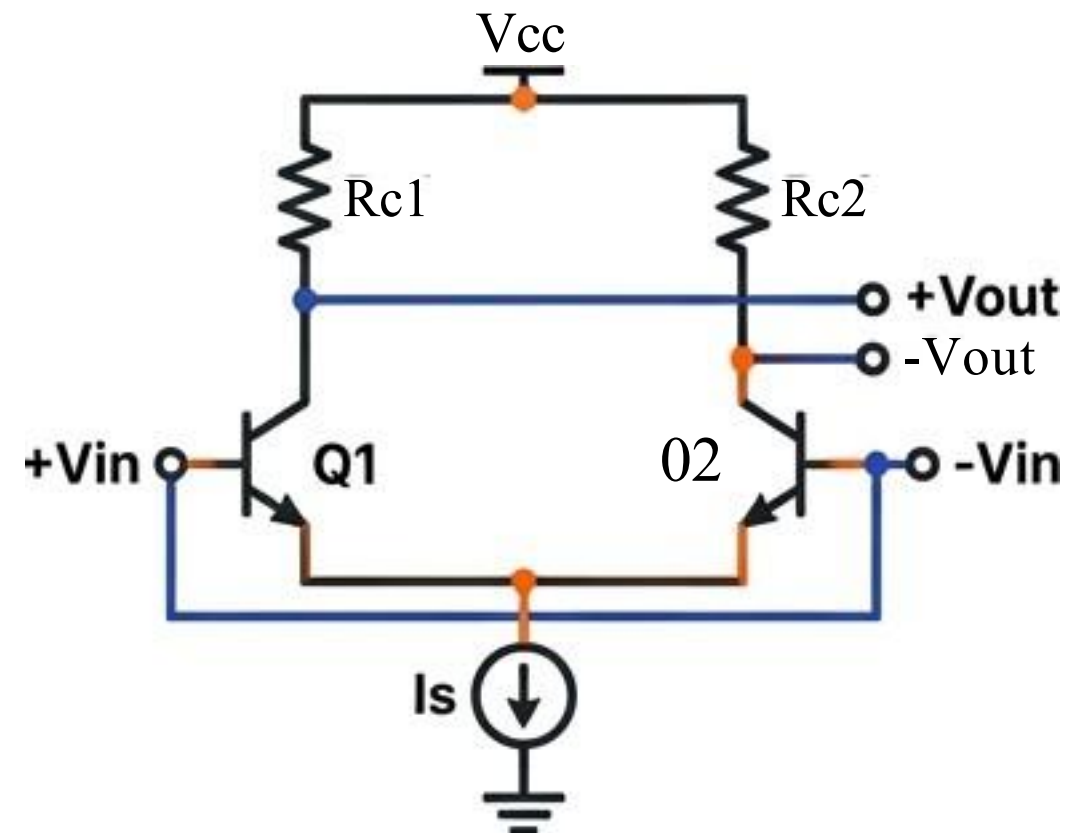
$$\text{Equation: } I_c = I_s \cdot e^{(V_{be}/V_t)}$$

Challenge: How to achieve linear multiplication using non-linear devices?

Requirement: Must operate in all 4 quadrants (Positive/Negative inputs).

# Design Thinking Stage 3: Ideate

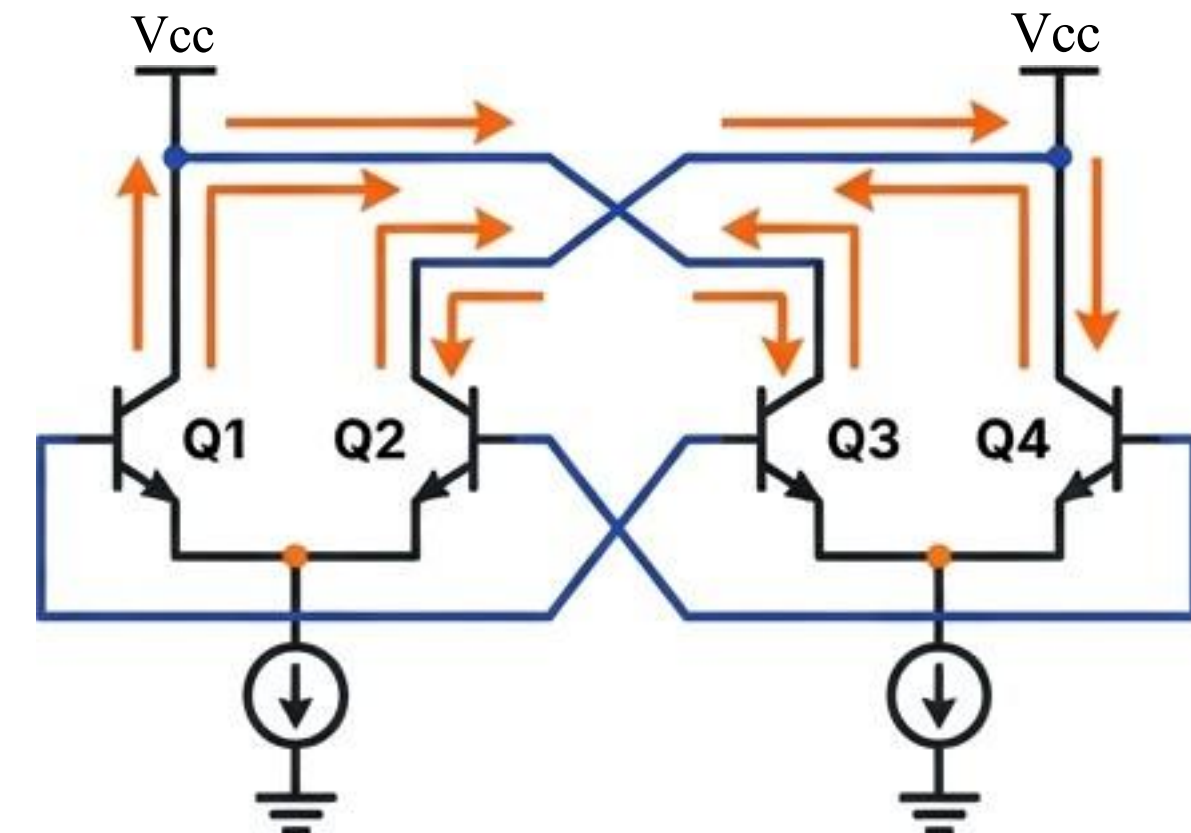
Ideation A



Standard Differential Pair Good

for gain, but limited linearity.

Ideation B

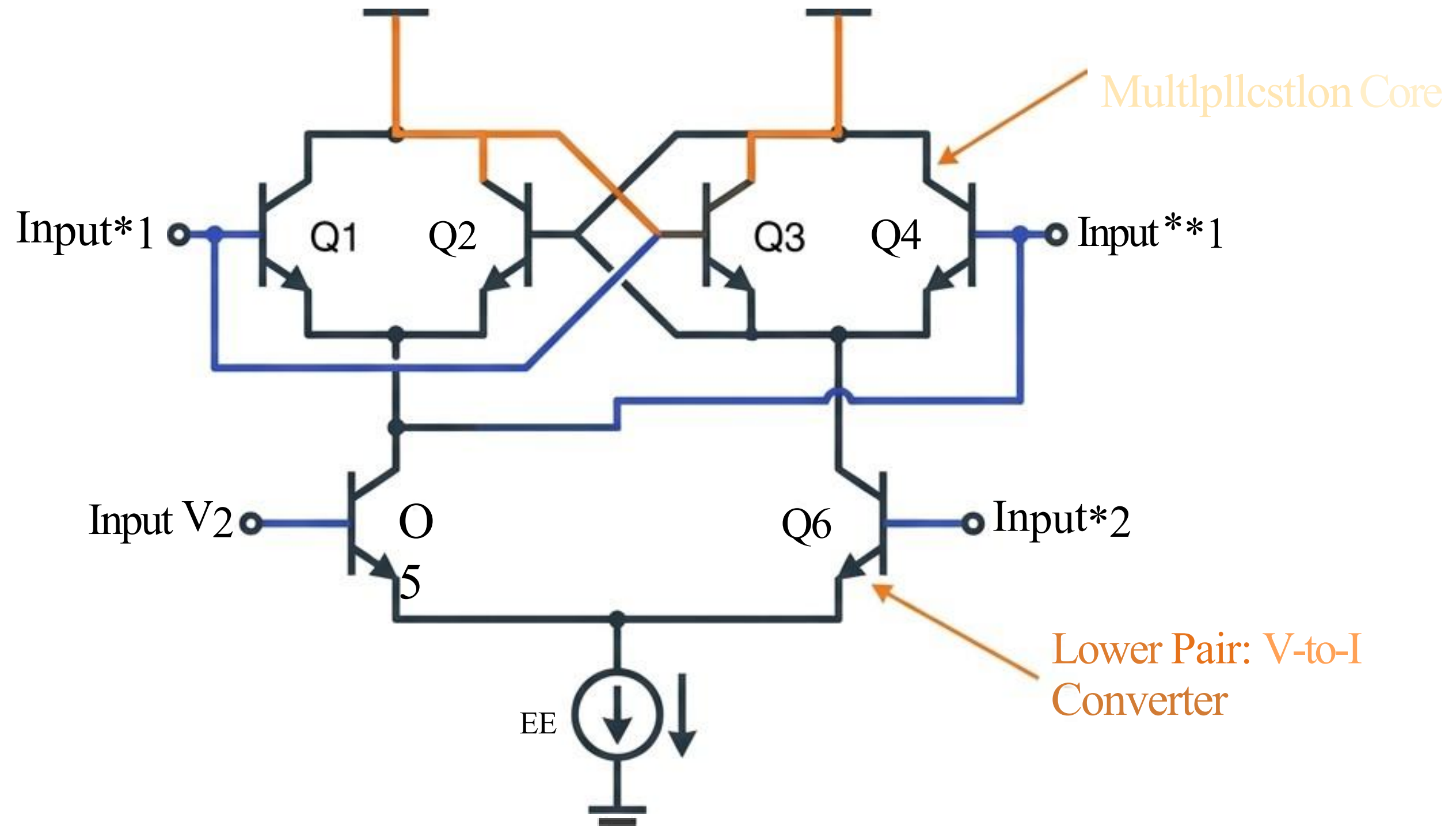


Cross-Coupled Architecture

The Breakthrough: Cancellation of non-linear terms.

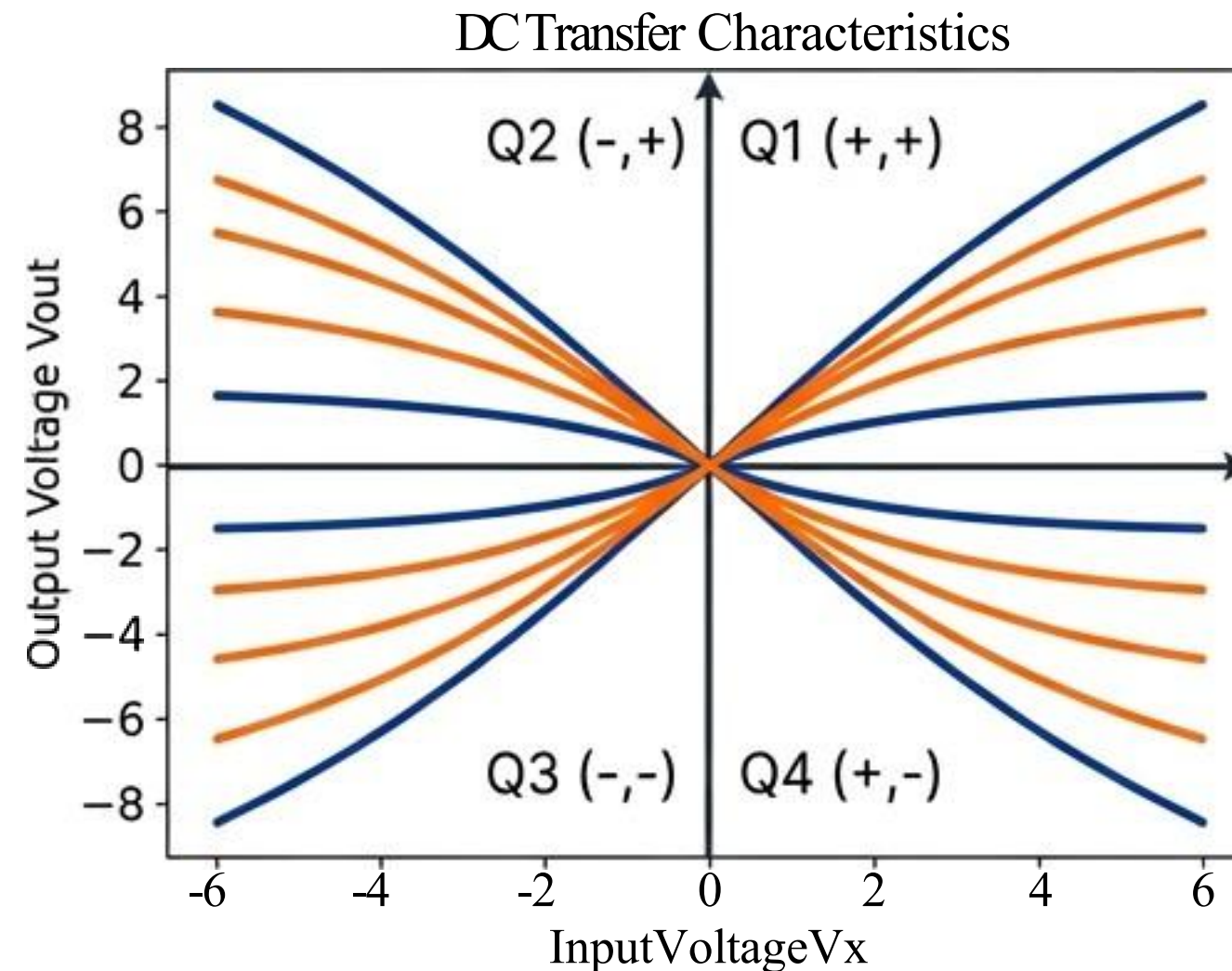
- Concept: Variable Transconductance.
- Solution: Cross-coupling two pairs allows the non-linear exponential terms to subtract and cancel each other.
- Mechanism: Current Steering Logic.

# Design Thinking Stage 4: Prototype



# Design Thinking Stage 5: Test

## Validating Four-Quadrant Operation



- Verification: The circuit multiplies successfully for both positive and negative polarities of inputs.
- Linearity Check: Response is linear within the range of Thermal Voltage ( $V_t$ ) (in JetBrains Mono).
- Result: The cross-coupled structure effectively linearizes the hyperbolic tangent ( $\tanh$ ) response (in JetBrains Mono).

# Key Parameters

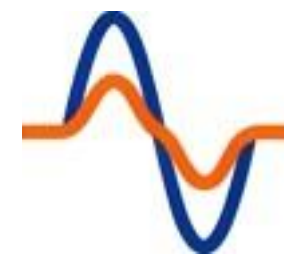


## Scale Factor (K)

The proportionality constant. Typical value:  $1/10 \text{ V}^{-1}$ .

$$V_{out} = \frac{V_x \cdot K}{V_y}$$

=



## Differential Gain

High ability to reject common-mode noise.



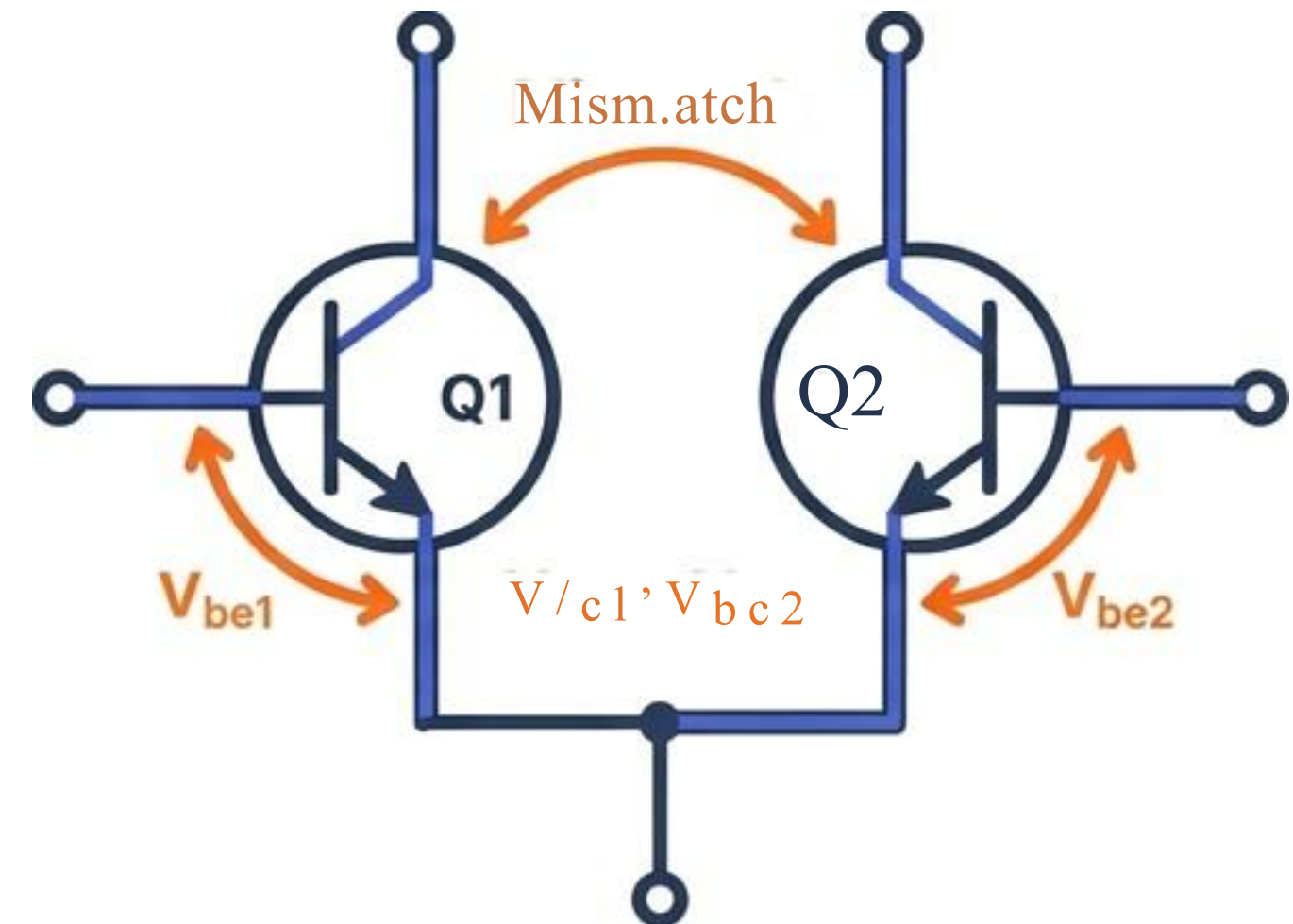
## Linearity & Range

Percentage deviation from ideal product.

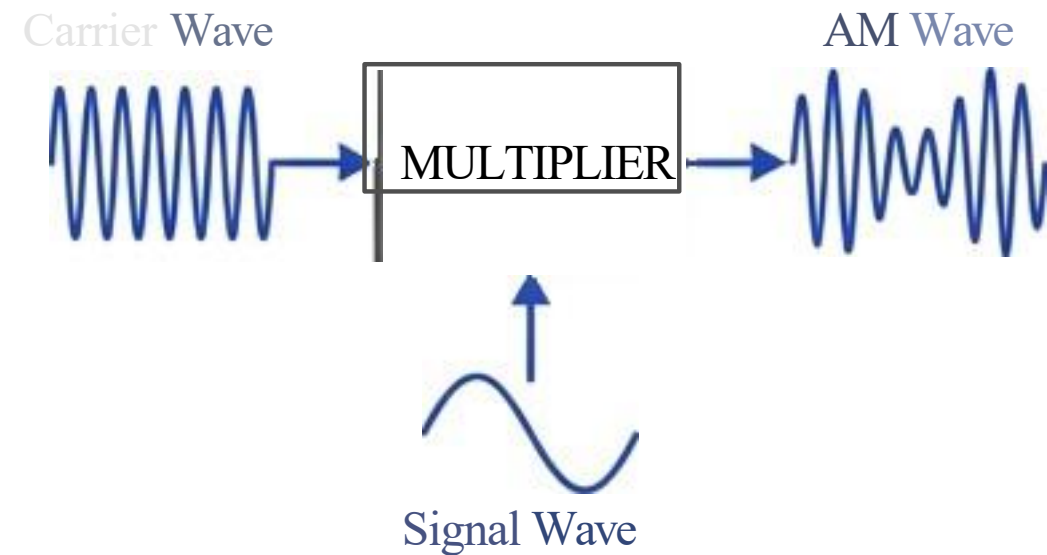
Dynamic range limited by  $V_{cc}$  and bias currents.

# Practical Limitations

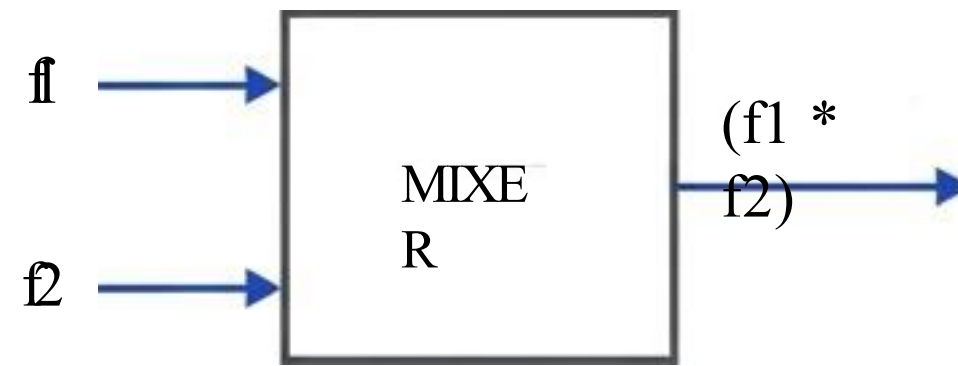
- Device Mismatch: Slight manufacturing differences in Transistor Beta or  $V_{be}$  cause DC Offset Errors (Output is not zero when input is zero).
- Temperature Drift: Transconductance ( $g_m$ ) depends on Thermal Voltage ( $V_t = kT/q$ ) (rendered in 3 etBrains hono).  
—As Temperature rises  $\rightarrow$  Gain changes.
- Mitigation: External trimming resistors and pre-distortion circuits are used in commercial ICs (e.g., MC1496).



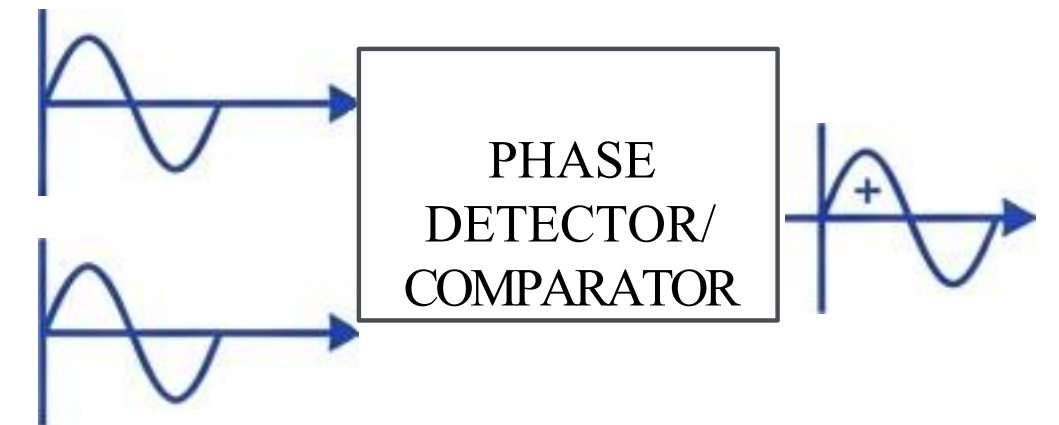
# Real-World Applications



Amplitude Modulation (AM) & DSB-SC.

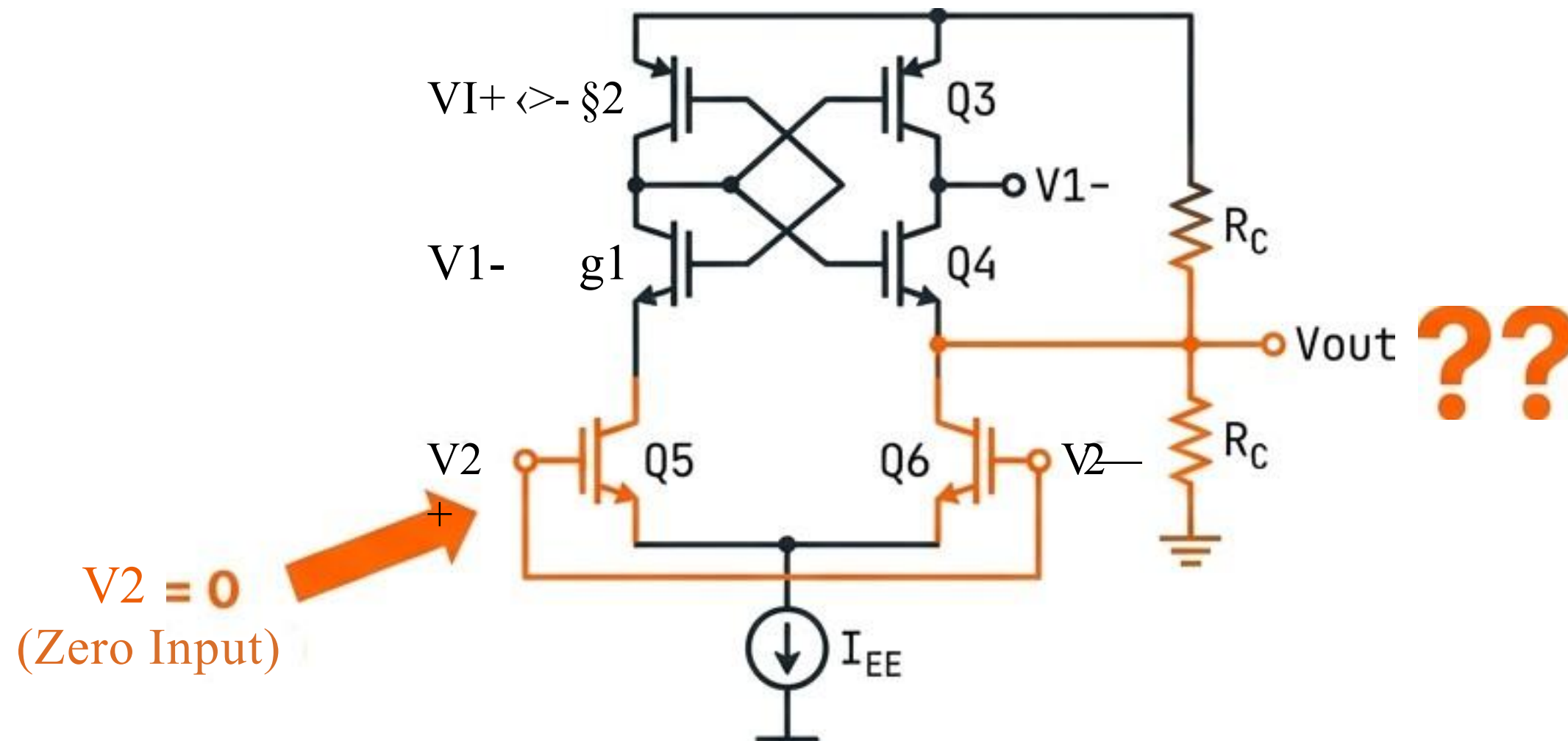


RF Communication Receivers (Superheterodyne).



Phase Locked Loops (PLL) for signal synchronization.

# Class Activity: Circuit Analysis

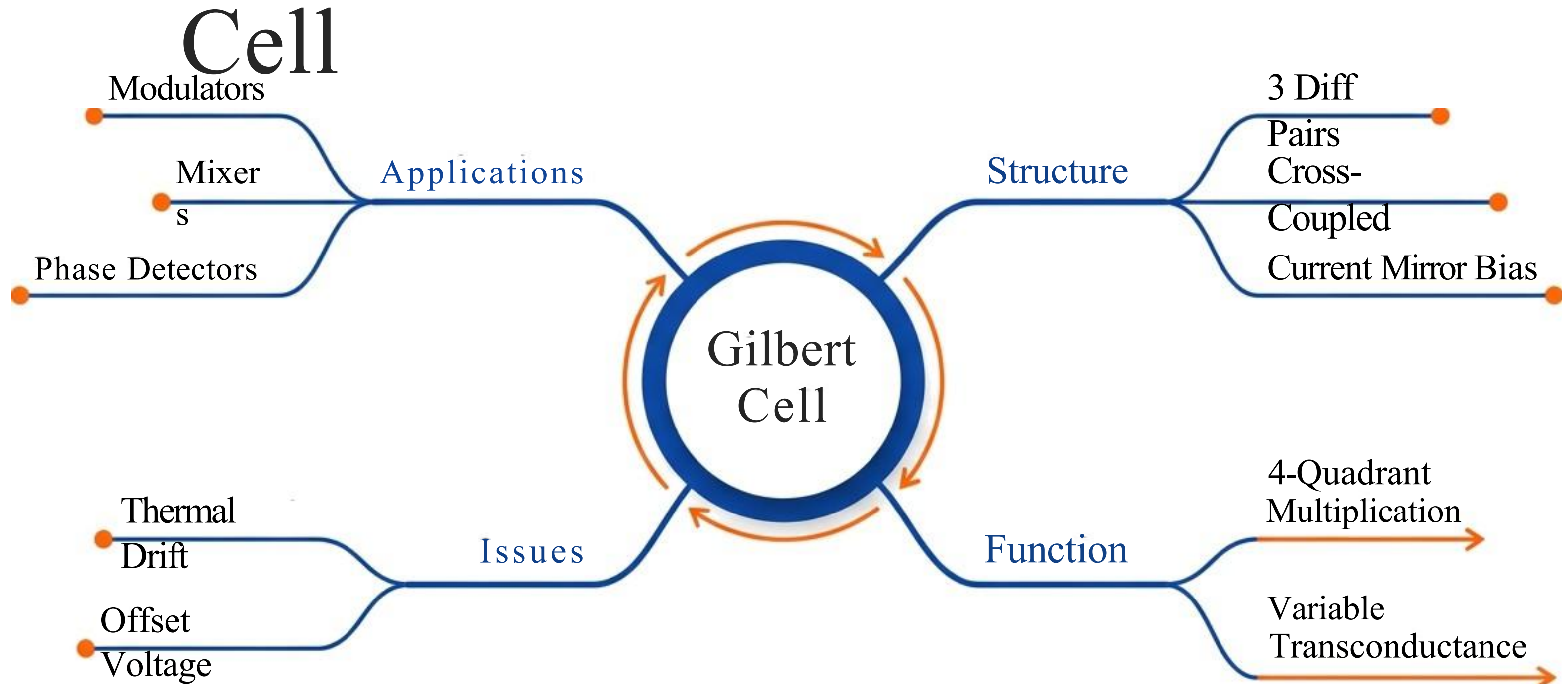


Challenge: Consider the Gilbert Cell Schematic.

Condition: If the differential input to the bottom pair ( $V_2$ ) is ZERO...

Question: What is the AC output voltage, regardless of what Input  $V_1$  is doing?

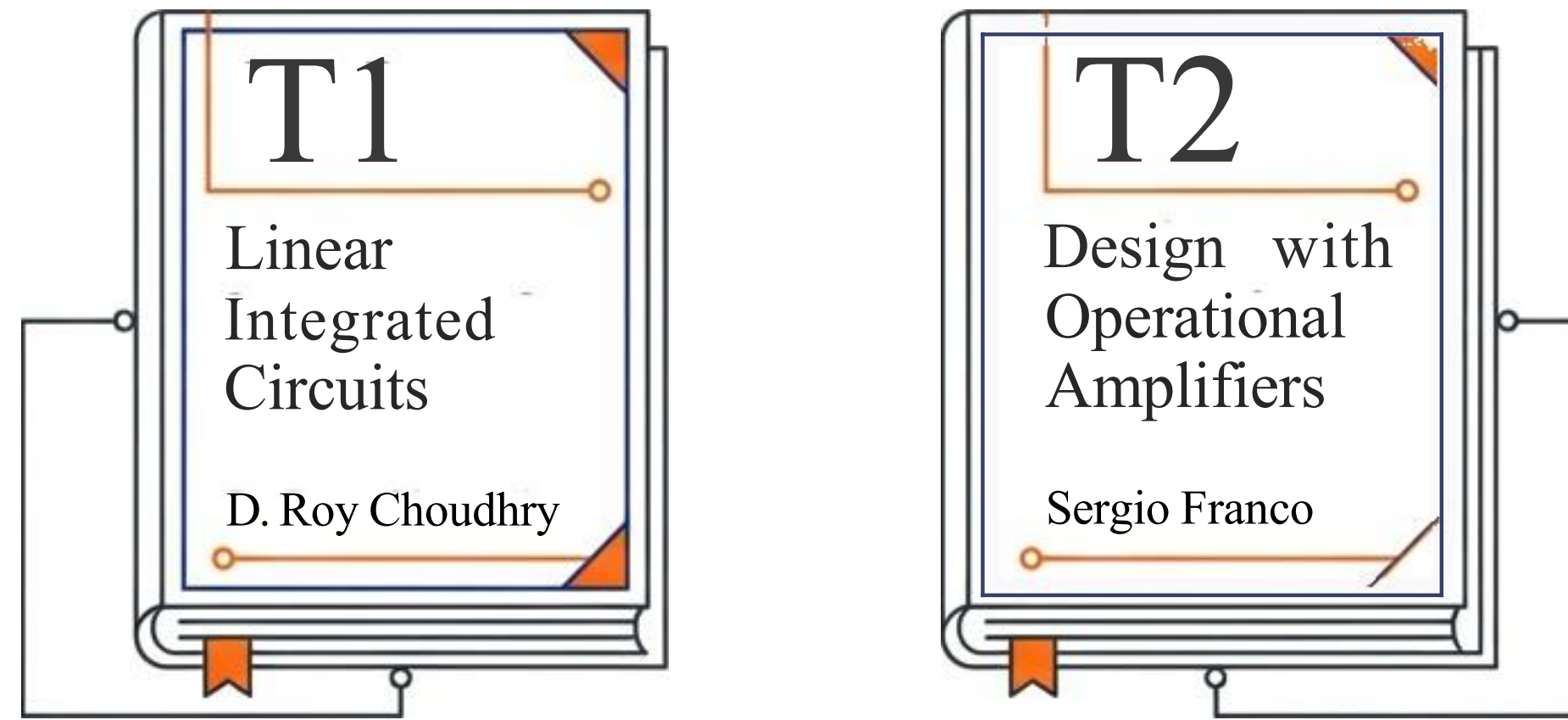
# Mind Map: Gilbert Multiplier



# Assessment

1. Why is 'cross-coupling' used in the Gilbert Cell?  
(Ans: **To cancel non-linear** terms)
2. What is the typical value of the scale factor K?  
(Ans: 1/10)
3. Name one practical **limitation** of this circuit.  
(Ans: **Temperature drift or Offset**)
4. In which quadrant(s) does the Gilbert cell operate?  
(Ans: **All** four)

# References



T1: D. Roy Choudhry, Shail Jain, 'Linear integrated Circuits', New Age International Pvt. Ltd., Fifth edition 2018.

T2: Sergio Franco, 'Design with Operational Amplifiers and Analog integrated Circuits', Fourth Edition, Tata McGraw-Hill, 2014.

W1: NPTEL Course - <https://nptel.ac.in/courses/108/106/108106153>

# Thank you